The fastLiquidAssociation Package

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1 Introduction

The fastLiquidAssociation package is intended to provide more efficient tools for genome-wide application of liquid association. The term liquid association (LA) was coined by K-C. Li in 2002 to describe a theory of co-expression dynamics which "conceptualize[s] the internal evolution of co-expression pattern for a pair of genes"? He used the term "liquid" here (as opposed to "solid") to convey the idea of a quantity which examined the extent to which the co-expression or correlation of two genes X_1 and X_2 might be mediated by the expression of a third gene X_3 , i.e. the degree to which the correlation of the two genes X_1 and X_2 might vary (e.g. go from contra- to co-expressed or vice-versa) based on the expression level of the third gene (with the third gene's expression functioning as a representation of the cellular state).

Building on Li's work, Ho et al. proposed a modification to the liquid association statistic in order to better capture more complex interdependencies between the variables, noting that, "[w]hen the conditional means and variances [of X_1 and X_2] also depend on X_3 , then the three-product-moment measure, as derived by Li for standardized variables, no longer precisely estimates the expected change of co-expression of X_1 and X_2 with respect to X_3 , but captures a larger set of interdependencies among the three variables"?

This software package provides an expansion of the functions available in the LiquidAssociation package. While the LiquidAssociation package refers to modified liquid association (MLA) as generalized liquid association (GLA), the 2011 publication refers to it as modified liquid association. For the purposes of this vignette, we will use the two terms interchangeably. The main function (fastMLA) reduces the processing power and memory needed to calculate MLA values for a genome ($\binom{N}{3}$ * 3, with N being the number of genes in the genome, e.g. 1.079×10^{11} for 6000 genes) by using a pre-screening method to reduce the candidate pool to triplets likely to have a high MLA value. It does this using matrix algebra to create an approximation to the direct MLA estimate for all possible pairs of $X_1, X_2 | X_3$. Intuitively, we can picture MLA as the change in correlation between X_1 and X_2 when X_3 is at a high level of expression versus their correlation when X_3 is at a low level of expression. This difference, ρ_{diff} ($\rho_{diff} = \rho_{high} - \rho_{low}$), gives an approximation of the relative magnitude of the MLA value for most triplet combinations (ρ_{diff} values range from -2 to 2 compared to MLA values which range from - $\sqrt{\pi/2}$ to $\sqrt{\pi/2}$). Figure 1 shows a comparison using the first 50 and the first 250 genes of the Spellman et al. data set (available in the yeastCC package) ? for all possible triplets of $|\widehat{MLA}|$ vs. $|\rho_{diff}|$ with lowess curves.

The package also incorporates functions to test for significance of the triplets returning a high MLA value and provides a faster, more robust version of the MLA bootstrapping estimation procedure for use with multicore systems.

2 Simple Usage

Here we present an example of package usage on a smaller data set. We start by loading the R package and the example data. In this package, we use the yeast cell cycle gene expression data by Spellman ?. The data can be obtained through package yeast CC. The annotation package for the yeast experiment org.Sc.sgd.db can be obtained through Bioconductor.

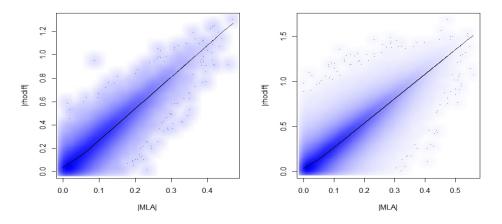
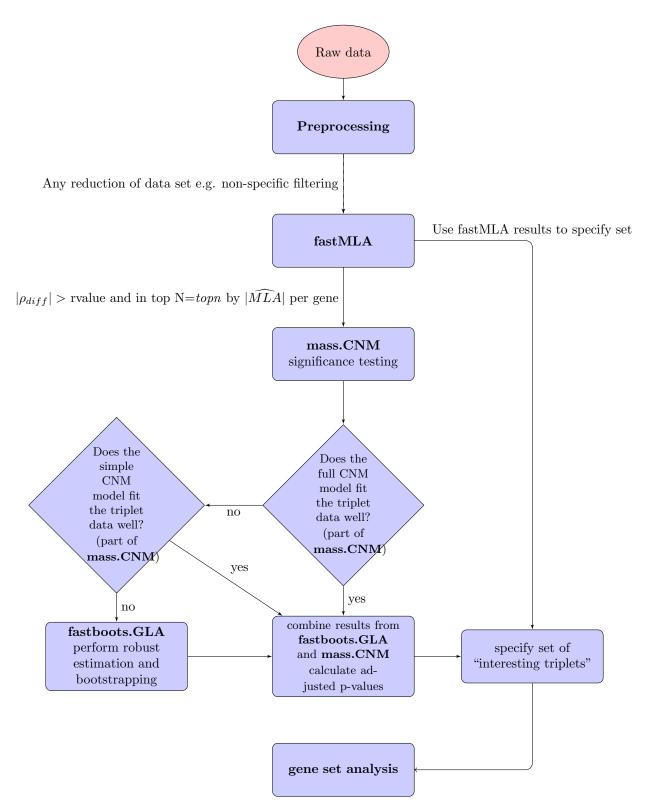


Figure 1: Comparison for all triplets possible using the first 50 and 250 genes of $|\widehat{MLA}|$ vs. $|\rho_{diff}|$ with lowess curves

2.1 fastMLA

```
Package WGCNA 1.51 loaded.
     Important note: It appears that your system supports multi-threading,
     but it is not enabled within WGCNA in R.
     To allow multi-threading within WGCNA with all available cores, use
           allowWGCNAThreads()
     within R. Use disableWGCNAThreads() to disable threading if necessary.
     Alternatively, set the following environment variable on your system:
           ALLOW_WGCNA_THREADS=<number_of_processors>
     for example
           ALLOW_WGCNA_THREADS=6
     To set the environment variable in linux bash shell, type
            export ALLOW_WGCNA_THREADS=6
     before running R. Other operating systems or shells will
     have a similar command to achieve the same aim.
> library(fastLiquidAssociation)
> library(yeastCC)
> library(org.Sc.sgd.db)
> data(spYCCES)
> lae <- spYCCES[,-(1:4)]
> ### get rid of samples with high % NA elements
```



 $Figure\ 2:\ Process\ map\ for\ data\ processing,\ testing,\ and\ gene\ set\ analysis\ using\ all\ components\ of\ the\ fastLiquidAssociation\ package$

```
> lae <- lae[apply(is.na(exprs(lae)),1,sum) < ncol(lae)*0.3,]
> data <- t(exprs(lae))
> data <- data[,1:50]
> dim(data)
[1] 73 50
```

After removing genes with high missing percentage, for speed in this example, we reduce the data set to the first 50 genes. A normal score transformation of the data as described in both Li and Ho et al.'s work ?? is performed within the **fastMLA** function. The top values are returned sorted by $|\widehat{MLA}|$.

> detectCores()

[1] 6

> example <- fastMLA(data=data,topn=50,nvec=1:5,rvalue=0.5,cut=4,threads=detectCores())</pre>

Allowing parallel execution with up to 6 working processes.

> example[1:5,]

```
X1 or X2 X2 or X1
                       ХЗ
                           rhodiff MLA value
YAL041W YAL046C YAL004W -1.14880
                                    -0.42498
YALO41W
         YAL042W YAL004W -1.22538
                                    -0.40982
YAL014C
         YAL015C YAL004W -1.09253
                                    -0.40199
YAL039C
         YAL045C YAL004W -1.03147
                                    -0.39181
YAL025C
         YAL035W YAL002W 0.94254
                                     0.39086
```

The arguments to the **fastMLA** function are a matrix of numerical data with genes as columns(data), the number of results to return (topn), the column numbers of the genes to test (nvec), the $|\rho_{diff}|$ cutoff to use (rvalue), the cut argument to pass to the GLA function from the LiquidAssociation package, and the number of processors available to use for increasing the speed of calculation for correlation values (threads)(for a fuller discussion of this argument please see the WGCNA package documentation, for a discussion of parallelization please see the section in this vignette entitled "Parallelization of the Direct Estimate"). The cut argument will depend on the number of observations in the data. Based on data from Ho et al. ?, the number of observations per bin should be in the 15-30 range for maximum specificity. The cut argument is equal to the number of bins plus one. Hence in this example, as we have 73 observations, we chose to se the cut value at 4. The maximum rvalue is theoretically 2 (as $\rho_{diff} = |\rho_{high} - \rho_{low}|$ and $-1 \le \rho_{X_1,X_2} \le 1$). The default value is set at 0.5 or 25% of the realizable correlation difference, however $|\rho_{diff}|$ a.k.a. rvalue was set at 1.1 in our example above for speed purposes. Caution should be used when determining the rvalue. Too high a value risks missing those triplets whose MLA values are not fully reflected by the more simplistic correlation, while too low a value approaches testing all possible triplets and forfeits any increase in testing efficiency. $| e^{-1} - e^{-1}$

2.2 Functions of the Conditional Normal Model

Two options for calculating significance are included in this package, **mass.CNM** which relies on estimation of parameters from a conditional normal model and **fastboots.GLA** which uses a more robust direct estimate method. Both functions return unadjusted p-values. The CNM model is written as:

$$X_3 \sim N(\mu_3, \sigma_3^2)$$

 $X_1, X_2 | X_3 \sim N(\begin{pmatrix} \mu_1 \\ \mu_2 \end{pmatrix}, \Sigma).$

¹The fastMLA function incorporates the more efficient correlation calculation of the **cor** function in the WGCNA package?.

where $\Sigma = \begin{pmatrix} \sigma_1^2 & \rho \sigma_1 \sigma_2 \\ \rho \sigma_1 \sigma_2 & \sigma_2^2 \end{pmatrix}$. The mean vector (μ_1, μ_2) and variance matrix Σ depend on the level of X_3 as written below:

$$\mu_{1} = \beta_{1}X_{3},$$

$$\mu_{2} = \beta_{2}X_{3},$$

$$\log \sigma_{1}^{2} = \alpha_{3} + \beta_{3}X_{3},$$

$$\log \sigma_{2}^{2} = \alpha_{4} + \beta_{4}X_{3},$$

$$\log \left[\frac{1+\rho}{1-\rho}\right] = \alpha_{5} + \beta_{5}X_{3}.$$

- > #from our example with fastMLA
- > CNMcalc <- mass.CNM(data=data,GLA.mat=example,nback=5)</pre>
- > CNMcalc

\$`top p-values`

```
X1 or X2 X2 or X1
                         X3 rhodiff MLA value estimates san.se wald p value
           YALO17W YALOO5C
                               0.79
                                          0.30
  YALO11W
                                                    0.70
                                                           0.17 17.14
                                                           0.20 10.87
           YALO48C YALO05C
                                          0.31
                                                                             0
  YAL040C
                               0.87
                                                    0.67
 YAL031C
           YALO36C YALO02W
                              -0.78
                                         -0.30
                                                   -0.79
                                                           0.24 10.42
                                                                             0
  YAL028W
           YALO41W YALOO4W
                               0.94
                                          0.30
                                                    1.22
                                                           0.38 10.03
                                                                             0
5 YALO41W YALO46C YALO04W
                                                           0.50 9.51
                              -1.15
                                         -0.42
                                                   -1.55
  model
      F
1
      F
2
3
      F
4
      F
```

\$`bootstrap triplets`

NULL

In our original subset of the data, there are no triplets not returning sensible values, so to demonstrate what is returned when sensible values are not returned for either model, we change the dataset used to the full 5721 genes in the yeastCC data set and use a matrix which specifically contains triplets not returning sensible values.

```
> fulldata <- t(exprs(lae))</pre>
> load(system.file('data','testmat.RData',package='fastLiquidAssociation'))
> notsense <- testmat
> CNMother <- mass.CNM(data=fulldata,GLA.mat=notsense,nback=5)
> CNMother
```

F

4

```
$`top p-values`
                         X3 rhodiff MLA value estimates san.se
  X1 or X2 X2 or X1
                                                                  wald p value
  YOL120C
           YOL143C YDR495C
                            1.2710
                                       0.5376
                                                 1.5562 0.4030 14.9116 0.0001
           YPRO45C YDR495C
 YHR129C
                             1.4467
                                       0.5474
                                                 2.4887 0.6495 14.6822
                                                                        0.0001
3 YIRO43C
           YLR375W YDR495C
                            1.3415
                                       0.5358
                                                 1.7832 0.5269 11.4531
                                                                        0.0007
 YIROO4W
           YOR291W YDR495C -1.4788
                                      -0.5662
                                                -2.1373 0.6774
                                                               9.9541
                                                                        0.0016
5 YCRX15W
           YDR257C YDR495C -1.3919
                                      -0.5435
                                                -2.1025 0.6693 9.8679
  model
     F
1
     F
2
3
     F
```

```
5 F
```

```
$`bootstrap triplets
     X1 or X2 X2 or X1
                          ХЗ
                                    rhodiff
                                              GLA value estimates
[1,] "YKR032W" "YNR021W" "YDR294C" "1.2808" "0.4567"
[2,] "YBR012C" "YDL191W" "YDR346C" "1.4023" "0.4298"
     san.se
                                 value
                                        model
                      wald
                               p
[1,] "20.0702"
                                         "S"
                      "1.2165" "0.27"
[2,] "15288623.7058" "0"
                               "0.9995" "S"
```

In the above example, we apply the **mass.CNM** function to the results of **fastMLA** to test for significance using both of the conditional normal model-based approaches laid out in Ho et al. ?. The **mass.CNM** function accepts three arguments: data, GLA.mat, and nback. data is the same matrix used as data in the **fastMLA** function, the GLA.mat is the returned matrix from a call to the **fastMLA** function, and nback is the number of results to return, sorted by p-value, then by size of the Wald statistic. The main parameter of interest in the CNM for significance testing using liquid association is b_5 .

The mass.CNM incorporates a two step process, first testing the triplets against the full CNM model and then for any triplets which do not return sensible values (sensible being defined as any triplet for which the p-value or SE estimate=0, SE estimate >10, or any β_5 statistics returned "NaN", "NA", or "Inf"), it tests them against the simple model. The full CNM model uses all parameter value (i.e. estimates the parameters of the model above using all five equations), while the simple model only uses the last three.

The mass.CNM output is a list with two components, one a data frame with *nback* rows which list the information from fastMLA (the triplet, the triplet's GLA and ρ_{diff} values), the β_5 values estimated in the model (the estimate for β_5 , its SE, the Wald statistic, and p-value), and the model (full or simple) which was used to calculate the values and the second a list of any triplets who did not return sensible values for either model. For any triplets that do not return a sensible value using one of the two models, the more robust direct estimate method is available as the **fastboots.GLA** function. ²

2.3 Parallelization of the Direct Estimate

As mentioned before, for triplets that when tested with the full or simple models did not return sensible values, a direct estimator is available. The **fastboots.GLA** function makes use of the increased processing power that has become more widely available, both on standard desktops and servers. It is an updated and parallelized version of the getsGLA function available in the LiquidAssociation package. As the standard error in the direct estimate relies on bootstrapping and the significance calculations can require a large number of iterations, we sought a more efficient method to increase efficiency.

Parallelization has as its basis the idea that large problems (e.g. a high number of calculations) can be split into smaller problems that are being run at the same time, rather than sequentially. Parallelization of processes makes sense when each process itself takes significantly longer to complete than to allocate. In the below example, we use the **detectCores** function from the parallel package to detect the number of CPU cores. On systems where more processors are available, e.g. servers for supercomputing which normally have multiple nodes of several processors each, it is possible to set a larger number of cores than the **detectCores** function may detect.

fastboots.GLA is intended to be used with the results of a call to mass.CNM, specifically the output labelled bootstrap triplets. The fastboots.GLA function is intended for use on multicore systems in order to make use of possible parallelization. While it can be used on a single core system, there would be no speed benefit over the getsGLA function available in the LiquidAssociation package, though the fastboots.GLA function does resolve an error in the getsGLA function that can be caused by data redundancy. In the below example, we are using a six core system.

```
> #determine number of processors for multicore systems
> cores <- detectCores()
> cores
```

²The above example may produce a warning message "In sqrt(diag(object\$valpha)): NaNs produced". This is normal behavior when one or both of the CNM models cannot fit at least one of the triplets.

```
[1] 6
> clust <- makeCluster(cores)
> boottrips <- CNMother[[2]]
> dim(boottrips)
[1] 2 10
```

Below we an example of processing speed with the fastboots.GLA function. Using the getsGLA function from the LiquidAssociation package, the triplet had the following values: ³

```
p value
  user
       system
                elapsed sGLA
 30.85
          0.01
                 30.92
                          5.25
                               0.00000
> #We take the results for the single triplet and put it in matrix format
> example.boots <- t(as.matrix(boottrips[1,]))</pre>
> dim(example.boots)
[1] 1 10
> set.seed(1)
> system.time(GLAnew <- fastboots.GLA(tripmat=example.boots,data=fulldata,
+ clust=clust, boots=30, perm=500, cut=4))
   user
         system elapsed
  1.927
          0.012 21.150
> GLAnew
  X1 or X2 X2 or X1
                         X3 rhodiff MLA value MLA stat boots p-value
  YKR032W YNR021W YDR294C
                            1.2808
                                       0.4567 5.25085
> #the matrix conversion is not needed for the 2 line result
> set.seed(1)
> system.time(GLAtwo <- fastboots.GLA(tripmat=boottrips,data=fulldata,
+ clust=clust, boots=30, perm=500, cut=4))
        system elapsed
  1.988
          0.004 21.772
> GLAtwo
                         X3 rhodiff MLA value MLA stat boots p-value
  X1 or X2 X2 or X1
1 YKR032W YNR021W YDR294C
                             1.2808
                                                            0.000000
                                        0.4567 5.250850
  YBR012C YDL191W YDR346C 1.4023
                                        0.4298 2.748675
                                                            0.0362173
> stopCluster(clust)
```

tripmat here is the list of triplets where a direct estimate is needed. The data is the numeric matrix of data used in both the **fastMLA** and **mass.CNM** functions. clust is a cluster of CPU cores to use in parallelization, created by a call to the **makeCluster** function from package parallel. The boots argument specifies the number of bootstrap iterations for estimating the bootstrap standard error. The perm argument specifies the number of iterations to calculate the permuted p-value. Given that the results of the permutations depend on random number generation, for reproduciblity here we use the set.seed option. The cut option is used to determine the number of "buckets" to used in the estimation procedure.

Because the normalization of the data matrix is incorporated into the **fastboots.GLA** function, the full time decrease is not apparent until the number of iterations significantly exceeds the time to normalize the data matrix or the number of triplets to test increases. This is partially displayed in the example, where even the calculation of two triplets has a lower processing time than the single triplet run serially.

³The original getsGLA code is not called here as it sometimes produces an error due to non-unique cut values with higher numbers of permutations.

3 Further Applications

In this section, we cover further applications available with the results of the fastLiquidAssociation package. Using the GOstats package in conjunction with the results from either the **fastMLA**, the **mass.CNM**, or **fastboots.GLA** we can specify our set of interesting genes and perform GO analysis. We show an example here using the genes in the X_3 position of the results from **fastMLA** to define our list of interesting genes and a p-value cutoff of 0.05 for the BP ontology. Only categories containing a minimum of five genes are displayed.

```
> library(GOstats)
> library("org.Sc.sgd.db")
> ##X3 genes
> topX3 <- unique(example[,3])</pre>
> hyp.cutoff <- 0.05
> ####
> params <- new("GOHyperGParams", geneIds=topX3,universeGeneIds=colnames(data),
+ annotation="org.Sc.sgd.db",ontology="BP",pvalueCutoff=hyp.cutoff,conditional=TRUE,
+ testDirection="over")
> GOout <- hyperGTest(params)
> summary(GOout,categorySize=5)
      GOBPID
                 Pvalue OddsRatio ExpCount Count Size
1 GO:0071822 0.01187172 23.40000 0.6666667
2 GD:0034613 0.02451434 15.85714 0.8333333
                                                     10
3 GD:0033036 0.04324699 11.66667 1.0000000
                                                 3
                                                     12
4 GD:1902580 0.04864323 13.66667 0.4166667
                                   Term
  protein complex subunit organization
2
          cellular protein localization
             macromolecule localization
4 single-organism cellular localization
```

Because we used open reading frame (ORF) IDs in order to use the GOstats package with yeast data, we can the following to unpack the associated gene names.

```
> ###extracts GO list elements of summary(hyperGtestobj)<cutoff
> ###converts ORFids to Gene names and returns under GO list element
> ##for ontology BP
> GOids <- summary(GOout, categorySize=5)$GOBPID</pre>
> check <- GOout@goDag@nodeData@data
> subset <- check[GOids]
> terms <- summary(GOout,categorySize=5)$Term
> test <- sapply(subset,function(m) m[1])</pre>
> orflist <- lapply(test,function(x) intersect(x,topX3))</pre>
> ##creates mapping of ORFids to gene names
> x <- org.Sc.sgdGENENAME
> mappedgenes <- mappedkeys(x)
> xx <- as.list(x[mappedgenes])</pre>
> mapid <- names(xx)
> ##creates list of GO ids
> genename1 <- lapply(orflist,function(x) xx[match(x,mapid)])
> ###if reduced num of terms desired use next line else skip to next ##
> for(i in 1:length(genename1)){
+ if (length(genename1[[i]])>10) genename1[[i]]<-genename1[[i]][1:10]
+ }
```

```
> ##for full list use below
> genelist <- lapply(genename1,function(x) paste(x,collapse=", "))
> ugenes <- unlist(genelist)</pre>
> names <- sapply(names(ugenes), function(x) unlist(strsplit(x, split='.', fixed=TRUE))[1])</pre>
> umat <- matrix(ugenes)</pre>
> umat <- cbind(terms,umat)</pre>
> rownames(umat) <- names
> colnames(umat) <- c("GO description", "Associated genes")
> umat
           GO description
                                                    Associated genes
GO:0071822 "protein complex subunit organization"
                                                   "VPS8, EFB1, SSA1"
GO:0034613 "cellular protein localization"
                                                    "TFC3, VPS8, SSA1"
GO:0033036 "macromolecule localization"
                                                    "TFC3, VPS8, SSA1"
GO:1902580 "single-organism cellular localization" "VPS8, SSA1"
    References
4
    Session Information
R version 3.3.0 (2016-05-03)
Platform: x86_64-pc-linux-gnu (64-bit)
Running under: Ubuntu 14.04.4 LTS
locale:
 [1] LC_CTYPE=en_US.UTF-8
                                LC_NUMERIC=C
 [3] LC_TIME=en_US.UTF-8
                                LC_COLLATE=C
 [5] LC_MONETARY=en_US.UTF-8
                                LC_MESSAGES=en_US.UTF-8
 [7] LC_PAPER=en_US.UTF-8
                                LC_NAME=C
 [9] LC_ADDRESS=C
                                LC_TELEPHONE=C
[11] LC_MEASUREMENT=en_US.UTF-8 LC_IDENTIFICATION=C
attached base packages:
[1] stats4
                                  graphics grDevices utils
              parallel stats
                                                                 datasets
[8] methods
              base
other attached packages:
 [1] GO.db_3.3.0
                                 GOstats_2.38.0
 [3] graph_1.50.0
                                 Category_2.38.0
 [5] Matrix_1.2-6
                                 fastLiquidAssociation_1.8.0
 [7] Hmisc_3.17-4
                                 ggplot2_2.1.0
[9] Formula_1.2-1
                                 survival_2.39-2
[11] lattice_0.20-33
                                 LiquidAssociation_1.26.0
[13] org.Sc.sgd.db_3.3.0
                                 AnnotationDbi_1.34.0
[15] IRanges_2.6.0
                                 S4Vectors_0.10.0
[17] yeastCC_1.11.0
                                 Biobase_2.32.0
[19] BiocGenerics_0.18.0
                                 geepack_1.2-0.1
[21] WGCNA_1.51
                                 fastcluster_1.1.20
[23] dynamicTreeCut_1.63-1
loaded via a namespace (and not attached):
```

colorspace_1.2-6
RBGL_1.48.0

splines_3.3.0

XML_3.98-1.4

[1] genefilter_1.54.0

[4] chron_2.3-47

[7] foreign_0.8-66	DBI_0.4	RColorBrewer_1.1-2
[10] matrixStats_0.50.2	foreach_1.4.3	plyr_1.8.3
[13] munsell_0.4.3	gtable_0.2.0	codetools_0.2-14
[16] latticeExtra_0.6-28	doParallel_1.0.10	preprocessCore_1.34.0
[19] GSEABase_1.34.0	Rcpp_0.12.4.5	acepack_1.3-3.3
[22] xtable_1.8-2	scales_0.4.0	annotate_1.50.0
[25] gridExtra_2.2.1	impute_1.46.0	grid_3.3.0
[28] tools_3.3.0	RSQLite_1.0.0	cluster_2.0.4
[31] data.table_1.9.6	iterators_1.0.8	AnnotationForge_1.14.0
[34] rpart_4.1-10	nnet_7.3-12	