

# Package ‘MBQN’

January 29, 2025

**Version** 2.19.0

**Title** Mean/Median-balanced quantile normalization

**Description** Modified quantile normalization for omics or other matrix-like data distorted in location and scale.

**License** GPL-3 + file LICENSE

**Depends** R (>= 3.6)

**Imports** stats, graphics, utils, limma (>= 3.30.13),  
SummarizedExperiment (>= 1.10.0), preprocessCore (>= 1.36.0),  
BiocFileCache, rappdirs, xml2, RCurl, ggplot2, PairedData,  
rmarkdown

**Suggests** knitr

**biocViews** Normalization, Preprocessing, Proteomics, Software

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**BugReports** <https://github.com/arianeschad/MBQN/issues>

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|                   |                                      |
|-------------------|--------------------------------------|
| example_NApattern | <i>Missing value pattern dataset</i> |
|-------------------|--------------------------------------|

---

## Description

An exemplary matrix of a missing value (MV) pattern extracted from LFQ intensities of the proteinGroups.txt dataset from PXD001584 [1].

## Usage

```
example_NApattern
```

## Format

A matrix of zero and ones with 1264 rows and 18 columns; 0 means MV, 1 means no MV.

## Author(s)

Ariane Schad

**Source**

<https://www.ebi.ac.uk/pride/archive/projects/PXD001584>

**References**

[1] Ramond E, et al. Importance of host cell arginine uptake in Francisella phagosomal escape and ribosomal protein amounts. Mol Cell Proteomics. 2015 14(4):870-881

---

|            |  |
|------------|--|
| getKminmax | <i>Get the k largest/smallest elements</i> |
|------------|--|

---

**Description**

Extract the k largest or smallest values and their indices for each column of a matrix.

**Usage**

```
getKminmax(x, k, flag = "max")
```

**Arguments**

|      |  |
|------|--|
| x    | a data matrix or data frame.   |
| k    | an integer specifying the number of extreme values. Must be $\leq$ nrows(x). |
| flag | use "min" or "max" (default) to select smallest or largest elements.         |

**Details**

Order the values of each column of x and determine the k smallest (flag = "min") or largest (flag = "max") values and their indices. NA's in the data are ignored.

**Value**

List with elements:

|        |                                   |
|--------|-----------------------------------|
| ik     | indices of ordered extreme values |
| minmax | ordered extreme values.           |

**Author(s)**

Ariane Schad

**References**

Brombacher, E., Schad, A., Kreutz, C. (2020). Tail-Robust Quantile Normalization. BioRxiv.

**Examples**

```
# Create a data matrix
x <- matrix(c(5,2,3,NA,4,1,4,2,3,4,6,NA,1,3,1),ncol=3)
# Get indices of the 5 largest values in each column
getKminmax(x, k = 5, "max")
```

---

getPvalue

*Calculates Pitman-Morgan variance test on two matrices*

---

**Description**

Calculates Pitman-Morgan variance test on two matrices

**Usage**

```
getPvalue(mtx1, mtx2)
```

**Arguments**

mtx1            Matrix with samples in columns and features in rows  
 mtx2            Matrix with samples in columns and features in rows

**Value**

Data frame with p values and statistics

**Examples**

```
set.seed(30)
n <- 20
m <- 20
mtx1 <- matrix(rnorm(m * n), m, n)
mtx2 <- mbqn(mtx1, FUN = "mean")
getPvalue(mtx1, mtx2)
```

---

mbqn

*Mean/Median-balanced quantile normalization*

---

**Description**

Modified quantile-normalization (QN) of a matrix, e.g., intensity values from omics data or other data sorted in columns. The modification prevents systematic flattening of features (rows) which are rank invariant (RI) or nearly rank invariant (NRI) across columns, for example features that populate mainly the tails of the intensity distribution or features that separate in intensity.

**Usage**

```
mbqn(  
  x,  
  FUN = "mean",  
  na.rm = TRUE,  
  method = "limma",  
  offsetmatrix = FALSE,  
  verbose = FALSE  
)
```

**Arguments**

|              |   |
|--------------|---|
| x            | a data matrix, where rows represent features, e.g. of protein abundance, and columns represent groups or samples, e.g. replicates, treatments, or conditions.   |
| FUN          | a function like mean, median (default), a user defined function, or a numeric vector of weights with length nrow(x) to balance each feature across samples. Functions can be parsed also as characters. If FUN = NULL, features are not balanced, i.e. normal QN is used. |
| na.rm        | logical indicating to omit NAs in the computation of feature mean.  |
| method       | character specifying function for computation of quantile normalization; "limma" (default) for normalizeQuantiles() from the limma package or "preprocessCore" for normalize.quantiles() from the preprocessCore package.   |
| offsetmatrix | logical indicating if offset matrix should be used instead of offset vector specifying offset for each row  |
| verbose      | logical indicating to print messages.   |

**Details**

Balance each matrix row by subtracting its feature offset computed with FUN, e.g. the median; apply quantile-normalization and add the feature means to the normalized matrix. For further details see [4]. For quantile normalization with the "limma" package see [1,2] and for the preprocessCore package see [3].

**Value**

Normalized matrix

**Author(s)**

Ariane Schad

**References**

- [1] Smyth, G. K., and Speed, T. P. (2003). Normalization of cDNA microarray data. *Methods* 31, 265–273.
- Ritchie, M.E., Phipson, B., Wu, D., Hu, Y., Law, C.W., Shi, W., and Smyth, [2] G.K. (2015). limma powers differential expression analyses for RNA-sequencing and microarray studies. *Nucleic Acids Research* 43(7), e47.

[3] Bolstad B. M. (2016). preprocessCore: A collection of pre-processing functions. R package version 1.36.0. <https://github.com/bmbolstad/preprocessCore>

[4] Brombacher, E., Schad, A., Kreutz, C. (2020). Tail-Robust Quantile Normalization. BioRxiv.

### See Also

[mbqnNRI\(\)](#), [mbqnGetNRIfeatures\(\)](#).

### Examples

```
## Compute mean and median balanced quantile normalization
X <- matrix(c(5,2,3,NA,4,1,4,2,3,4,6,NA,1,3,1),ncol=3)
mbqn(X, mean) # Use arithmetic mean to center features
mbqn(X, median) # Use median to center features
mbqn(X, "median")

## Use user defined array of weights for averaging
wt <- c(1,3,1)/5 # Weights for each sample
user_array <- apply(X,1,weighted.mean, wt ,na.rm =TRUE)
mbqn(X, user_array)
```

---

mbqnBoxplot

*Combined box plot and line plot*

---

### Description

Create a box-and-whisker plot of a data matrix and plot selected features and/or additional user-defined data on top of it.

### Usage

```
mbqnBoxplot(mtx, irow = NULL, vals = NULL, add.leg = TRUE, ...)
```

### Arguments

|         |  |
|---------|--|
| mtx     | a matrix or data frame.  |
| irow    | index or vector of row indices of matrix features to plot on top of the boxplot.   |
| vals    | numeric, array, matrix, or data frame of features with length <code>ncol(mtx)</code> to plot on top of the boxplot.  |
| add.leg | add legend to plot.  |
| ...     | additional arguments passed to the plot functions, e.g. <code>xlab</code> , <code>ylab</code> , <code>main</code> , <code>ylim</code> , <code>type</code> , <code>las</code> . |

### Details

This function calls `graphics::boxplot`. Groups are represent by matrix columns. Selected rows/features or user-defined arrays are plot on top of the box plot. Missing values are ignored.

**Value**

Figure.

**Author(s)**

Ariane Schad

**References**

Brombacher, E., Schad, A., Kreutz, C. (2020). Tail-Robust Quantile Normalization. BioRxiv.

**Examples**

```
## Create boxplot of quantile normalized data matrix and plot
## feature from median balanced quantile normalization on top of it.
X <- matrix(c(5,2,3,NA,4,1,4,2,3,4,6,NA,1,3,1),ncol=3) # Create data matrix
# Quantile normalization
qn.dat <- mbqn(x=X,FUN = NULL ,na.rm = TRUE)
# Median balanced quantile normalization
mbqn.dat <- mbqn(x=X,FUN = median ,na.rm = TRUE)
## Create boxplot:
plot.new()
mbqnBoxplot(qn.dat,irow = 1, vals = mbqn.dat[1,], type = "b")
```

---

mbqnGetIntersect      *Helper function for mbqnGetThreshold*

---

**Description**

Helper function for mbqnGetThreshold

**Usage**

```
mbqnGetIntersect(combined_qn, combined_mbqn, threshold, plot = TRUE)
```

**Arguments**

|               |  |
|---------------|--|
| combined_qn   | Data frame containing RI, p value and statistic calculated for QN  |
| combined_mbqn | Data frame containing RI, p value and statistic calculated for MBQN  |
| threshold     | Significance threshold for p value of Pitman-Morgan variance test  |
| plot          | Boolean values if logistic regression curves that are used to calculate intersection point should be plotted |

**Value**

threshold value

---

mbqnGetNRIfeatures      *Identify rank invariant (RI) and nearly rank invariant (NRI) features*

---

### Description

Compute the rank frequency of each feature of a matrix and identify NRI/RI features.

### Usage

```
mbqnGetNRIfeatures(x, low_thr = 0.5, method = NULL, verbose = TRUE)
```

### Arguments

|         |   |
|---------|---|
| x       | a data matrix. Rows represent features, e.g. protein abundances; columns represent samples.   |
| low_thr | a value between [0 1]. Features with RI frequency $\geq$ low_thr are considered as NRI/RI; default 0.5.   |
| method  | character specifying function for computation of quantile normalization; "limma" (default) for normalizeQuantiles() from the limma package or "preprocessCore" for normalize.quantiles() from the preprocessCore package. |
| verbose | logical indicating to print messages.   |

### Details

Quantile normalize the data matrix and sort ranks. Determine the maximum frequency of equal rank across all columns for each feature. Features with maximum frequency above the user-defined threshold are declared as nearly rank invariant.

### Value

A list with elements:

|              |  |
|--------------|--|
| p            | a matrix with the rank invariance frequencies <code>ri.freq</code> and the sample coverage <code>sample.coverage</code> for all detected RI/NRI features |
| max_p        | maximum rank invariance frequency in percent   |
| ip           | index of feature with maximum rank invariance frequency  |
| nri          | table of the rank invariance frequencies in percent for each NRI/RI feature  |
| var0_feature | indices of features with zero sample variance after QN   |
| low_thr      | threshold used for NRI/RI detection from RI frequency.   |

### Author(s)

Ariane Schad



## References

Brombacher, E., Schad, A., Kreutz, C. (2020). Tail-Robust Quantile Normalization. BioRxiv.

## See Also

[mbqnPlotRI\(\)](#) for visualization of detected NRI/RI features.

## Examples

```
## Check data matrix for RI and NRI features
set.seed(1234)
x <- mbqnSimuData("omics.dep")
RI <- mbqnGetNRIfeatures(x, low_thr = 0.5, verbose = FALSE)
mbqnPlotRI(RI)
```

---

|                  |   |
|------------------|---|
| mbqnGetThreshold | <i>Calculates the rank invariance threshold from which on MBQN should be used instead of 'classical' QN</i> |
|------------------|---|

---

## Description

Calculates the rank invariance threshold from which on MBQN should be used instead of 'classical' QN

## Usage

```
mbqnGetThreshold(mtx, meanMedian = "mean", plot = TRUE)
```

## Arguments

|            |  |
|------------|--|
| mtx        | Matrix with samples in columns and features in rows  |
| meanMedian | Offset function for the MBQN calculation   |
| plot       | Boolean values if logistic regression curves that are used to calculate intersection point should be plotted |

## Value

threshold value

## Examples

```
set.seed(30)
n <- 20
m <- 20
mtx <- matrix(rnorm(m * n), m, n)
mbqnGetThreshold(mtx)
```

mbqnNRI

*Selective mean/median-balanced quantile normalization***Description**

Quantile normalization of a data matrix where rank invariant (RI)/nearly rank invariant (NRI) rows/features or other user-selected rows are normalized by the mean/median-balanced quantile normalization.

**Usage**

```
mbqnNRI(
  x,
  FUN = "mean",
  na.rm = TRUE,
  method = NULL,
  low_thr = 0.5,
  index = NULL,
  offsetmatrix = FALSE,
  verbose = TRUE
)
```

**Arguments**

|              |   |
|--------------|---|
| x            | a data matrix, where rows represent features, e.g. of protein abundance, and columns represent groups or samples, e.g. replicates, treatments, or conditions.   |
| FUN          | a function like mean, median (default), a user defined function, or a numeric vector of weights with length nrow(x) to balance each feature across samples. Functions can be parsed also as characters. If FUN = NULL, features are not balanced, i.e. normal QN is used. |
| na.rm        | logical indicating to omit NAs in the computation of feature mean.  |
| method       | character specifying function for computation of quantile normalization; "limma" (default) for normalizeQuantiles() from the limma package or "preprocessCore" for normalize.quantiles() from the preprocessCore package.   |
| low_thr      | a value between [0 1]. Features with RI frequency $\geq$ low_thr are considered as NRI/RI; default 0.5.   |
| index        | an integer or a vector integers specifying the indices of selected rows.  |
| offsetmatrix | logical indicating if offset matrix should be used instead of offset vector specifying offset for each row  |
| verbose      | logical indicating to print messages.   |

**Details**

Selected rows and/or rows with rank invariance frequency  $\geq$  threshold are normalized with the mean/median-balanced quantile normalization. Remaining rows are quantile normalized without mean balancing.

**Value**

Normalized matrix.

**Author(s)**

Ariane Schad

**References**

Brombacher, E., Schad, A., Kreutz, C. (2020). Tail-Robust Quantile Normalization. BioRxiv.

**See Also**

[mbqn\(\)](#), [mbqnGetNRIfeatures\(\)](#).

**Examples**

```
## Quantile normalize a data matrix where
## nearly rank invariant (NRI) features are balanced
X <- matrix(c(5,2,3,NA,4,1,4,2,3,4,6,NA,1,3,1),ncol=3)
mbqnNRI(X, median,low_thr = 0.5) # Balance NRI features selected by threshold
mbqnNRI(X, median, index = c(1,2)) # Balance selected features
```

---

mbqnPlotAll

*Plot RI/NRI feature frequencies and normalized/unnormalized features*

---

**Description**

Check data matrix for rank invariant (RI) and nearly rank invariant (NRI) features/rows across samples and visualize result for different normalizations.

**Usage**

```
mbqnPlotAll(  
  x,  
  FUN = NULL,  
  low_thr = 0.5,  
  show_nri_only = FALSE,  
  verbose = TRUE,  
  ...  
)
```

**Arguments**

|                            |  |
|----------------------------|--|
| <code>x</code>             | a data matrix. Rows represent features, e.g. protein abundances; columns represent samples.  |
| <code>FUN</code>           | a function like mean, median (default), a user defined function, or a numeric vector of weights with length <code>nrow(x)</code> to balance each feature across samples. Functions can be parsed also as characters. If <code>FUN = NULL</code> , features are not balanced, i.e. normal QN is used. |
| <code>low_thr</code>       | a value between [0 1]. Features with RI frequency $\geq$ <code>low_thr</code> are considered as NRI/RI; default 0.5.   |
| <code>show_nri_only</code> | logical indicating to display only the RI/NRI detection graph.   |
| <code>verbose</code>       | logical indicating to print messages.  |
| <code>...</code>           | additional plot arguments passed to <code>mbqnBoxplot</code> , and <code>mbqnPlotRI</code> .   |

**Details**

Rank data and check if lower and upper intensity tails are dominated by few features. Apply quantile normalization without and with mean-balancing and check the standard deviation of normalized features located in the tails.

**Value**

A set of figures that display the detected RI/NRI features and a list with elements:

|                           |  |
|---------------------------|--|
| <code>p</code>            | a matrix with the rank invariance frequencies <code>ri.freq</code> and the sample coverage <code>sample.coverage</code> for all detected RI/NRI features |
| <code>max_p</code>        | maximum rank invariance frequency in percent   |
| <code>ip</code>           | index of feature with maximum rank invariance frequency  |
| <code>nri</code>          | table of the rank invariance frequencies in percent for each NRI/RI feature  |
| <code>var0_feature</code> | indices of features with zero sample variance after QN.  |

**Author(s)**

Ariane Schad

**References**

Brombacher, E., Schad, A., Kreutz, C. (2020). Tail-Robust Quantile Normalization. BioRxiv.

**See Also**

[mbqnPlotRI\(\)](#) and [mbqnBoxplot\(\)](#) for the generation of figures, and [mbqn\(\)](#) for normalization.

**Examples**

```
## Check data matrix for RI and NRI features
X <- matrix(c(5,2,3,NA,4,1,4,2,3,4,6,NA,1,3,1), ncol=3)
mbqnPlotAll(X, mean, low_thr = 0.5)
```

---

`mbqnPlotRI`*Plot frequency of detected RI/NRI features*

---

**Description**

Plot rank invariance frequency and feature coverage of detected RI and NRI features

**Usage**

```
mbqnPlotRI(obj, verbose = FALSE, ...)
```

**Arguments**

|                      |   |
|----------------------|---|
| <code>obj</code>     | list object of RI frequencies from <code>mbqnGetNRIfeatures()</code> .  |
| <code>verbose</code> | logical indicating to run function quietly.   |
| <code>...</code>     | additional arguments ( <code>cex</code> , <code>cex.lab</code> , <code>cex.axis</code> , <code>cex.main</code> ) passed to the plot function. |

**Details**

Graphical output of the NRI/RI identification results from `mbqnGetNRIfeatures()`. For each detected NRI/RI feature, plot the feature index against the RI frequencies together with the RI frequency detection threshold and print the sample coverage.

**Value**

Figure

**Author(s)**

Ariane Schad

**References**

Brombacher, E., Schad, A., Kreutz, C. (2020). Tail-Robust Quantile Normalization. BioRxiv.

**See Also**

[mbqnGetNRIfeatures\(\)](#) for detection of NRI/RI features.

**Examples**

```
## Check data matrix for RI and NRI features
x <- mbqnSimuData("omics.dep")
RI <- mbqnGetNRIfeatures(x, low_thr = 0.5, verbose = FALSE)
mbqnPlotRI(RI)
```

---

|              |   |
|--------------|---|
| mbqnSimuData | <i>Generate a random/structured data matrix</i> |
|--------------|---|

---

**Description**

Generate a random data matrix with or without proteomics, log-transformed feature intensity-like properties.

**Usage**

```
mbqnSimuData(model = "rand", nrow = NULL, ncol = NULL, show.fig = FALSE)
```

**Arguments**

|          |  |
|----------|--|
| model    | character indicating one of the three different type of models: "rand"(default) a Gaussian random matrix of size nrow x ncol (default 1000 x 10), "omics" a Gaussian random matrix of size 1264 x 18 that mimics intensity profiles and missing values as present in real data, and "omics.dep" is the same as "omics" but with an additional single, differentially expressed RI feature. |
| nrow     | number of rows of data matrix (only for model = "rand").   |
| ncol     | number of columns of data matrix (only for model = "rand").  |
| show.fig | logical indicating whether data properties are plot to figure (only for model = "omics" and model = "omics.dep").  |

**Details**

For model "rand", each matrix element is drawn from a standard normal distribution  $N(0, 1)$ . For model "omics", the matrix elements of each row are drawn from a Gaussian distribution  $N(\mu_i, \sigma_i^2)$  where the mean and standard deviation itself are drawn Gaussian distributions, i.e.  $\sigma_i \sim N(0, 0.0625)$  and  $\mu_i \sim N(28, 4)$ . About 35% to the missing value pattern present in real protein LFQ intensities. For model "omics.dep", a single differentially expressed RI feature is stacked on top of the matrix from model "omics".

**Value**

matrix of size nrow x ncol.

**Author(s)**

Ariane Schad

**References**

Brombacher, E., Schad, A., Kreutz, C. (2020). Tail-Robust Quantile Normalization. BioRxiv.

**See Also**

[example\\_NApattern\(\)](#) for description of missing value pattern.

## Examples

```
mbqnSimuData(model = "rand")
mbqnSimuData(model = "rand", 2000,6)
set.seed(1234)
mbqnSimuData(model = "omics")
set.seed(1111)
mbqnSimuData(model = "omics.dep")
```

---

mbqnSimuDistortion      *Perturbation of sample mean and scale*

---

## Description

mbqnSimuDistortion adds a random perturbation of mean and scale to each column of a matrix.

## Usage

```
mbqnSimuDistortion(x, s.mean = 0.05, s.scale = 0.01)
```

## Arguments

|         |  |
|---------|--|
| x       | a matrix or data frame.  |
| s.mean  | scatter of relative change of mean.                                      |
| s.scale | scatter of realtive change in scale, i.e. 0.01 corresponds to 1 percent. |

## Details

Shift and scale the sample mean and standard deviation of a matrix. The perturbation of center and scale relative to mean and standard deviation of each sample are drawn from a Gaussian distribution  $|N(0, \sigma^2)|$  with  $\sigma_{mean} = s.mean$  and  $\sigma_{scale} = s.scale$ , respectively.

## Value

List with:

|           |   |
|-----------|---|
| x.mod     | perturbed matrix  |
| mx.offset | numeric array of shifts of the sample means                         |
| mx.scale  | numeric array of relative scales of the sample standard deviations. |

## Author(s)

Ariane Schad

## References

Brombacher, E., Schad, A., Kreutz, C. (2020). Tail-Robust Quantile Normalization. BioRxiv.

**See Also**

[mbqnSimuData\(\)](#) for data generation.

**Examples**

```
set.seed(1234)
x <- mbqnSimuData("omics.dep")
df <- mbqnSimuDistortion(x)
```

---

|              |  |
|--------------|--|
| oneSidedTest | <i>Recalculate p value from two-sided to one-sided</i> |
|--------------|--|

---

**Description**

Recalculate p value from two-sided to one-sided

**Usage**

```
oneSidedTest(sign_value, z_value)
```

**Arguments**

|            |  |
|------------|--|
| sign_value | P value from two-sided significance test |
| z_value    | Z value from two-sided significance test |

**Value**

P value from one sided significance test

---

|                  |   |
|------------------|---|
| truncateDecimals | <i>Truncate float to defined number of decimal values</i> |
|------------------|---|

---

**Description**

Truncate float to defined number of decimal values

**Usage**

```
truncateDecimals(x, digits = 2)
```

**Arguments**

|        |                          |
|--------|--------------------------|
| x      | float                    |
| digits | Number of decimal values |



**Value**

Truncated number

**Examples**

```
x <- 2.567836
truncateDecimals(x, 3)
```

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