# Package 'logicFS'

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data.logicfs

Example Data of logicFS

# Description

data.logicfs contains two objects: a simulated matrix data.logicfs of 400 observations (rows) and 15 variables (columns) and a vector cl.logicfs of length 400 containing the class labels of the observations.

Each variable is categorical with realizations 1, 2 and 3. The first 200 observations are cases, the remaining are controls. If one of the following expression is TRUE, then the corresponding observation is a case:

```
SNP1 == 3
```

SNP2 == 1 AND SNP4 == 3

SNP3 == 3 AND SNP5 == 3 AND SNP6 == 1

where SNP1 is in the first column of data. logicfs, SNP2 in the second, and so on.

# See Also

logic.bagging, logicFS

getMatEval

**Evaluate Prime Implicants** 

# **Description**

Computes the values of prime implicants for observations for which the values of the variables composing the prime implicants are available.

# Usage

```
getMatEval(data, vec.primes, check = TRUE)
```

### **Arguments**

data a data frame in which each row corrsponds to an observation, and each column

to a binary variable.

vec.primes a character vector naming the prime implicants that should be evaluated. Each

of the variables composing these prime implicants must be represented by one

column of data.

check should some checks be done before the evaluation is performed? It is highly

recommended not to change the default check = TRUE.

#### Value

a matrix in which each row corresponds to an observation (the same observations in the same order as in data, and each column to one of the prime implicants.

# Author(s)

Holger Schwender, <holger.schwender@hhu.de>

logic.bagging

Bagged Logic Regression

### **Description**

A bagging and subsampling version of logic regression. Currently available for the classification, the linear regression, and the logistic regression approach of logreg. Additionally, an approach based on multinomial logistic regressions as implemented in mlogreg can be used if the response is categorical.

# Usage

```
## Default S3 method:
logic.bagging(x, y, B = 100, useN = TRUE, ntrees = 1, nleaves = 8,
   glm.if.1tree = FALSE, replace = TRUE, sub.frac = 0.632,
   anneal.control = logreg.anneal.control(), oob = TRUE,
   onlyRemove = FALSE, prob.case = 0.5, importance = TRUE,
   score = c("DPO", "Conc", "Brier", "PL"), addMatImp = FALSE, fast = FALSE,
   neighbor = NULL, adjusted = FALSE, ensemble = FALSE, rand = NULL, ...)

## S3 method for class 'formula'
logic.bagging(formula, data, recdom = TRUE, ...)
```

### **Arguments**

x a matrix consisting of 0's and 1's. Each column must correspond to a binary variable and each row to an observation. Missing values are not allowed.

y a numeric vector, a factor, or a vector of class Surv specifying the values of a response for all the observations represented in x, where no missing values are allowed in y. If a numeric vector, then y either contains the class labels (coded by 0 and 1) or the values of a continuous response depending on whether the classification or logistic regression approach of logic regression, or the linear

> regression approach, respectively, should be used. If the response is categorical, then y must be a factor naming the class labels of the observations. If the response is a (right-censored survival time), then y must be vector of class Surv (generated, e.g., with the function Surv from the R package survival.

В an integer specifying the number of iterations.

logical specifying if the number of correctly classified out-of-bag observations useN

should be used in the computation of the importance measure. If FALSE, the proportion of correctly classified oob observations is used instead. Ignored if

importance = FALSE. Also ignored in the survival case.

an integer indicating how many trees should be used. ntrees

> For a binary response: If ntrees is larger than 1, the logistic regression approach of logic regreesion will be used. If ntrees is 1, then by default the classification approach of logic regression will be used (see glm.if.1tree.)

> For a continuous response: A linear regression model with ntrees trees is fitted in each of the B iterations.

> For a categorical response: n.lev - 1 logic regression models with ntrees trees are fitted, where n.lev is the number of levels of the response (for details, see

> For a response of class Surv: A Cox proportional hazards regression model with ntrees trees is fitted in each of the B iterations.

nleaves a numeric value specifying the maximum number of leaves used in all trees

combined. See the help page of the function logreg of the package LogicReg

for details.

if ntrees is 1 and glm.if.1tree is TRUE the logistic regression approach of glm.if.1tree

logic regression is used instead of the classification approach. Ignored if ntrees

is not 1 or the response is not binary.

replace should sampling of the cases be done with replacement? If TRUE, a bootstrap

> sample of size length(cl) is drawn from the length(cl) observations in each of the B iterations. If FALSE, ceiling(sub.frac \* length(cl)) of the obser-

vations are drawn without replacement in each iteration.

sub.frac a proportion specifying the fraction of the observations that are used in each

iteration to build a classification rule if replace = FALSE. Ignored if replace =

TRUF.

anneal.control a list containing the parameters for simulated annealing. See the help page of

logreg.anneal.control in the LogicReg package.

oob should the out-of-bag error rate (classification and logistic regression) or the

out-of-bag root mean square prediction error (linear regression), respectively,

be computed?

onlyRemove should in the single tree case the multiple tree measure be used? If TRUE, the

> prime implicants are only removed from the trees when determining the importance in the single tree case. If FALSE, the original single tree measure is computed for each prime implicant, i.e.\ a prime implicant is not only removed from the trees in which it is contained, but also added to the trees that do not

contain this interaction. Ignored in all other than the classification case.

a numeric value between 0 and 1. If the outcome of the logistic regression, i.e.\

the class probability, for an observation is larger than prob. case, this observations will be classified as case (or 1).

importance should the measure of importance be computed?

prob.case

score

a character string naming the score that should be used in the computation of the importance measure for a survival time analysis. By default, the distance between predicted outcomes (score = "DPO") proposed by Tietz et al.\ (2018) is used in the determination of the importance of the variables. Alternatively, Harrell's C-Index ("Conc"), the Brier score ("Brier"), or the predictive partial log-likelihood ("PL") can be used.

addMatImp

should the matrix containing the improvements due to the prime implicants in each of the iterations be added to the output? (For each of the prime implicants, the importance is computed by the average over the B improvements.) Must be set to TRUE, if standardized importances should be computed using vim.norm, or if permutation based importances should be computed using vim.signperm. If ensemble = TRUE and addMatImp = TRUE in the survival case, the respective score of the full model is added to the output instead of an improvement matrix.

fast

should a greedy search (as implemented in logreg) be used instead of simulated annealing?

neighbor

a list consisting of character vectors specifying SNPs that are in LD. If specified, all SNPs need to occur exactly one time in this list. If specified, the importance measures are adjusted for LD by considering the SNPs within a LD block as exchangable.

adjusted

logical specifying whether the measures should be adjusted for noise. Often, the interaction actually associated with the response is not exactly found in some iterations of logic bagging, but an interaction is identified that additionally contains one (or seldomly more) noise SNPs. If adjusted is set to TRUE, the values of the importance measure is corrected for this behaviour.

ensemble

in the case of a survival outcome, should ensemble importance measures (as, e.g., in randomSurvivalSRC be used? If FALSE, importance measures analogous to the ones in the logicFS analysis of other outcomes are used (see Tietz et al., 2018).

rand

numeric value. If specified, the random number generator will be set into a reproducible state.

formula

an object of class formula describing the model that should be fitted.

data

a data frame containing the variables in the model. Each row of data must correspond to an observation, and each column to a binary variable (coded by 0 and 1) or a factor (for details, see recdom) except for the column comprising the response, where no missing values are allowed in data. The response must be either binary (coded by 0 and 1), categorical, continuous, or a right-censored survival time. If a survival time, i.e. an object of class Surv, a Cox propotional hazard model is fitted in each of the B iterations of logicFS. If continuous, a linear model is fitted in each iterations. If categorical, the column of data specifying the response must be a factor. In this case, multinomial logic regressions are performed as implemented in mlogreg. Otherwise, depending on ntrees (and glm.if.1tree) the classification or the logistic regression approach of logic regression is used.

recdom

a logical value or vector of length ncol (data) comprising whether a SNP should be transformed into two binary dummy variables coding for a recessive and a dominant effect. If recdom is TRUE (and a logical value), then all factors/variables with three levels will be coded by two dummy variables as described in make.snp.dummy. Each level of each of the other factors (also factors specifying a SNP that shows only two genotypes) is coded by one indicator variable. If recdom isFALSE (and a logical value), each level of each factor is coded by an indicator variable. If

recdom is a logical vector, all factors corresponding to an entry in recdom that is TRUE are assumed to be SNPs and transformed into two binary variables as described above. All variables corresponding to entries of recdom that are TRUE (no matter whether recdom is a vector or a value) must be coded either by the integers 1 (coding for the homozygous reference genotype), 2 (heterozygous), and 3 (homozygous variant), or alternatively by the number of minor alleles, i.e. 0, 1, and 2, where no mixing of the two coding schemes is allowed. Thus, it is not allowed that some SNPs are coded by 1, 2, and 3, and others are coded by 0, 1, and 2.

for the formula method, optional parameters to be passed to the low level function logic.bagging.default. Otherwise, ignored.

#### Value

logic.bagging returns an object of class logicBagg containing

logreg.model a list containing the B logic regression models,

inbagg a list specifying the B Bootstrap samples,

vim an object of class logicFS (if importance = TRUE),

oob.error the out-of-bag error (if oob = TRUE),
... further parameters of the logic regression.

# Author(s)

Holger Schwender, <holger.schwender@hhu.de>; Tobias Tietz, <tobias.tietz@hhu.de>

### References

Ruczinski, I., Kooperberg, C., LeBlanc M.L. (2003). Logic Regression. *Journal of Computational and Graphical Statistics*, 12, 475-511.

Schwender, H., Ickstadt, K. (2007). Identification of SNP Interactions Using Logic Regression. *Biostatistics*, 9(1), 187-198.

Tietz, T., Selinski, S., Golka, K., Hengstler, J.G., Gripp, S., Ickstadt, K., Ruczinski, I., Schwender, H. (2018). Identification of Interactions of Binary Variables Associated with Survival Time Using survivalFS. Submitted.

#### See Also

```
predict.logicBagg, plot.logicBagg, logicFS
```

### **Examples**

```
## Not run:
# Load data.
  data(data.logicfs)

# For logic regression and hence logic.bagging, the variables must
# be binary. data.logicfs, however, contains categorical data
# with realizations 1, 2 and 3. Such data can be transformed
# into binary data by
bin.snps<-make.snp.dummy(data.logicfs)

# To speed up the search for the best logic regression models</pre>
```

logic.oob 7

```
# only a small number of iterations is used in simulated annealing.
   my.anneal<-logreg.anneal.control(start=2,end=-2,iter=10000)</pre>
   # Bagged logic regression is then performed by
   bagg.out<-logic.bagging(bin.snps,cl.logicfs,B=20,nleaves=10,</pre>
       rand=123,anneal.control=my.anneal)
   # The output of logic.bagging can be printed
   bagg.out
   # By default, also the importances of the interactions are
   # computed
   bagg.out$vim
   # and can be plotted.
   plot(bagg.out)
   # The original variable names are displayed in
   plot(bagg.out,coded=FALSE)
   # New observations (here we assume that these observations are
   # in data.logicfs) are assigned to one of the classes by
   predict(bagg.out,data.logicfs)
## End(Not run)
```

logic.oob

Prime Implicants

# **Description**

Computes the out-of-bag error of the classification rule comprised by a logicBagg object.

### Usage

```
logic.oob(log.out, prob.case = 0.5)
```

# **Arguments**

log.out an object of class logicBagg, i.e.\ the output of logic.bagging.

a numeric value between 0 and 1. If the logic regression models are logistic prob.case

> regression models, i.e.\ if in logic.bagging ntree is set to a value larger than 1, or glm. if. 1 tree is set to TRUE, then an observation will be classified as case

(or more exactly, as 1) if the class probability is larger than prob. case.

### Value

The out-of-bag error estimate.

### Author(s)

Holger Schwender, <holger.schwender@hhu.de>

#### See Also

logic.bagging

logic.pimp

Prime Implicants

# Description

Determines the prime implicants contained in the logic regression models comprised in an object of class logicBagg.

# Usage

```
logic.pimp(log.out)
```

# Arguments

log.out

an object of class logicBagg, i.e.\ the output of logic.bagging.

### **Details**

Since we are interested in all potentially interested interactions and not in a minimum set of them, logic.pimp and returns all prime implicants and not a minimum number of them.

# Value

A list consisting of the prime implicants for each of the B logic regression models of log.out.

# Author(s)

Holger Schwender, <holger.schwender@hhu.de>

# See Also

```
logic.bagging, logicFS, prime.implicants
```

logicFS

Feature Selection with Logic Regression

# **Description**

Identification of interesting interactions between binary variables using logic regression. Currently available for the classification, the linear regression and the logistic regression approach of logreg and for a multinomial logic regression as implemented in mlogreg.

### Usage

```
## Default S3 method:
logicFS(x, y, B = 100, useN = TRUE, ntrees = 1, nleaves = 8,
   glm.if.1tree = FALSE, replace = TRUE, sub.frac = 0.632,
   anneal.control = logreg.anneal.control(), onlyRemove = FALSE,
   prob.case = 0.5, score = c("DPO", "Conc", "Brier", "PL"),
   addMatImp = TRUE, fast = FALSE, neighbor = NULL,
   adjusted = FALSE, ensemble = FALSE, rand = NULL, ...)

## S3 method for class 'formula'
logicFS(formula, data, recdom = TRUE, ...)

## S3 method for class 'logicBagg'
logicFS(x, neighbor = NULL, adjusted = FALSE,
   prob.case = 0.5, score = c("DPO", "Conc", "Brier", "PL"),
   ensemble = FALSE, addMatImp = TRUE, ...)
```

### Arguments

х

a matrix consisting of 0's and 1's. Alternatively, x can also be an object of class logicBagg, i.e. the output of logic.bagging. If a matrix, each column must correspond to a binary variable and each row to an observation. Missing values are not allowed.

У

a numeric vector, a factor, or a vector of class Surv specifying the values of a response for all the observations represented in x, where no missing values are allowed in y. If a numeric vector, then y either contains the class labels (coded by 0 and 1) or the values of a continuous response depending on whether the classification or logistic regression approach of logic regression, or the linear regression approach, respectively, should be used. If the response is categorical, then y must be a factor naming the class labels of the observations. If the response is a (right-censored survival time), then y must be vector of class Surv (generated, e.g., with the function Surv from the R package survival.

В

an integer specifying the number of iterations.

useN

logical specifying if the number of correctly classified out-of-bag observations should be used in the computation of the importance measure. If FALSE, the proportion of correctly classified oob observations is used instead. Ignored in the survival case.

ntrees

an integer indicating how many trees should be used.

For a binary response: If ntrees is larger than 1, the logistic regression approach of logic regression will be used. If ntrees is 1, then by default the classification approach of logic regression will be used (see glm.if.ltree.)

For a continuous response: A linear regression model with ntrees trees is fitted in each of the B iterations.

For a categorical response: n.lev-1 logic regression models with ntrees trees are fitted, where n.lev is the number of levels of the response (for details, see mlogreg).

For a response of class Surv: A Cox proportional hazards regression model with ntrees trees is fitted in each of the B iterations.

nleaves

a numeric value specifying the maximum number of leaves used in all trees combined. For details, see the help page of the function logreg of the package LogicReg.

glm.if.1tree if ntrees is 1 and glm.if.1tree is TRUE the logistic regression approach of logic regression is used instead of the classification approach. Ignored if ntrees

is not 1, or the response is not binary.

replace should sampling of the cases be done with replacement? If TRUE, a Bootstrap

sample of size length(y) is drawn from the length(y) observations in each of the B iterations. If FALSE, ceiling(sub.frac \* length(y)) of the observa-

tions are drawn without replacement in each iteration.

sub.frac a proportion specifying the fraction of the observations that are used in each

iteration to build a classification rule if replace = FALSE. Ignored if replace =

TRUE.

anneal.control a list containing the parameters for simulated annealing. See the help of the

function logreg.anneal.control in the LogicReg package.

onlyRemove should in the single tree case the multiple tree measure be used? If TRUE, the

prime implicants are only removed from the trees when determining the importance in the single tree case. If FALSE, the original single tree measure is computed for each prime implicant, i.e.\ a prime implicant is not only removed from the trees in which it is contained, but also added to the trees that do not

contain this interaction. Ignored in all other than the classification case.

a numeric value between 0 and 1. If the outcome of the logistic regression, i.e.\ the predicted probability, for an observation is larger than prob. case this

observations will be classified as case (or 1).

score a character string naming the score that should be used in the computation of

the importance measure for a survival time analysis. By default, the distance between predicted outcomes (score = "DPO") proposed by Tietz et al.\ (2018) is used in the determination of the importance of the variables. Alternatively, Harrell's C-Index ("Conc"), the Brier score ("Brier"), or the predictive partial

log-likelihood ("PL") can be used.

addMatImp should the matrix containing the improvements due to the prime implicants in

each of the iterations be added to the output? (For each of the prime implicants, the importance is computed by the average over the B improvements.) Must be set to TRUE, if standardized importances should be computed using vim.norm, or if permutation based importances should be computed using vim.signperm. If ensemble = TRUE and addMatImp = TRUE in the survival case, the respective

score of the full model is added to the output instead of an improvement matrix.

should a greedy search (as implemented in logreg) be used instead of simulated

annealing?

fast

neighbor a list consisting of character vectors specifying SNPs that are in LD. If specified,

all SNPs need to occur exactly one time in this list. If specified, the importance measures are adjusted for LD by considering the SNPs within a LD block as

exchangable.

adjusted logical specifying whether the measures should be adjusted for noise. Often, the

interaction actually associated with the response is not exactly found in some iterations of logic bagging, but an interaction is identified that additionally contains one (or seldomly more) noise SNPs. If adjusted is set to TRUE, the values

of the importance measure is corrected for this behaviour.

ensemble in the case of a survival outcome, should ensemble importance measures (as,

e.g., in randomSurvivalSRC be used? If FALSE, importance measures analogous to the ones in the logicFS analysis of other outcomes are used (see Tietz et al.,

2018).

rand numeric value. If specified, the random number generator will be set into a

reproducible state.

formula an object of class formula describing the model that should be fitted.

data a data frame containing the variables in the model. Each row of data must

correspond to an observation, and each column to a binary variable (coded by 0 and 1) or a factor (for details, see recdom) except for the column comprising the response, where no missing values are allowed in data. The response must be either binary (coded by 0 and 1), categorical, continuous, or a right-censored survival time. If a survival time, i.e. an object of class Surv, a Cox propotional hazard model is fitted in each of the B iterations of logicFS. If continuous, a linear model is fitted in each iterations. If categorical, the column of data specifying the response must be a factor. In this case, multinomial logic regressions are performed as implemented in mlogreg. Otherwise, depending on ntrees (and glm.if.1tree) the classification or the logistic regression ap-

proach of logic regression is used.

recdom a logical value or vector of length ncol(data) comprising whether a SNP should

be transformed into two binary dummy variables coding for a recessive and a dominant effect. If recdom is TRUE (and a logical value), then all factors/variables

with three levels will be coded by two dummy variables as described in make.snp.dummy. Each level of each of the other factors (also factors specifying a SNP that shows only two genotypes) is coded by one indicator variable. If recdom isFALSE (and a logical value), each level of each factor is coded by an indicator variable. If recdom is a logical vector, all factors corresponding to an entry in recdom that is TRUE are assumed to be SNPs and transformed into two binary variables as described above. All variables corresponding to entries of recdom that are TRUE (no matter whether recdom is a vector or a value) must be coded either by the integers 1 (coding for the homozygous reference genotype), 2 (heterozygous), and 3 (homozygous variant), or alternatively by the number of minor alleles, i.e.

1, and 2.

for the formula method, optional parameters to be passed to the low level func-

0, 1, and 2, where no mixing of the two coding schemes is allowed. Thus, it is not allowed that some SNPs are coded by 1, 2, and 3, and others are coded by 0,

tion logicFS.default. Otherwise, ignored.

### Value

An object of class logicFS containing

primes the prime implicants,

vim the importance of the prime implicants,

prop the proportion of logic regression models containing the prime implicants (or

the neighbors of the prime implicants, if neighbor != NULL; or the extended primes of the prime implicants, if adjusted = TRUE; or the extended primes of the neighbors of the prime implicants, if neighbor != NULL and adjusted =

TRUE),

type the type of model (1: classification, 2: linear regression, 3: logistic regression,

4: Cox regression),

param further parameters (if addInfo = TRUE),

mat.imp either the matrix containing the improvements if addMatImp = TRUE and ensemble

= FALSE, or the respective score of the full model if addMatImp = TRUE and

ensemble = TRUE, or NULL if addMatImp = FALSE,

measure the name of the used importance measure,

neighbor neighbor,

useN the value of useN,

threshold NULL, mu NULL.

### Author(s)

Holger Schwender, <holger.schwender@hhu.de>; Tobias Tietz, <tobias.tietz@hhu.de>

#### References

Ruczinski, I., Kooperberg, C., LeBlanc M.L. (2003). Logic Regression. *Journal of Computational and Graphical Statistics*, 12, 475-511.

Schwender, H., Ickstadt, K. (2007). Identification of SNP Interactions Using Logic Regression. *Biostatistics*, 9(1), 187-198.

Tietz, T., Selinski, S., Golka, K., Hengstler, J.G., Gripp, S., Ickstadt, K., Ruczinski, I., Schwender, H. (2018). Identification of Interactions of Binary Variables Associated with Survival Time Using survivalFS. Submitted.

### See Also

```
plot.logicFS, logic.bagging
```

### **Examples**

```
## Not run:
   # Load data.
   data(data.logicfs)
   # For logic regression and hence logic.fs, the variables must
   # be binary. data.logicfs, however, contains categorical data
   # with realizations 1, 2 and 3. Such data can be transformed
   # into binary data by
   bin.snps<-make.snp.dummy(data.logicfs)</pre>
   # To speed up the search for the best logic regression models
   # only a small number of iterations is used in simulated annealing.
   my.anneal<-logreg.anneal.control(start=2,end=-2,iter=10000)</pre>
   # Feature selection using logic regression is then done by
   log.out<-logicFS(bin.snps,cl.logicfs,B=20,nleaves=10,</pre>
       rand=123,anneal.control=my.anneal)
   # The output of logic.fs can be printed
   log.out
   # One can specify another number of interactions that should be
   # printed, here, e.g., 15.
   print(log.out,topX=15)
   # The variable importance can also be plotted.
   plot(log.out)
```

logicFS-internal

```
# And the original variable names are displayed in
plot(log.out,coded=FALSE)
## End(Not run)
```

logicFS-internal

Internal logicFS functions

### **Description**

Internal logicFS functions.

### **Details**

These functions are not meant to be directly called by the user.

### Author(s)

Holger Schwender, <holger.schwender@hhu.de>

make.snp.dummy

SNPs to Dummy Variables

### **Description**

Transforms SNPs into binary dummy variables.

### Usage

```
make.snp.dummy(data)
```

### **Arguments**

data

a matrix in which each column corresponds to a SNP and each row to an observation. The genotypes of all SNPs must be either coded by 1 (for the homozygous reference genotype), 2 (heterozygous), and 3 (homozygous variant) or by 0, 1, 2. It is not allowed that some SNPs following the 1, 2, 3 coding scheme and some SNPs the 0, 1, 2 coding. Missing values are allowed, but please note that neither logic.bagging nor logicFS can handle missing values so that the missing values need to be imputed (preferably before an application of make.snp.dummy.

### **Details**

make.snp.dummy assumes that the homozygous dominant genotype is coded by 1, the heterozygous genotype by 2, and the homozygous recessive genotype by 3. Alternatively, the three genotypes can be coded by the number of minor alleles, i.e. by 0, 1, and 2. For each SNP, two dummy variables are generated:

**SNP.1** At least one of the bases explaining the SNP are of the recessive type.

**SNP.2** Both bases are of the recessive type.

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#### Value

A matrix with 2\*ncol(data) columns containing 2 dummy variables for each SNP.

#### Note

See the R package scrime for more general functions for recoding SNPs.

#### Author(s)

Holger Schwender, <holger.schwender@hhu.de>

mlogreg

Multinomial Logic Regression

# Description

Performs a multinomial logic regression for a nominal response by fitting a logic regression model (with logit as link function) for each of the levels of the response except for the level with the smallest value which is used as reference category.

# Usage

```
## S3 method for class 'formula'
mlogreg(formula, data, recdom = TRUE, ...)
## Default S3 method:
mlogreg(x, y, ntrees = 1, nleaves = 8, anneal.control = logreg.anneal.control(),
    select = 1, rand = NA, ...)
```

#### **Arguments**

formula

an object of class formula describing the model that should be fitted.

data

a data frame containing the variables in the model. Each column of data must correspond to a binary variable (coded by 0 and 1) or a factor (for details on factors, see recdom) except for the column comprising the response, and each row to an observation. The response must be a categorical variable with less than 10 levels. This response can be either a factor or of type numeric or character.

recdom

a logical value or vector of length ncol (data) comprising whether a SNP should be transformed into two binary dummy variables coding for a recessive and a dominant effect. If TRUE (logical value), then all factors (variables) with three levels will be coded by two dummy variables as described in make.snp.dummy. Each level of each of the other factors (also factors specifying a SNP that shows only two genotypes) is coded by one indicator variable. If FALSE (logical value), each level of each factor is coded by an indicator variable. If recdom is a logical vector, all factors corresponding to an entry in recdom that is TRUE are assumed to be SNPs and transformed into the two binary variables described above. Each variable that corresponds to an entry of recdom that is TRUE (no matter whether recdom is a vector or a value) must be coded by the integers 1 (coding for the homozygous reference genotype), 2 (heterozygous), and 3 (homozygous variant).

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a matrix consisting of 0's and 1's. Each column must correspond to a binary Х variable and each row to an observation. either a factor or a numeric or character vector specifying the values of the re-У sponse. The length of y must be equal to the number of rows of x. ntrees an integer indicating how many trees should be used in the logic regression models. For details, see logreg in the LogicReg package. nleaves a numeric value specifying the maximum number of leaves used in all trees combined. See the help page of the function logreg in the LogicReg package for details. anneal.control a list containing the parameters for simulated annealing. For details, see the help page of logreg.anneal.control in the LogicReg package. select numeric value. Either 0 for a stepwise greedy selection (corresponds to select = 6 in logreg) or 1 for simulated annealing. rand numeric value. If specified, the random number generator will be set into a reproducible state.

tion mlogreg. default. Otherwise, ignored.

for the formula method, optional parameters to be passed to the low level func-

#### Value

An object of class mlogreg composed of

model a list containing the logic regression models,
data a matrix containing the binary predictors,
cl a vector comprising the class labels,
ntrees a numeric value naming the maximum number of trees used in the logic regressions,
nleaves a numeric value comprising the maximum number of leaves used in the logic regressions,
fast a logical value specifying whether the faster search algorithm, i.e.\ the greedy search, has been used.

# Author(s)

Holger Schwender, <holger.schwender@hhu.de>

### References

Schwender, H., Ruczinski, I., Ickstadt, K. (2011). Testing SNPs and Sets of SNPs for Importance in Association Studies. *Biostatistics*, 12, 18-32.

# See Also

predict.mlogreg, logic.bagging, logicFS

plot.logicFS

| plot.logicFS | Variable Importance Plot |
|--------------|--------------------------|
|              |                          |

# **Description**

Generates a dotchart of the importance of the most important interactions for an object of class logicFS or logicBagg.

# Usage

```
## S3 method for class 'logicFS'
plot(x, topX = 15, cex = 0.9, pch = 16, col = 1, show.prop = FALSE,
  force.topX = FALSE, coded = TRUE, add.thres = TRUE, thres = NULL,
  include0 = TRUE, add.v0 = TRUE, v0.col = "grey50", main = NULL, ...)

## S3 method for class 'logicBagg'
plot(x, topX = 15, cex = 0.9, pch = 16, col = 1, show.prop = FALSE,
  force.topX = FALSE, coded = TRUE, include0 = TRUE, add.v0 = TRUE,
  v0.col = "grey50", main = NULL, ...)
```

# Arguments

| х          | an object of either class logicFS or logicBagg.  |
|------------|--|
| topX       | integer specifying how many interactions should be shown. If $topX$ is larger than the number of interactions contained in $x$ all the interactions are shown. For further information, see force.topX.          |
| cex        | a numeric value specifying the relative size of the text and symbols.  |
| pch        | specifies the used symbol. See the help of par for details.  |
| col        | the color of the text and the symbols. See the help of par for how colors can be specified.  |
| show.prop  | if TRUE the proportions of models that contain the interactions of interest are shown. If FALSE (default) the importances of the interactions are shown.   |
| force.topX | if TRUE exactly topX interactions are shown. If FALSE (default) all interactions up to the topXth most important one and all interactions having the same importance as the topXth most important one are shown. |
| coded      | should the coded variable names be displayed? Might be useful if the actual variable names are pretty long. The coded variable name of the $j$ -th variable is $Xj$ .  |
| add.thres  | should a vertical line marking the threshold for a prime implicant to be called important be drawn in the plot? If TRUE, this vertical line will be drawn at NULL.   |
| thres      | non-negative numeric value specifying the threshold for a prime implicant to be called important. If NULL and add. thres = TRUE, the suggested threshold from x will be used.                                    |
| include0   | should the x-axis include zero regardless whether the importances of the shown interactions are much higher than 0?  |
| add.v0     | should a vertical line be drawn at $x=0$ ? Ignored if include0 = FALSE and all importances are larger than zero.   |
|            |  |

plot.predict.survivalFS 17

| v0.col | the color of the vertical line at $x=0$ . See the help page of par for how colors                   |
|--------|---|
|        | can be specified.   |
| main   | character string naming the title of the plot. If NULL, the name of the importance measure is used. |
|        | measure is used.  |
|        | Ignored.  |

# Author(s)

Holger Schwender, <holger.schwender@hhu.de>

# See Also

```
logicFS, logic.bagging
```

```
plot.predict.survivalFS
```

Survival and Cumulative Hazard Function Plot

# **Description**

Plots predicted survival or cumulative hazard curves of new observations for an object of class predict.survivalFS.

# Usage

# **Arguments**

| Х          | an object of class predict. survivalFS as generated by the function predict.logicBagg.  |
|------------|---|
| select_obs | a numeric vector identifying the observations whose survival curves should be plotted. If is.missing(select.obs) the first five observations, or, if the number of observations is less than five, all observations are chosen. |
| xlab       | a title for the x axis: see title.  |
| ylab       | a title for the y axis: see title. If NULL, the title is generated automatically.   |
| ylim       | a numeric vector of length 2 that sets the limits of the y axis. If NULL, the limits are generated automatically.   |
| type       | character indicating the type of plotting; actually any of the types as in plot.default.  |
| main       | an overall title for the plot: see title. If NULL, the main title is generated automatically.   |
| sub        | a sub title for the plot: see title. If NULL, the sub title is generated automatically.   |
| vec_col    | a numeric or character vector that specifies the plotting colors of the survival curves (see par). Vector must have the same length as select_obs.  |
| vec_lty    | a numeric or character vector that specifies the line types of the survival curves (see par). Vector must have the same length as select_obs.   |
| addLegend  | should a legend be added to the plot automatically?   |
| • • •      | Ignored.  |

18 predict.logicBagg

#### Author(s)

Tobias Tietz, <tobias.tietz@hhu.de>

predict.logicBagg

Predict Method for logicBagg objects

### **Description**

Prediction for test data using an object of class logicBagg.

# Usage

```
## S3 method for class 'logicBagg'
predict(object, newData, prob.case = 0.5,
    type = c("class", "prob"), score = c("DPO", "Conc", "Brier"), ...)
```

# **Arguments**

type

object an object of class logicBagg.

newData a matrix or data frame containing new data. If omitted object\\$data, i.e.\ the

original training data, are used. Each row of newData must correspond to a new observation. Each row of newData must contain the same variable as the corresponding column of the data matrix used in logic.bagging, i.e.\ x if the default method of logic.bagging has been used, or data without the column

containing the response if the formula method has been used.

prob.case a numeric value between 0 and 1. A new observation will be classified as case

(or more exactly, as 1) if the class probability, i.e.\ the average of the predicted probabilities of the models (if the logistic regression approach of logic regression has been used), or the percentage of votes for class 1 (if the classification approach of logic regression has been used) is larger than prob. case. Ignored if

type = "prob" or the response is either quantitative or an object of class Surv.

character vector indicating the type of output. If "class", a numeric vector of zeros and ones containing the predicted classes of the observations (using the specification of prob.case) will be returned. If "prob", the class probabilities or percentages of votes for class 1, respectively, for all observations are returned.

Ignored if the response is quantitative or an object of class Surv.

score a character string naming the score that should be used to assess the performance

of the prediction model in the survival case. By default, the distance between predicted outcomes (score = "DPO") proposed by Tietz et al.\ (2018) is used in the assessment of the prediction performance. Alternatively, Harrell's C-Index ("Conc"), or the Brier score ("Brier") can be used. Furthermore, score determines whether a prediction for the cumulative hazard function (score = "DPO" or score = "Conc") or the survival function (score = "Brier") of the new ob-

servations should be made. Ignored in all other than the survival case.

... Ignored.

predict.mlogreg 19

#### Value

A numeric vector containing the predicted classes (if type = "class") or the class probabilities (if type = "prob") of the new observations if the classification or the logistic regression approach of logic regression is used. If the response is quantitative, the predicted value of the response for all observations in the test data set is returned. If the response is of class Surv, an object of class predict.survivalFS with either an prediction for the cumulative hazard function or the survival function of the new observations is returned.

### Author(s)

Holger Schwender, <holger.schwender@hhu.de>, Tobias Tietz, <tobias.tietz@hhu.de>

#### See Also

logic.bagging

predict.mlogreg

Predict Method for mlogreg Objects

# **Description**

Prediction for test data using an object of class mlogreg.

# Usage

```
## S3 method for class 'mlogreg'
predict(object, newData, type = c("class", "prob"), ...)
```

### **Arguments**

object an object of class mlogreg, i.e.\ the output of the function mlogreg.

newData a matrix or data frame containing new data. If omitted object\\$data, i.e.\ the

original training data, are used. Each row of newData must correspond to a new observation. Each row of newData must contain the same variable as the corresponding column of the data matrix used in mlogreg, i.e.\ x if the default method of mlogreg has been used, or data without the column containing the

response if the formula method has been used.

type character vector indicating the type of output. If "class", a vector containing

the predicted classes of the observations will be returned. If "prob", the class

probabilities for each level and all observations are returned.

... Ignored.

### Value

A numeric vector containing the predicted classes (if type = "class"), or a matrix composed of the class probabilities (if type = "prob").

### Author(s)

Holger Schwender, <holger.schwender@hhu.de>

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### See Also

mlogreg

print.logicFS

Print a logicFS object

# Description

Prints an object of class logicFS.

# Usage

```
## S3 method for class 'logicFS'
print(x, topX = 5, show.prop = TRUE, coded = FALSE, digits = 2, ...)
```

# **Arguments**

| X | an object of either cla | ass logicES. |
|---|-------------------------|--------------|
|   |                         |              |

topX integer indicating how many interactions should be shown. Additionally to the

topX most important interactions, any interaction having the same importance

as the topX most important one are also shown.

show.prop should the proportions of models containing the interactions of interest also be

shown?

coded should the coded variable names be displayed? Might be useful if the actual

variable names are pretty long. The coded variable name of the j-th variable is

Χi.

digits number of digits used in the output.

... Ignored.

# Author(s)

Holger Schwender, <holger.schwender@hhu.de>

# See Also

logicFS, vim.logicFS

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| survivalFS Logic Feature Selection for Survival Data |  |
|--|--|
|--|--|

### **Description**

Identification of interactions of binary variables associated with survival time using logic regression.

# Usage

```
## Default S3 method:
survivalFS(x, y, B = 20, replace = FALSE,
    sub.frac = 0.632, score = c("DPO", "Conc", "Brier", "PL"),
    addMatImp = TRUE, adjusted = FALSE, neighbor = NULL,
    ensemble = FALSE, rand = NULL, ...)

## S3 method for class 'formula'
survivalFS(formula, data, recdom = TRUE, ...)

## S3 method for class 'logicBagg'
survivalFS(x, score = c("DPO", "Conc", "Brier", "PL"),
    adjusted = FALSE, neighbor = NULL, ensemble = FALSE,
    addMatImp = TRUE, rand = NULL, ...)
```

# Arguments

addMatImp

| e e      |   |
|----------|---|
| х        | a matrix consisting of 0's and 1's. Alternatively, x can also be an object of class logicBagg, i.e. the output of logic.bagging. If a matrix, each column must correspond to a binary variable and each row to an observation. Missing values are not allowed.  |
| У        | a vector of class Surv specifying the right-censored survival time for all observations represented in x, where no missing values are allowed in y. This vector can, e.g., be generated using the function Surv from the R package survival.  |
| В        | an integer specifying the number of iterations.   |
| replace  | should sampling of the cases be done with replacement? If TRUE, a Bootstrap sample of size length(y) is drawn from the length(y) observations in each of the B iterations. If FALSE, ceiling(sub.frac * length(y)) of the observations are drawn without replacement in each iteration.   |
| sub.frac | a proportion specifying the fraction of the observations that are used in each iteration to build a classification rule if replace = FALSE. Ignored if replace = TRUE.  |
| score    | a character string naming the score that should be used in the computation of the importance measure for a survival time analysis. By default, the distance between predicted outcomes (score = "DPO") proposed by Tietz et al.\ (2018) is used in the determination of the importance of the variables. Alternatively, Harrell's C-Index ("Conc"), the Brier score ("Brier"), or the predictive partial log-likelihood ("PL") can be used. |

should the matrix containing the improvements due to the prime implicants in each of the iterations be added to the output if ensemble = FALSE? (For each of the prime implicants, the importance is computed by the average over the

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> B improvements.) If ensemble = TRUE and addMatImp = TRUE, the respective score of the full model is added to the output instead of an improvement matrix.

adjusted

logical specifying whether the measures should be adjusted for noise. Often, the interaction actually associated with the response is not exactly found in some iterations of logic bagging, but an interaction is identified that additionally contains one (or seldomly more) noise SNPs. If adjusted is set to TRUE, the values of the importance measure is corrected for this behaviour.

neighbor

a list consisting of character vectors specifying SNPs that are in LD. If specified, all SNPs need to occur exactly one time in this list. If specified, the importance measures are adjusted for LD by considering the SNPs within a LD block as exchangable.

ensemble

in the case of a survival outcome, should ensemble importance measures (as, e.g., in randomSurvivalSRC be used? If FALSE, importance measures analogous to the ones in the logicFS analysis of other outcomes are used (see Tietz et al., 2018).

rand

numeric value. If specified, the random number generator will be set into a reproducible state.

formula

an object of class formula describing the model that should be fitted.

data

a data frame containing the variables in the model. Each row of data must correspond to an observation, and each column to a binary variable (coded by 0 and 1) or a factor (for details, see recdom) except for the column comprising the response, where no missing values are allowed in data. The response must be

an object of class Surv.

recdom

a logical value or vector of length ncol (data) comprising whether a SNP should be transformed into two binary dummy variables coding for a recessive and a dominant effect. If recdom is TRUE (and a logical value), then all factors/variables with three levels will be coded by two dummy variables as described in make.snp.dummy. Each level of each of the other factors (also factors specifying a SNP that shows only two genotypes) is coded by one indicator variable. If recdom isFALSE (and a logical value), each level of each factor is coded by an indicator variable. If recdom is a logical vector, all factors corresponding to an entry in recdom that is TRUE are assumed to be SNPs and transformed into two binary variables as described above. All variables corresponding to entries of recdom that are TRUE (no matter whether recdom is a vector or a value) must be coded either by the integers 1 (coding for the homozygous reference genotype), 2 (heterozygous), and 3 (homozygous variant), or alternatively by the number of minor alleles, i.e. 0, 1, and 2, where no mixing of the two coding schemes is allowed. Thus, it is not allowed that some SNPs are coded by 1, 2, and 3, and others are coded by 0, 1, and 2.

further arguments of logicFS. Ignored, if x is an object of class logicBagg.

### Value

An object of class logicFS containing

primes the prime implicants,

the importance of the prime implicants, vim

the proportion of logic regression models containing the prime implicants, (or prop the neighbors of the prime implicants, if neighbor != NULL; or the extended

primes of the prime implicants, if adjusted = TRUE; or the extended primes of

vim.approxPval 23

the neighbors of the prime implicants, if neighbor != NULL and adjusted =

TRUE),

type the type of model (1: classification, 2: linear regression, 3: logistic regression,

4: Cox regression),

param further parameters (if addInfo = TRUE),

mat.imp either the matrix containing the improvements if addMatImp = TRUE and ensemble

= FALSE, or the respective score of the full model if addMatImp = TRUE and

ensemble = TRUE, or NULL if addMatImp = FALSE,

measure the name of the used importance measure,

neighbor neighbor,

useN the value of useN,

 $\begin{array}{ll} \text{threshold} & \text{NULL}, \\ \text{mu} & \text{NULL}. \end{array}$ 

### Author(s)

Tobias Tietz, <tobias.tietz@hhu.de>

### References

Tietz, T., Selinski, S., Golka, K., Hengstler, J.G., Gripp, S., Ickstadt, K., Ruczinski, I., Schwender, H. (2018). Identification of Interactions of Binary Variables Associated with Survival Time Using survivalFS. Submitted.

# See Also

logicFS, logic.bagging

vim.approxPval

Approximate P-Value Based Importance Measure

### **Description**

Computes the importances based on an approximation to a t- or F-distribution.

# Usage

```
vim.approxPval(object, version = 1, adjust = "bonferroni")
```

### **Arguments**

object an object of class logicFS which contains the values of standardized impor-

tances. Only in the linear regression case, the importances in object are allowed

to be non-standardized.

version either 1 or 2. If 1, then the importance measure is computed by 1 - padj, where

padj is the adjusted p-value. If 2, the importance measure is determined by log10(padj), where a raw p-value equal to 0 is set to log10(padj), where a raw p-value equal to 0 is set to log10(padj), where a raw p-value equal to 0 is set to log10(padj), where a raw p-value equal to 0 is set to log10(padj), where a raw p-value equal to 0 is set to log10(padj), where a raw p-value equal to 0 is set to log10(padj), where a raw p-value equal to 0 is set to log10(padj), where a raw p-value equal to 0 is set to log10(padj), where log10(padj), where log10(padj) is set to log10(padj).

infinitive importances.

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adjust character vector naming the method with which the raw permutation based p-

values are adjusted for multiplicity. If "qvalue", the function qvalue.cal from the package siggenes is used to compute q-values. Otherwise, p.adjust is used to adjust for multiple comparisons. See p.adjust for all other possible

specifications of adjust. If "none", the raw p-values will be used.

#### Value

An object of class logicFS containing the same object as object except for

vim the values of the importance measure based on an approximation to the t- or

F-distribution,

measure the name of the used importance measure,

threshold 0.95 if version = 1, and  $-\log 10(0.05) \text{ if version} = 2$ .

# Author(s)

Holger Schwender, <holger.schwender@hhu.de>

#### References

Schwender, H., Ruczinski, I., Ickstadt, K. (2011). Testing SNPs and Sets of SNPs for Importance in Association Studies. *Biostatistics*, 12, 18-32.

#### See Also

logic.bagging, logicFS, vim.input, vim.set, vim.permSet

vim.chisq

ChiSquare Based Importance

# Description

Determining the importance of interactions found by logic.bagging or logicFS by Pearson's ChiSquare Statistic. Only available for the classification and the logistic regression approach of logic regression.

### Usage

```
vim.chisq(object, data = NULL, cl = NULL)
```

### **Arguments**

object either an object of class logicFS or the output of an application of logic.bagging

with importance = TRUE.

data a data frame or matrix consisting of 0's and 1's in which each column corre-

sponds to one of the explanatory variables used in the original analysis with logic.bagging or logicFS, and each row corresponds to an observation. Must be specified if object is an object of class logicFS, or cl is specified. If object is an object of class logicBagg and neither data nor cl is specified, data and cl stored in object is used to compute the ChiSquare statistics. It is, however, highly recommended to use new data to test the interactions contained in

vim.chisq 25

object, as they have been found using the data stored in object, and it is very likely that most of them will show up as interesting if they are tested on the same

data set.

cl a numeric vector of 0's and 1's specifying the class labels of the observations

in data. Must be specified either if object is an object of class logicFS, or if

data is specified.

#### **Details**

Currently Pearson's ChiSquare statistic is computed without continuity correction.

Contrary to vim.logicFS (and vim.norm and vim.signperm), vim.chisq does neither take the logic regression models into acount nor uses the out-of-bag observations for computing the importances of the identified interactions. It "just" tests each of the found interactions on the whole data set by calculating Pearson's ChiSquare statistic for each of these interactions. It is, therefore, highly recommended to use an independent data set for specifying the importances of these interactions with vim.chisq.

### Value

An object of class logicFS containing

primes the prime implicants

vim the values of Pearson's ChiSquare statistic,

prop NULL, type NULL,

param further parameters (if object is the output of logicFS or vim.logicFS with

addInfo = TRUE),

mat.imp NULL,

measure "ChiSquare Based",

threshold the 1 - 0.05/m quantile of the ChiSquare distribution with one degree of freedom,

mu NULL.

# Author(s)

Holger Schwender, <holger.schwender@hhu.de>

### See Also

logic.bagging, logicFS, vim.logicFS, vim.norm, vim.ebam

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vim.ebam

EBAM Based Importance

### **Description**

Determines the importance of interactions found by logic.bagging or logicFS by an Empirical Bayes Analysis of Microarrays (EBAM). Only available for the classification and the logistic regression approach of logic regression.

### Usage

```
vim.ebam(object, data = NULL, cl = NULL, storeEBAM = FALSE, ...)
```

### **Arguments**

object either an object of class logicFS or the output of an application of logic.bagging

with importance = TRUE.

data a data frame or matrix consisting of 0's and 1's in which each column corre-

sponds to one of the explanatory variables used in the original analysis with logic.bagging or logicFS, and each row corresponds to an observation. Must be specified if object is an object of class logicFS, or cl is specified. If object is an object of class logicBagg and neither data nor cl is specified, data and cl stored in object is used to compute the ChiSquare statistics. It is, however, highly recommended to use new data to test the interactions contained in object, as they have been found using the data stored in object, and it is very likely that most of them will show up as interesting if they are tested on the same

data set.

cl a numeric vector of 0's and 1's specifying the class labels of the observations

in data. Must be specified either if object is an object of class logicFS, or if

data is specified.

storeEBAM logical specifying whether the output of the EBAM analysis should be stored in

the output of vim.ebam.

... further arguments of ebam and cat.ebam. For details, see the help files of these

functions from the package siggenes.

### Details

For each interaction found by logic.bagging or logicFS, the posterior probability that this interaction is significant is computed using the Empirical Bayes Analysis of Microarrays (EBAM). These posterior probabilities are used as the EBAM based importances of the interactions.

The test statistic underlying this EBAM analysis is Pearson's ChiSquare statistic. Currently, the value of this statistic is computed without continuity correction.

Contrary to vim.logicFS (and vim.norm and vim.signperm), vim.ebam does neither take the logic regression models into acount nor uses the out-of-bag observations for computing the importances of the identified interactions. It "just" tests each of the found interactions on the whole data set by calculating Pearson's ChiSquare statistic for each of these interactions and performing an EBAM analysis. It is, therefore, highly recommended to use an independent data set for specifying the importances of these interactions with vim.ebam.

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### Value

An object of class logicFS containing

primes the prime implicants,

vim the posterior probabilities of the interactions,

 $\begin{array}{ll} \text{prop} & \text{NULL,} \\ \\ \text{type} & \text{NULL,} \end{array}$ 

param further parameters (if object is the output of logicFS or vim.logicFS with

addInfo = TRUE),

mat.imp NULL,

measure "EBAM Based",

threshold the value of delta used in the EBAM analysis (see help files for ebam); by

default: 0.9,

mu NULL,

ebam an object of class EBAM (only available if storeEBAM = TRUE).

### Author(s)

Holger Schwender, <holger.schwender@hhu.de>

### References

Schwender, H. and Ickstadt, K. (2008). Empirical Bayes Analysis of Single Nucleotide Polymorphisms. *BMC Bioinformatics*, 9:144.

# See Also

logic.bagging, logicFS, vim.logicFS, vim.norm, vim.chisq

vim.input VIM for Inputs

# Description

Quantifies the importance of each input variable occurring in at least one of the logic regression models found in the application of logic.bagging.

### Usage

```
vim.input(object, useN = NULL, iter = NULL, prop = TRUE,
    standardize = NULL, mu = 0, addMatImp = FALSE,
    prob.case = 0.5, rand = NA)
```

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### **Arguments**

object an object of class logicBagg, i.e.\ the output of logic.bagging

useN logical specifying if the number of correctly classified out-of-bag observations

should be used in the computation of the importance measure. If FALSE, the proportion of correctly classified oob observations is used instead. If NULL (default),

then the specification of useN in object is used.

iter integer specifying the number of times the values of the considered variable are

permuted in the computation of its importance. If NULL (default), the values of the variable are not permuted, but the variable is removed from the model.

prop should the proportion of logic regression models containing the respective vari-

able also be computed?

standardize should a standardized version of the importance measure for a set of variables

be returned? By default, standardize = TRUE is used in the classification and the (multinomial) logistic regression case, and standarize is set to FALSE in

the linear regression case. For details, see mu.

mu a non-negative numeric value. Ignored if standardize = FALSE. Otherwise, a

t-statistic for testing the null hypothesis that the importance of the respective

variable is equal to mu is computed.

addMatImp should the matrix containing the improvements due to each of the variables in

each of the logic regression models be added to the output?

prob. case a numeric value between 0 and 1. If the logistic regression approach of logic

regression has been used in logic.bagging, then an observation will be classified as a case (or more exactly, as 1), if the class probability of this observation

is larger than prob. case. Otherwise, prob. case is ignored.

rand an integer for setting the random number generator in a reproducible case.

### Value

An object of class logicFS containing

vim the importances of the variables,

prop the proportion of logic regression models containing the respective variable (if

prop = TRUE) or NULL (if prop = FALSE),

primes the names of the variables,

type the type of model (1: classification, 2:linear regression, 3: logistic regression), param further parameters (if addInfo = TRUE in the previous call of logic.bagging),

mat.imp either a matrix containing the improvements due to the variables for each of the

models (if addMatImp = TRUE), or NULL (if addMatImp = FALSE),

measure the name of the used importance measure,

useN the value of useN,

threshold NULL if standardize = FALSE, otherwise the 1 - 0.05/m quantile of the t-

distribution with B-1 degrees of freedom, where m is the number of variables

and B is the number of logic regression models composing object,

mu (if standardize = TRUE), or NULL (otherwise),

iter iter.

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### Author(s)

Holger Schwender, <holger.schwender@hhu.de>

#### References

Schwender, H., Ruczinski, I., Ickstadt, K. (2011). Testing SNPs and Sets of SNPs for Importance in Association Studies. *Biostatistics*, 12, 18-32.

#### See Also

```
logic.bagging, logicFS, vim.logicFS, vim.set, vim.ebam, vim.chisq
```

vim.logicFS

Importance Measures

# **Description**

Computes the value of the single or the multiple tree measure, respectively, for each prime implicant contained in a logic bagging model to specify the importance of the prime implicant for classification, if the response is binary. If the response is quantitative, the importance is specified by a measure based on the log2-transformed mean square prediction error. If the response is a time to an event, performance measures for time-to-event models are employed to determine the importance measures.

# Usage

```
vim.logicFS(log.out, neighbor = NULL, adjusted = FALSE, useN = TRUE,
  onlyRemove = FALSE, prob.case = 0.5, addInfo = FALSE,
  score = c("DPO", "Conc", "Brier", "PL"), ensemble = FALSE,
  addMatImp = TRUE)
```

# Arguments

log.out an object of class logicBagg, i.e.\ the output of logic.bagging.

neighbor a list consisting of character vectors specifying SNPs that are in LD. If specified,

all SNPs need to occur exactly one time in this list. If specified, the importance measures are adjusted for LD by considering the SNPs within a LD block as

exchangable.

adjusted logical specifying whether the measures should be adjusted for noise. Often, the

interaction actually associated with the response is not exactly found in some iterations of logic bagging, but an interaction is identified that additionally contains one (or seldomly more) noise SNPs. If adjusted is set to TRUE, the values

of the importance measure is corrected for this behaviour.

useN logical specifying if the number of correctly classified out-of-bag observations

should be used in the computation of the importance measure. If FALSE, the proportion of correctly classified oob observations is used instead. Ignored in

the survival case.

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onlyRemove should in the single tree case the multiple tree measure be used? If TRUE, the

prime implicants are only removed from the trees when determining the importance in the single tree case. If FALSE, the original single tree measure is computed for each prime implicant, i.e.\ a prime implicant is not only removed from the trees in which it is contained, but also added to the trees that do not

contain this interaction. Ignored in all other than the classification case.

prob. case a numeric value between 0 and 1. If the logistic regression approach of logic

regression is used (i.e.\ if the response is binary, and in logic.bagging ntrees is set to a value larger than 1, or glm.if.1tree is set to TRUE), then an observation will be classified as a case (or more exactly as 1), if the class probability of this observation estimated by the logic bagging model is larger than prob.case.

addInfo should further information on the logic regression models be added?

score a character string naming the score that should be used in the computation of

the importance measure for a survival time analysis. By default, the distance between predicted outcomes (score = "DPO") proposed by Tietz et al.\ (2018) is used in the determination of the importance of the variables. Alternatively, Harrell's C-Index ("Conc"), the Brier score ("Brier"), or the predictive partial

log-likelihood ("PL") can be used.

ensemble in the case of a survival outcome, should ensemble importance measures (as,

e.g., in randomSurvivalSRC be used? If FALSE, importance measures analogous to the ones in the logicFS analysis of other outcomes are used (see Tietz et al.,

2018).

addMatImp should the matrix containing the improvements due to the prime implicants in

each of the iterations be added to the output? (For each of the prime implicants, the importance is computed by the average over the B improvements.) Must be set to TRUE, if standardized importances should be computed using vim.norm, or if permutation based importances should be computed using vim.signperm. If ensemble = TRUE and addMatImp = TRUE in the survival case, the respective

score of the full model is added to the output instead of an improvement matrix.

Value

An object of class logicFS containing

primes the prime implicants,

vim the importance of the prime implicants,

prop the proportion of logic regression models containing the prime implicants (or

the neighbors of the prime implicants, if neighbor != NULL; or the extended primes of the prime implicants, if adjusted = TRUE; or the extended primes of the neighbors of the prime implicants, if neighbor != NULL and adjusted =

TRUE),

type the type of model (1: classification, 2: linear regression, 3: logistic regression,

4: Cox regression),

param further parameters (if addInfo = TRUE),

mat.imp either the matrix containing the improvements if addMatImp = TRUE and ensemble

= FALSE, or the respective score of the full model if addMatImp = TRUE and

ensemble = TRUE, or NULL if addMatImp = FALSE,

measure the name of the used importance measure,

neighbor neighbor,

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useN the value of useN,

 $\begin{array}{ll} \text{threshold} & \text{NULL}, \\ \text{mu} & \text{NULL}. \end{array}$ 

# Author(s)

Holger Schwender, <holger.schwender@hhu.de>; Tobias Tietz, <tobias.tietz@hhu.de>

#### References

Schwender, H., Ickstadt, K. (2007). Identification of SNP Interactions Using Logic Regression. *Biostatistics*, 9(1), 187-198.

Tietz, T., Selinski, S., Golka, K., Hengstler, J.G., Gripp, S., Ickstadt, K., Ruczinski, I., Schwender, H. (2018). Identification of Interactions of Binary Variables Associated with Survival Time Using survivalFS. Submitted.

#### See Also

logic.bagging, logicFS, vim.norm, vim.signperm

vim.norm

Standardized and Sign-Permutation Based Importance Measure

# Description

Computes a standarized or a sign-permutation based version of either the Single Tree Measure, the Quantitative Response Measure, or the Multiple Tree Measure.

# Usage

```
vim.norm(object, mu = 0)
vim.signperm(object, mu = 0, n.perm = 10000, n.subset = 1000,
version = 1, adjust = "bonferroni", rand = NA)
```

# **Arguments**

| object   | either the output of logicFS or vim.logicFS with addMatImp = TRUE, or the output of logic.bagging with importance = TRUE and addMatImp = TRUE.   |
|----------|--|
| mu       | a non-negative numeric value against which the importances are tested. See Details.  |
| n.perm   | the number of sign permutations used in vim.signperm.  |
| n.subset | an integer specifying how many permutations should be considered at once.  |
| version  | either 1 or 2. If 1, then the importance measure is computed by 1 - padj, where padj is the adjusted p-value. If 2, the importance measure is determined by $-\log 10(padj)$ , where a raw p-value equal to 0 is set to $1/(10*n.perm)$ to avoid infinitive importances. |

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adjust character vector naming the method with which the raw permutation based p-

values are adjusted for multiplicity. If "qvalue", the function qvalue.cal from the package siggenes is used to compute q-values. Otherwise, p.adjust is used to adjust for multiple comparisons. See p.adjust for all other possible specifications of adjust. If "none", the raw p-values will be used. For more

details, see Details.

rand an integer for setting the random number generator in a reproducible case.

#### **Details**

In both vim.norm and vim.signperm, a paired t-statistic is computed for each prime implicant, where the numerator is given by VIM-mu with VIM being the single or the multiple tree importance, and the denominator is the corresponding standard error computed by employing the B improvements of the considered prime implicant in the B logic regression models, where VIM is the mean over these B improvements.

Note that in the case of a quantitative response, such a standardization is not necessary. Thus, vim.norm returns a warning when the response is quantitative, and vim.signperm does not divide VIM-mu by its sample standard error.

Using mu = 0 might lead to calling a prime implicant important, even though it actually shows only improvements of 1 or 0. When considering the prime implicants, it might be therefore be helpful to set mu to a value slightly larger than zero.

In vim.norm, the value of this t-statistic is returned as the standardized importance of a prime implicant. The larger this value, the more important is the prime implicant. (This applies to all importance measures – at least for those contained in this package.) Assuming normality, a possible threshold for a prime implicant to be considered as important is the 1-0.05/m quantile of the t-distribution with B-1 degrees of freedom, where m is the number of prime implicants.

In vim.signperm, the sign permutation is used to determine n.perm permuted values of the one-sample t-statistic, and to compute the raw p-values for each of the prime implicants. Afterwards, these p-values are adjusted for multiple comparisons using the method specified by adjust. The permutation based importance of a prime implicant is then given by 1- these adjusted p-values. Here, a possible threshold for calling a prime implicant important is 0.95.

### Value

An object of class logicFS containing

primes the prime implicants,

vim the respective importance of the prime implicants,

prop NULL,

type the type of model (1: classification, 2: linear regression, 3: logistic regression),

param further parameters (if addInfo = TRUE),

mat.imp NULL,

measure the name of the used importance measure,

useN the value of useN from the original analysis with, e.g., logicFS,

threshold the threshold suggested in Details,

mu mu.

### Author(s)

Holger Schwender, <holger.schwender@hhu.de>

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#### References

Schwender, H., Ruczinski, I., Ickstadt, K. (2011). Testing SNPs and Sets of SNPs for Importance in Association Studies. *Biostatistics*, 12, 18-32.

#### See Also

```
logic.bagging, logicFS, vim.logicFS, vim.chisq, vim.ebam
```

vim.permSNP

Permutation Based Importance Measures

# Description

Computes the importances of input variables, SNPs, or sets of SNPs, respectively, based on permutations of the response. Currently only available for the classification and the logistic regression approach of logic regression.

### Usage

```
vim.permInput(object, n.perm = NULL, standardize = TRUE,
  rebuild = FALSE, prob.case = 0.5, useAll = FALSE, version = 1,
  adjust = "bonferroni", addMatPerm = FALSE, rand=NA)

vim.permSNP(object, n.perm = NULL, standardize = TRUE,
  rebuild = FALSE, prob.case = 0.5, useAll = FALSE, version = 1,
  adjust = "bonferroni", addMatPerm = FALSE, rand = NA)

vim.permSet(object, set = NULL, n.perm = NULL, standardize = TRUE,
  rebuild = FALSE, prob.case = 0.5, useAll = FALSE, version = 1,
  adjust = "bonferroni", addMatPerm = FALSE, rand = NA)
```

### **Arguments**

object

an object of class logicBagg, i.e.\ the output of logic.bagging.

set

either a list or a character or numeric vector.

If NULL (default), then it will be assumed that data, i.e.\ the data set used in the application of logic.bagging, has been generated using make.snp.dummy or similar functions for coding variables by binary variables, i.e.\ with a function that splits a variable, say SNPx, into the dummy variables SNPx.1, SNPx.2, ... (where the "." can also be any other sign, e.g., an underscore).

If a character or a numeric vector, then the length of set must be equal to the number of variables used in object, i.e.\ the number of columns of data in the logicBagg object, and must specify the set to which a variable belongs either by an integer between 1 and the number of sets, or by a set name. If a variable should not be included in any of the sets, set the corresponding entry of set to NA. Using this specification of set it is not possible to assign a variable to more than one sets. For such a case, set set to a list (as follows).

If set is a list, then each object in this list represents a set of variables. Therefore, each object must be either a character or a numeric vector specifying either the names of the variables that belongs to the respective set or the columns of

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data that contains these variables. If names(set) is NULL, generic names will be employed as names for the sets. Otherwise, names(set) are used.

n.perm number of permutations used in the computation of the importances. By default

(i.e.\ if n.perm = NULL), 100 permutations are used if rebuild = TRUE and the regression approach of logic regression has been used in logic.bagging (by setting ntrees to an integer larger than 1, or glm.if.ltree = TRUE). Otherwise, 1000 permutation are employed. Note that actually much more permutations

should be used.

standardize should the standardized importance measure be used?

rebuild logical indicating whether the logic regression models should be rebuild (i.e.\

the parameters  $\beta$  of the generalized linear models should be recomputed) after removing a variable or a set of variables from the logic trees and for each permutation of the response. Note that setting rebuild = TRUE increases the

computation time substantially.

prob.case a numeric value between 0 and 1. If the logistic regression approach of logic

regression has been used in logic.bagging, then an observation will be classified as a case (or more exactly, as 1), if the class probability of this observation

is larger than prob. case. Otherwise, prob. case is ignored.

useAll logical indicating whether all m\* n.perm permuted values should be used in

the computation of the permutation based p-values, where m is the number of variables or sets of variables, respectively. If FALSE, the n. perm permuted values corresponding to the respective variable (or set of variables) are employed in the

determination of the p-value of this variable (or set of variables).

version either 1 or 2. If 1, then the importance measure is computed by 1 - padj, where

padj is the adjusted p-value. If 2, the importance measure is determined by log 10(padj), where a raw p-value equal to 0 is set to 1/(10 \* n.perm) to avoid

infinitive importances.

adjust character vector naming the method with which the raw permutation based p-

values are adjusted for multiplicity. If "qvalue", the function qvalue.cal from the package siggenes is used to compute q-values. Otherwise, p.adjust is used to adjust for multiple comparisons. See p.adjust for all other possible

specifications of adjust. If "none", the raw p-values will be used.

addMatPerm should the (n.perm + 1) x m matrix containing the original values (first column)

and the permuted values (the remaining columns) of the importance measure for

the m variables or m sets of variables be added to the output?

rand an integer for setting the random number generator in a reproducible state.

#### Value

An object of class logicFS containing

vim the values of the importance measure for the input variables, the SNPs, or the

sets of SNPs, respectively,

prop NULL,

primes the names of the inputs, SNPs, or sets of variables, respectively,

type the type of model (1: classification, 3: logistic regression),

param NULL,
mat.imp NULL,

measure the name of the used importance measure,

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threshold 0.95, i.e.\ the suggested threshold for calling an input, SNP or set of SNPs,

respectively, important (this is just used as default value when plotting the im-

portances, see argument thres of plot.logicFS),

 $\begin{array}{ll} \text{mu} & \text{NULL,} \\ \\ \text{useN} & \text{TRUE,} \end{array}$ 

name either "Variable", "SNP", or "Set",

mat.perm if addMatPerm = FALSE, NULL; otherwise, a matrix containing the original and

the permuted values of the respective importance measure.

### Author(s)

Holger Schwender, <holger.schwender@hhu.de>

#### References

Schwender, H., Ruczinski, I., Ickstadt, K. (2011). Testing SNPs and Sets of SNPs for Importance in Association Studies. *Biostatistics*, 12, 18-32.

#### See Also

logic.bagging, vim.input, vim.set, vim.signperm

vim.set

VIM for SNPs and Sets of Variables

# **Description**

Quantifies the importances of SNPs or sets of variables, respectively, contained in a logic bagging model.

#### Usage

```
vim.snp(object, useN = NULL, iter = NULL, standardize = NULL,
    mu = 0, addMatImp = FALSE, prob.case = 0.5,
    score = c("DPO", "Conc", "Brier", "PL"), ensemble = FALSE,
    rand = NULL)

vim.set(object, set = NULL, useN = NULL, iter = NULL, standardize = NULL,
    mu = 0, addMatImp = FALSE, prob.case = 0.5,
    score = c("DPO", "Conc", "Brier", "PL"), ensemble = FALSE,
    rand = NULL)
```

# **Arguments**

object an object of class logicBagg, i.e.\ the output of logic.bagging.

set either a list or a character or numeric vector.

If NULL (default), then it will be assumed that data, i.e.\ the data set used in the application of logic.bagging, has been generated using make.snp.dummy or similar functions for coding variables by binary variables, i.e.\ with a function

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that splits a variable, say SNPx, into the dummy variables SNPx.1, SNPx.2, ... (where the "." can also be any other sign, e.g., an underscore).

If a character or a numeric vector, then the length of set must be equal to the number of variables used in object, i.e.\ the number of columns of data in the logicBagg object, and must specify the set to which a variable belongs either by an integer between 1 and the number of sets, or by a set name. If a variable should not be included in any of the sets, set the corresponding entry of set to NA. Using this specification of set it is not possible to assign a variable to more than one sets. For such a case, set set to a list (as follows).

If set is a list, then each object in this list represents a set of variables. Therefore, each object must be either a character or a numeric vector specifying either the names of the variables that belongs to the respective set or the columns of data that contains these variables. If names(set) is NULL, generic names will be employed as names for the sets. Otherwise, names(set) are used.

logical specifying if the number of correctly classified out-of-bag observations should be used in the computation of the importance measure. If FALSE, the proportion of correctly classified oob observations is used instead. If NULL (default), then the specification of useN in object is used. In the survival case, useN is ignored.

integer specifying the number of times the values of the variables in the respective set are permuted in the computation of the importance of this set. If NULL (default), the values of the variables are not permuted, but all variables belonging to the set are removed from the model. Permutation of variables is not available in the survival case, i.e. iter is set to NULL.

should a standardized version of the importance measure for a set of variables be returned? By default, standardize = TRUE is used in the classification and the (multinomial) logistic regression case, and standarize is set to FALSE in the linear regression case. Standardization is not available in the survival case. For details, see mu.

a non-negative numeric value. Ignored if standardize = FALSE. Otherwise, a t-statistic for testing the null hypothesis that the importance of the respective set is equal to mu is computed.

should the matrix containing the improvements due to each of the sets in each of the logic regression models be added to the output? If ensemble = TRUE and addMatImp = TRUE in the survival case, the respective score of the full model is added to the output instead of an improvement matrix.

a numeric value between 0 and 1. If the logistic regression approach of logic regression has been used in logic.bagging, then an observation will be classified as a case (or more exactly, as 1), if the class probability of this observation is larger than prob.case. Otherwise, prob.case is ignored.

a character string naming the score that should be used in the computation of the importance measure for a survival time analysis. By default, the distance between predicted outcomes (score = "DPO") proposed by Tietz et al.\ (2018) is used in the determination of the importance of the variables. Alternatively, Harrell's C-Index ("Conc"), the Brier score ("Brier"), or the predictive partial log-likelihood ("PL") can be used.

in the case of a survival outcome, should ensemble importance measures (as, e.g., in randomSurvivalSRC be used? If FALSE, importance measures analogous to the ones in the logicFS analysis of other outcomes are used (see Tietz et al., 2018)

an integer for setting the random number generator in a reproducible state.

useN

iter

standardize

mu

addMatImp

prob.case

score

ensemble

rand

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#### Value

An object of class logicFS containing

vim the importances of the sets of variables,

prop NULL,

primes the names of the sets of variables,

type the type of model (1: classification, 2:linear regression, 3: logistic regression, 4:

Cox regression),

param further parameters (if addInfo = TRUE in the previous call of logic.bagging),

or NULL (otherwise),

mat.imp either a matrix containing the improvements due to the sets of variables for each

of the models (if addMatImp = TRUE and ensemble = FALSE), or the respective score of the full model (if addMatImp = TRUE and ensemble = TRUE, or NULL (if

addMatImp = FALSE),

measure the name of the used importance measure,

useN the value of useN,

threshold NULL if standardize = FALSE, otherwise the 1 - 0.05/m quantile of the t-

distribution with B-1 degrees of freedom, where m is the number of sets

and B is the number of logic regression models composing object,

mu (if standardize = TRUE), or NULL (otherwise),

iter iter,
name "Set".

### Author(s)

Holger Schwender, <holger.schwender@hhu.de>; Tobias Tietz, <tobias.tietz@hhu.de>

### References

Schwender, H., Ruczinski, I., Ickstadt, K. (2011). Testing SNPs and Sets of SNPs for Importance in Association Studies. *Biostatistics*, 12, 18-32.

Tietz, T., Selinski, S., Golka, K., Hengstler, J.G., Gripp, S., Ickstadt, K., Ruczinski, I., Schwender, H. (2018). Identification of Interactions of Binary Variables Associated with Survival Time Using survivalFS. Submitted.

### See Also

logic.bagging, logicFS, vim.logicFS, vim.input, vim.ebam, vim.chisq

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