The GOSim package

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1 Introduction

The Gene Ontology (GO) has become one of the most widespread systems for systematically annotating gene products within the bioinformatics community and is developed by the Gene Ontology Consortium (The Gene Ontology Consortium, 2004). It is specifically intended for describing gene products with a controlled and structured vocabulary. GO terms are part of a Directed Acyclic Graph (DAG), covering three orthogonal taxonomies or "aspects": molecular function, biological process and cellular component. Two different kinds of relationship between GO terms exist: the "is-a" relationship and the "part-of" relationship. Providing a standard vocabulary across any biological resources, the GO enables researchers to use this information for automated data analysis.

The GOSim package (Fröhlich et al., 2007) provides the researcher with various information theoretic similarity concepts for GO terms (Resnik, 1995, 1999; Lin, 1998; Jiang and Conrath, 1998; Lord et al., 2003; Couto et al., 2003, 2005). Moreover, since version 1.1.5 GOSim contains several new similarity concepts, which are based on so-called diffusion kernel techniques (Lerman and Shakhnovich, 2007). Additionally GOSim implements different methods for computing functional similarities between gene products based on the similarties between the associated GO terms (Speer et al., 2005; Fröhlich et al., 2006; Schlicker et al., 2006; Lerman and Shakhnovich, 2007; del Pozo et al., 2008). This can, for instances, be used for clustering genes according to their biological function (Speer et al., 2005; Fröhlich et al., 2006) and thus may help to get a better understanding of the biological aspects covered by a set of genes.

Since version 1.1 *GOSim* additionally offers the possibility of a GO enrichment analysis using the topGO package (Alexa et al., 2006). Hence, *GOSim* acts now as an umbrella for different analysis methods employing the GO structure.

2 Usage of GOSim

To elucidate the usage of GOSim we show an example workflow and explain the employed similarity concepts. We create a character vector of Entrez gene IDs, which we assume to be from human:

- > library(GOSim)
- > genes=c("207","208","596","901","780","3169","9518","2852","26353","8614","7494",

Next we investigate the GO annotation within the current ontology (which is *biological process* by default):

> getGOInfo(genes)

	207	208	596	901	780
go_id	Character, 144	Character,33	Character,11	l3 Character,	4 Character,24
Term	Character, 144	Character,33	Character,11	l3 Character,	4 Character,24
Definition	Character, 144	Character,33	Character,11	l3 Character,	4 Character,24
IC	Numeric,144	Numeric,33	Numeric,113	Numeric,4	Numeric,24
	3169	9518	2852	26353	8614
go_id	Character,31	Character,17	Character,53	Character,4	Character,14
Term	Character,31	Character,17	Character,53	Character,4	Character,14
Definition	Character,31	Character, 17	Character,53	Character,4	Character,14
IC	Numeric,31	Numeric,17	Numeric,53	Numeric,4	Numeric,14
	7494				
go_id	Character,55				
Term	Character,55				
Definition	Character,55				
IC	Numeric,55				

2.1 Term Similarities

Let us examine the similarity of the GO terms for genes "8614" and "2852" in greater detail:

> getTermSim(c("GO:0007166","GO:0007267","GO:0007584","GO:0007165","GO:0007186"),me

```
GD:0007166 GD:0007267 GD:0007584 GD:0007165 GD:0007186
GD:0007166
           0.2628131
                       0.1806383
                                  0.1266641
                                             0.1945233
                                                         0.1945233
GO:0007267
            0.1806383
                       0.3551639
                                  0.0000000
                                             0.1806383
                                                         0.1806383
GD:0007584 0.1266641
                       0.0000000
                                  0.5128961
                                             0.1266641
                                                         0.1266641
GD:0007165
           0.1945233
                       0.1806383
                                  0.1266641
                                              0.1945233
                                                         0.1945233
GD:0007186
            0.1945233
                       0.1806383
                                  0.1266641
                                              0.1945233
                                                         0.4016432
```

This calculates Resnik's pairwise similarity between GO terms (Resnik, 1995, 1999):

$$sim(t, t') = IC_{ms}(t, t') := \max_{\hat{t} \in Pa(t, t')} IC(\hat{t})$$
 (1)

Here Pa(t, t') denotes the set of all common ancestors of GO terms t and t', while IC(t) denotes the information content of term t. It is defined as (e.g. Lord et al. (2003))

$$IC(\hat{t}) = -\log P(\hat{t}) \tag{2}$$

i.e. as the negative logarithm of the probability of observing \hat{t} . The information content of each GO term is already precomputed for each ontology based on the empirical observation, how many times a specific GO term or any of its direct or indirect offsprings appear in the annotation of the GO with gene products. GOSim provides a normalized version of Resnik's similarity measure, which divides the information content of the minimum subsumber by the maximum information content of all GO terms, hence obtaining a number between 0 and 1.

```
> data("ICsBPhumanall")
> IC[c("GD:0007166","GD:0007267","GD:0007584","GD:0007165","GD:0007186")]
GD:0007166 GD:0007267 GD:0007584 GD:0007165 GD:0007186
   3.006413   4.062846   5.867200   2.225221   4.594539
```

This loads the information contents of all GO terms within "biological process". Likewise, the data files ICsMFhumanall and ICsCChumanall contain the information contents of all GO terms within "molecular function" and "cellular component" for human. Since GOSim version 1.1.4.0 the information content of GO terms relies on the mapping of primary gene IDs (mainly Entrez) to GO terms provided by the libraries org.Dm.eg.db (fly), org.Hs.eg.db (human), org.Mm.eg.db (mouse), etc. Additionally, it is possible to pass a user provided mapping via the function setEvidenceLevel. Please refer to the manual pages for details. If only GO terms having certain evidence codes should be considered, one must explicitly calculate the corresponding information contents in the function calcICs. Again, more information on this function can be found in the manual pages.

To continue our example from above, let us also calculate Jiang and Conrath's pairwise similarity between GO terms, which is the default, for compairson reasons (Jiang and Conrath, 1998):

```
> getTermSim(c("GD:0007166", "GD:0007267", "GD:0007584", "GD:0007165", "GD:0007186"), ve
```

```
GD:0007166 GD:0007267 GD:0007584 GD:0007165 GD:0007186
GD:0007166
            0.9505312
                        0.5105747
                                    0.2498911
                                               0.7587689
                                                           0.5222505
GD:0007267
            0.5105747
                        0.9828000
                                    0.0000000
                                               0.5740054
                                                           0.4169139
GO:0007584
            0.2498911
                        0.0000000
                                    0.9971692
                                               0.2740140
                                                           0.2119568
GD:0007165
            0.7587689
                        0.5740054
                                    0.2740140
                                               0.8919565
                                                           0.5820734
GD:0007186
                                               0.5820734
            0.5222505
                        0.4169139
                                    0.2119568
                                                           0.9898931
```

Jiang and Conrath's similarity measure is defined as

$$sim(t, t') = 1 - \min(1, IC(t) - 2IC_{ms}(t, t') + IC(t'))$$
(3)

i.e. the similarity between t and t' is 0, if their normalized distance is at least 1.

Likewise, we can also compute Lin's pairwise similarity between GO terms (Lin, 1998):

> getTermSim(c("GD:0007166","GD:0007267","GD:0007584","GD:0007165","GD:0007186"),m

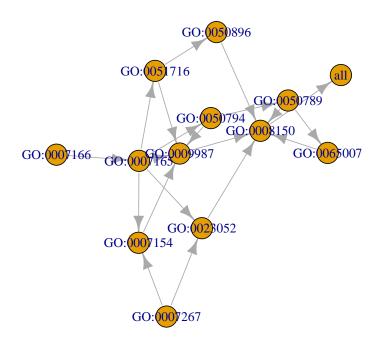
```
GD:0007166 GD:0007267 GD:0007584 GD:0007165 GD:0007186
GD:0007166
           1.0000000 0.5846115
                                0.3265762
                                          0.8506792 0.5855112
GD:0007267
           0.5846115
                     1.0000000
                                0.0000000 0.6572401 0.4773693
GD:0007584 0.3265762 0.0000000
                                1.0000000 0.3581018
                                                      0.2770009
GD:0007165 0.8506792 0.6572401
                                0.3581018
                                          1.0000000 0.6525805
GO:0007186
           0.5855112 0.4773693
                                0.2770009 0.6525805
                                                     1.0000000
```

It is defined as:

$$sim(t,t') = \frac{2IC_{ms}(t,t')}{IC(t) + IC(t')}$$
(4)

Resnik's, Jiang-Conraths's and Lin's term similarities all refer to $IC_{ms}(t,t')$, the information content of the minimum subsumer of t and t', i.e. of the lowest common ancestor in the hierarchy. For illustration let us plot the GO graph with leaves GO:0007166 and GO:0007267 and let us compute their minimum subsumer (see Fig. ??):

- > library(igraph)
- > G = getGOGraph(c("GO:0007166", "GO:0007267"))
- > G2 = igraph.from.graphNEL(G)
- > plot(G2, vertex.label=V(G2)\$name)



> getMinimumSubsumer("GO:0007166", "GO:0007267")

[1] "GD:0023052"

In contrast to the above defined similarity measures Couto et al. (Couto et al., 2005) introduced a concept, which is not based on the minimum subsumer, but on the set of all disjunctive common ancestors. Roughly speaking, the idea is not to consider the common ancestor having the highest information content only, but also others, if they are somehow "separate" from each other, i.e. there exists a path to t or to t' not passing any other of the disjunctive common ancestors.

> getDisjCommAnc("GO:0007166", "GO:0007267")

[1] "GD:0007154" "GD:0009987" "GD:0023052"

In this case the set of disjunctive common ancestors consists of the minimum subsumer, GO:0007154, and its parent, GO:0009987, because from both there exists a path to GO:0007166 not passing any other disjunctive common ancestor(see Fig. ??).

Based on the notion of disjunctive common ancestors Resnik's similarity concept can be extended by defining:

$$sim(t, t') = IC_{share}(t, t') = \frac{1}{|DisjCommAnc|} \sum_{t \in DisjCommAnc} IC(t)$$
 (5)

Likewise, Jiang-Conraths's and Lin's measures can be extended as well by replacing $IC_{ms}(t,t')$ by $IC_{share}(t,t')$.

> getTermSim(c("GO:0007166", "GO:0007267"), method="CoutoResnik", verbose=FALSE)

GD:0007166 GD:0007267

GD:0007166 3.006413 1.507568 GD:0007267 1.507568 4.062846

Finally, it should be mentioned that also the depth and density enriched term similarity by Couto et al. (Couto et al., 2003) has been integrated into *GOSim*:

- > setEnrichmentFactors(alpha=0.5,beta=0.3)
- > getTermSim(c("GO:0007166", "GO:0007267"), method="CoutoEnriched", verbose=FALSE)

GD:0007166 GD:0007267

GD:0007166 9.038517 0.00000 GD:0007267 0.000000 16.50672

0.5222505

GO:0007186

Since version 1.1.5 GOSim contains several new similarity concepts, which are based on so-called diffusion kernel techniques (Lerman and Shakhnovich, 2007) rather than on the information theoretic ideas presented before. For using these similarity measures it is necessary to pre-compute a diffusion kernel on the Gene Ontology graph via calc.diffusion.kernel. This will take some time and result in a kernel/similarity matrix that is stored in a file called e.g. 'diffKernelpowerBPhumanall.rda' (meaning matrix power diffusion kernel for ontology BP in human using all evidence codes) in the current working directory. Once the kernel is created, it has to be loaded into the environment first load.diffusion.kernel. Afterwards GO term similarities can be computed via function getTermSim. Please check the manual pages for details.

Since version 1.2 *GOSim* also contains Schlicker et al.'s GO term similarity measure (Schlicker et al., 2006), which is an adaption of Lin's similarity measure. Moreover, the graph information content similarity by Pesquita et al. has been implemented (Pesquita et al., 2007).

> getTermSim(c("GO:0007166", "GO:0007267", "GO:0007584", "GO:0007165", "GO:0007186"), mo

0.5820734

0.9898931

GD:0007166 GD:0007267 GD:0007584 GD:0007165 GD:0007186

0.2119568

GD:0007166 0.9505312 0.5105747 0.2498911 0.7587689 0.5222505 GO:0007267 0.5105747 0.9828000 0.0000000 0.5740054 0.4169139 GO:0007584 0.2498911 0.0000000 0.9971692 0.2740140 0.2119568 GO:0007165 0.7587689 0.5740054 0.2740140 0.8919565 0.5820734

0.4169139

2.2 Functional Gene Similarities

The special strength of *GOSim* lies in the possibility not only to calculate similarities for individual GO terms, but also for genes based on their complete GO annutation. Since *GOSim* version 1.1.5 for this purpose the following ideas have been implemented:

- 1. Maximum (Couto et al., 2003) and average pairwise GO term similarity
- 2. Average of best matching GO term similarities (Schlicker et al., 2006).
- 3. Computation of a so-called *optimal assignment* of terms from one gene to those of another one (Fröhlich et al., 2006).
- 4. Similarity derived from Hausdorff distances between sets (del Pozo et al., 2008).
- 5. Embedding of each gene into a feature space: (Speer et al., 2005; Fröhlich et al., 2006) proposed to define feature vectors by a gene's maximum GO term similarity to certain prototype genes. More simple (but probably also less accurate), (Mistry and Pavlidis, 2008) recently proposed to represent each gene by a feature vector describing the presence/absence of all GO terms. The absence of each GO term is additionally weighted by its information content. Within a feature space gene functional similarities naturally arise as dot products between feature vectors. These dot products can be understood as so-called kernel functions (Schölkopf and Smola, 2002), as used in e.g. Support Vector Machines (Cortes and Vapnik, 1995). Depending on the choice of later normalization (see below) one can arrive at the cosine similarity (Eq. 6), at the Tanimoto coefficient (Eq. 7) or at a measure similiar to Lin's one (Eq. 8, Eq. 4).

2.2.1 Normalization of Similarities

Often, people want to normalize similarities, e.g. on the interval [0,1], for better interpretation. To do so, we can perform the transformation

$$sim_{gene}(g, g') \leftarrow \frac{sim_{gene}(g, g')}{\sqrt{sim_{gene}(g, g)sim_{gene}(g', g')}}$$
 (6)

Provided $sim_{gene} \geq 0$, the consequence will be a similarity of 1 for g with itself and between 0 and 1 for g with any other gene. In case of a feature space embedding this transformation is equivalent to computing the cosine similarity between two feature vectors.

Another possibility is to use Lin's normalization (see Eq. 4):

$$sim_{gene}(g, g') \leftarrow \frac{2sim_{gene}(g, g')}{sim_{gene}(g, g) + sim_{gene}(g', g')}$$
 (7)

Furthermore, one can use a normalization in the spirit of the Tanimoto coefficient:

$$sim_{gene}(g, g') \leftarrow \frac{sim_{gene}(g, g')}{sim_{gene}(g, g) + sim_{gene}(g', g') - sim_{gene}(g, g')}$$
 (8)

In case of a feature space embedding the transformation corresponds exactly to the Tanimoto coefficient betweem two feature vectors.

We now give a more detailed overview over the different similarity concepts mentioned above.

2.2.2 Maximum and Average Pairwise GO Term Similarity

The idea of the maximum pairwise GO term similarity is straight forward. Given two genes g and g' annotated with GO terms $t_1, ..., t_n$ and $t'_1, ..., t'_m$ we define the functional similarity between between g and g' as

$$sim_{gene}(g, g') = \max_{i = 1, \dots, n} sim(t_i, t'_j)$$

$$j = 1, \dots, m$$

$$(9)$$

where sim is some similarity measure to compare GO terms t_i and t'_j . This idea is, for instance, realized in FuSSiMeg (Couto et al., 2003). Instead of computing the maximum pairwise GO term similarity one may also take the average here.

2.2.3 Average of Best Matching GO Term Similarities

The idea of this approach (Schlicker et al., 2006) is to assign each GO term t_i occuring in gene g to its best matching partner $t'_{\pi i}$ in gene g'. Hence multiple GO terms from gene g can be assigned to one GO term from gene g'. A similarity score is computed by taking the average similarity of assigned GO terms. Since, however, genes can have an unequal number of GO terms the result depends on whether GO terms of gene g are assigned to those of gene g' or vice versa. Hence, in Schlicker et al. (2006) it was proposed to either take the maximum or the average of both similarity scores. Both strategies are implemented in GOSim.

2.2.4 Optimal Assignment Gene Similarities

To elucidate the idea of the optimal assignment (Fröhlich et al., 2006), consider the GO terms associated with gene "8614" on one hand and gene "2852" on the other hand:

> getGOInfo(c("8614","2852"))

go_id Character,14 Character,53
Term Character,14 Character,53
Definition Character,14 Character,53
IC Numeric,14 Numeric,53

Given a similarity concept sim to compare individual GO terms, the idea is now to assign each term of the gene having fewer annotation to exactly one term of the other gene such that the overall similarity is maximized. More formally the optimal assignment problem can be stated as follows: Let π be some permutation of either an n-subset of natural numbers $\{1, ..., m\}$ or an m-subset of natural numbers $\{1, ..., n\}$ (this will be clear from context). Then we are looking for the quantity

$$sim_{gene}(g, g') = \begin{cases} \max_{\pi} \sum_{i=1}^{n} sim(t_i, t'_{\pi(i)}) & \text{if } m > n \\ \max_{\pi} \sum_{j=1}^{m} sim(t_{\pi(j)}, t'_j) & \text{otherwise} \end{cases}$$
 (10)

The computation of (10) corresponds to the solution of the classical maximum weighted bipartite matching (optimal assignment) problem in graph theory and can be carried out in $O(\max(n, m)^3)$ time (Mehlhorn and Näher, 1999). To prevent that larger lists of terms automatically achieve a higher similarity we may further sim_{gene} divide 10 by $\max(m, n)$.

In our example, using Lin's GO term similarity measure the following assignments yielding a corresponding similarity matrix are found:

```
> getGeneSim(c("8614","2852"),similarity="OA",similarityTerm="Lin",avg=FALSE, verb
```

filtering out genes not mapping to the currently set GO category \dots ===> list of 2 8614 2852

8614 1.0000000 0.3672487

2852 0.3672487 1.0000000

Note the difference to a gene similarity that is just based on the maximum GO term similarity and to a gene similarity that is based on the average of best matching GO terms:

> getGeneSim(c("8614","2852"),similarity="max",similarityTerm="Lin",verbose=FALSE)

filtering out genes not mapping to the currently set GO category ... ===> list of 2 8614 2852

8614 1.0000000 0.9827528

2852 0.9827528 1.0000000

> getGeneSim(c("8614","2852"),similarity="funSimMax",similarityTerm="Lin",verbose=

filtering out genes not mapping to the currently set GO category ... ===> list of 2 8614 2852

8614 1.0000000 0.7002258

2852 0.7002258 1.0000000

2.2.5 Gene Similarities In the Spirit of Hausdorff Metrics

Hausdorff metrics are a general concept for measuring distances between compact subsets of a metric space. Let X and Y be the two sets of GO terms associated to genes g and g', and let d(t,t') denote the distance between GO terms t and t'. Then the Hausdorff distance X and Y is defined as

$$d_{Hausdorff}(X,Y) = \max\{\sup_{t \in X} \inf_{t' \in Y} d(t,t'), \sup_{t' \in Y} \inf_{t \in X} d(t,t')\}$$
(11)

Using Hausdorff metrics for measuring gene functional distances was proposed in del Pozo et al. (2008). We translate the idea to define a similarity measure between g and g' (see the difference to previous GOSim versions):

$$sim_{gene}(q, q') = \exp(-d_{Hausdorff}(q, q'))$$
 (12)

> getGeneSim(c("8614","2852"),similarity="hausdorff",similarityTerm="Lin",verbose=

filtering out genes not mapping to the currently set GO category \dots ===> list of 2 8614 2852

8614 1.0000000 0.9873622

2852 0.9873622 1.0000000

2.2.6 Feature Space Embedding of Gene Products

The Simple Approach Mistry and Pavlidis (2008) proposed to represent each gene by a feature vector describing the presence/absence of all GO terms. The absence of each GO term is additionally weighted by its information content. In the feature space similarities arise as dot products. Hence, the similarity between two GO terms t and t' is implicitly defined as the product of their information content values, hence igoring the exact DAG structure of the Gene Ontology as employed by the GO term similarity measures explained in the beginning of this document.

> getGeneSim(c("8614","2852"),similarity="dot",method="Tanimoto", verbose=FALSE)

filtering out genes not mapping to the currently set GO category ... ===> list of 2 8614 2852

8614 1.00000000 0.06486856

2852 0.06486856 1.00000000

This will calculate the Tanimoto coefficient between feature vectors as a similarity measure. It is possible to retrieve the feature vectors via:

> features = getGeneFeatures(c("8614","2852"))

filtering out genes not mapping to the currently set GO category ... ===> list of 2

Embeddings via GO Term Similarities to Prototype Genes This approach is due to Speer et al. (2005); Fröhlich et al. (2006). The idea is to define a feature vector for each gene by its pairwise GO term similarity to certain prototype genes, i.e. the prototype genes form a (nonorthogonal) basis, and each gene is defined relative to this basis. The prototype genes can eithed be defined a priori or one can use one of the heuristics implemented in the function selectPrototypes. The default behavior is to select the 250 best annotated genes, i.e. which have been annotated with GO terms most often, but here we just use 3 for computational reasons:

> proto = selectPrototypes(n=3,verbose=FALSE)

We now calculate for each gene g feature vectors $\phi(g)$ by using their similarity to all prototypes $p_1, ..., p_n$:

$$\phi(g) = (sim'(g, p_1), ..., sim'(g, p_n))^T$$
(13)

Here sim' by default is the maximum pairwise GO term similarity. Alternatively, one can use other similarity measures for sim' as well. These similarity measures can by itself again be combined with arbitrary GO term similarity concepts. The default is the Jiang-Conrath term similarity.

Because the feature vectors are very high-dimensional we usually perform a principal component analysis (PCA) to project the data into a lower dimensional subspace. The results are not shown here due to long computation time.

> PHI = getGeneFeaturesPrototypes(genes, prototypes=proto, verbose=FALSE)

This uses the above define prototypes to calculate feature vectors and performs a PCA afterwards. The number of principal components is chosen such that at least 95% of the total variance in feature space can be explained (this is a relatively conservative criterion).

We can now plot our genes in the space spanned by the first 2 principal components to get an impression of the relative "position" of the genes to each other in the feature space (see Fig. ??). The feature vectors are normalized to Euclidian norm 1 by default:

- > x=seq(min(PHI\$features[,1]),max(PHI\$features[,1]),length.out=100)
- > y=seq(min(PHI\$features[,2]),max(PHI\$features[,2]),length.out=100)
- > plot(x,y,xlab="principal component 1",ylab="principal component 2",type="n")
- > text(PHI\$features[,1],PHI\$features[,2],labels=genes)

Finally, we can directly calculate the similarities of the genes to each other, this time using the Resnik's GO term similarity concept. These similarities may then be used to cluster genes with respect to their function:

- > plot(h,xlab="")

This produces a hierarchical clustering of all genes using average linkage clustering (see Fig. 2).

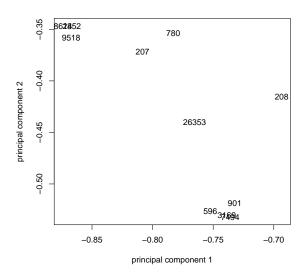


Figure 1: Embedding of genes into feature space spanned by the first 2 principal components

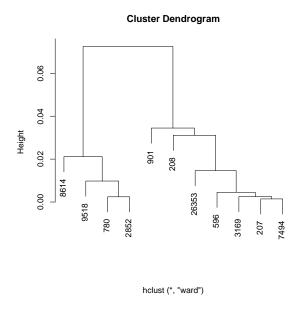


Figure 2: Possible functional clustering of the genes using Ward's method.

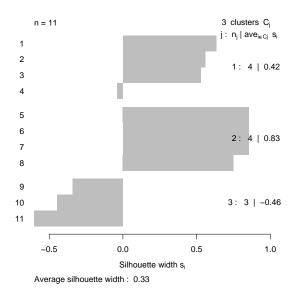


Figure 3: Silhouette plot of a possible given grouping of genes.

2.2.7 Combination of Similarities from Different Ontologies

It should be mentioned that up to now all similarity computations were performed within the ontology "biological process". One could imagine to combine functional similarities between gene products with regard to different taxonomies. An obvious way for doing so would be to consider the sum of the respective similarities:

$$sim_{total}(g, g') = sim_{Ontology1}(g, g') + sim_{Ontology2}(g, g')$$
 (14)

Of course, one could also use a weighted averaging scheme here, if desired.

2.3 Cluster Evaluations

GOSim has the possibility to evaluate a given clustering of genes or terms by means of their GO similarities. Supposed, based on other experiments (e.g. microarry), we have decided to put genes "8614", "9518", "780", "2852" in one group, genes "3169", "207", "7494", "596" in a second and the rest in a third group. Then we can ask ourselves, how similar these groups are with respect to their GO annotations:

A good indiciation of the clustering quality can be obtained by looking at the cluster silhouettes (Rousseeuw, 1987) (see Fig. 3). This shows that clusters 1 and 2 are relatively homogenous with respect to the functional similarity of the genes contained in it, while the genes in cluster 3 are more dissimilar.

2.4 GO Enrichment Analysis

Since version 1.1 *GOSim* also offers the possibility of a GO enrichment analysis. Suppose, we may now want to get a clearer picture of the genes involved in cluster 1. For this purpose we use the topGO tool (Alexa et al., 2006).

```
> library(org.Hs.eg.db)
```

- > library(topGO)
- > allgenes = union(c("8614", "9518", "780", "2852"), sample(keys(org.Hs.egGO), 1000)
- > GOenrichment(c("8614", "9518", "780", "2852"), allgenes) # print out what cluster

\$GOTerms

13108 16740 17949 24787 33709 42961 48275 51718 65425 69856 69993 72176	go_id GO:0007169 GO:0006874 GO:0007566 GO:0010817 GO:0022411 GO:0033993 GO:0040015 GO:0043410 GO:0048468 GO:0051128 GO:0051149 GO:0051896
72176 72261 80291	

Term

13108 transmembrane receptor protein tyrosine kinase signaling pat	thway
16740 cellular calcium ion homeost	tasis
17949 embryo implanta	ation
24787 regulation of hormone le	evels
33709 cellular component disasse	embly
42961 response to 1	lipid
negative regulation of multicellular organism gr	rowth
51718 positive regulation of MAPK cas	scade
65425 cell develop	pment
regulation of cellular component organization	ation
positive regulation of muscle cell differentia	ation
72176 regulation of protein kinase B signs	aling
72261 regulation of calcium ion trans	sport
cellular response to peptide hormone stir	nulus

```
13108
                                                                     A series of mole
16740
17949
24787 Any process that modulates the levels of hormone within an organism or a tissu
33709
42961
48275
51718
65425
69856
                                                        Any process that modulates th
69993
72176
72261
80291
           Any process that results in a change in state or activity of a cell (in t
$p.values
                                         GD:0010817
                                                       GD:0006874
  GD:0040015
               GD:0033993
                            GD:0048468
                                                                    GO:0051924
0.0003717940 0.0054093776 0.0067171487 0.0018349191 0.0054093776 0.0012286110
  GO:0051896
               GD:0007566
                            GO:0051128
                                         GO:0051149
                                                       GO:0043410
                                                                    GO:0022411
0.0003717940 0.0001244684 0.0096044100 0.0001244684 0.0092533319 0.0078643265
  GD:0071375
               GO:0007169
0.0033954354 0.0004368662
$genes
$genes$`GO:0040015`
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