Package 'diagL1'

January 30, 2024

Title Routines for Fit, Inference and Diagnostics in Linear L1 and LAD Models
Version 1.0.0
Author Kevin Allan Sales Rodrigues [aut, cre] (<https: 0000-0003-4925-5883="" orcid.org="">), Silvia Nagib Elian [ctb, ths]</https:>
Maintainer Kevin Allan Sales Rodrigues <kevin.asr@outlook.com></kevin.asr@outlook.com>
Description Diagnostics for linear L1 regression (also known as LAD - Least Absolute Deviations), including: estimation, confidence intervals, tests of hypotheses, measures of leverage, methods of diagnostics for L1 regression, special diagnostics graphs and measures of leverage. The algorithms are based in Dielman (2005) <doi:10.1080 0094965042000223680="">, Elian et al. (2000) <doi:10.1080 03610920008832518=""> and Dodge (19) age builds on the 'quantreg' package, which is a well-established package for tuning quantile regression models. There are also tests to verify if the errors have a Laplace distribution based on the work of Puig and Stephens (2000) <doi:10.2307 1270952="">.</doi:10.2307></doi:10.1080></doi:10.1080>
License GPL (>= 2)
Depends R (>= 3.5), quantreg (>= 5.97), greekLetters (>= 1.0.2)
Encoding UTF-8
LazyData true
Imports stats, methods, conquer, lawstat, MatrixModels, Matrix, MASS, cubature, doParallel, foreach
RoxygenNote 7.2.3
NeedsCompilation no
Repository CRAN
Date/Publication 2024-01-30 00:30:02 UTC

R topics documented:

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bile

Bile Data

Description

A dataset containing lithogenic bile concentrations in 29 Pima Indians. For 29 females, the data give age and percent saturation of bile cholesterol.

Usage

data(bile)

Format

A data frame with 29 rows and 2 variables.

boot.regL1

Details

- Age: age in years of each female indian
- Concentration: percent saturation of bile cholesterol

References

Goodall, C. (1983). Examining Residuals. In Hoaglin, D. C., Mosteller, F. and Tukey, J. W. (1983). Understanding Robust and Exploratory Data Analysis. *Wiley series in probability and mathematical statistics*.

boot.regL1

Bootstrapping Linear L1 Models

Description

This function can be used to construct standard errors, confidence intervals and tests of hypotheses regarding linear L1 regression models. The bootstrap method used compute xypairs bootstrap for linear L1 regression.

Usage

boot.regL1(x, y, R = 1000)

Arguments

х	the regression design matrix.
У	the regression response vector.
R	the number of bootstrap replications.

Value

A list consisting of four elements: a vector of lambda mle estimate for each bootstrap sample and another vector with empirical quantiles. A matrix B of dimension R by p is returned with the R resampled estimates of the vector of L1 linear regression parameters. A matrix U of sampled indices.

See Also

boot.rq Bootstrapping Quantile Regression from package quantreg.

```
data(stackloss)
bt1 = boot.regL1(stack.x, stack.loss, 1000)
plot(bt1$lambda_mle)
```

boot_het.regL1

Description

This function can be used to construct standard errors, confidence intervals and tests of hypotheses regarding linear L1 regression models. The bootstrap method used compute xypairs bootstrap for linear L1 regression.

Usage

boot_het.regL1(x, y, groups, R = 1000)

Arguments

x	the regression design matrix.
У	the regression response vector.
groups	vector with the group index associated with the observation, observations with the same index belong to the same group.
R	the number of bootstrap replications.

Value

A list consisting of four elements: a vector of lambda mle estimate for each bootstrap sample and another vector with empirical quantiles. A matrix B of dimension R by p is returned with the R resampled estimates of the vector of L1 linear regression parameters. A matrix U of sampled indices.

See Also

boot.rq Bootstrapping Quantile Regression from package quantreg.

```
set.seed(123)
x1 = matrix(rnorm(20), ncol = 2)
y1 = x1[, 1] + x1[, 2] + rlaplace(10, 0, 5)
x2 = matrix(rnorm(20), ncol = 2)
y2 = x2[, 1] + x2[, 2] + rlaplace(10, 0, 10)
x3 = matrix(rnorm(20), ncol = 2)
y3 = x3[, 1] + x3[, 2] + rlaplace(10, 0, 15)
x4 = matrix(rnorm(20), ncol = 2)
y4 = x4[, 1] + x4[, 2] + rlaplace(10, 0, 20)
x5 = matrix(rnorm(20), ncol = 2)
y5 = x5[, 1] + x5[, 2] + rlaplace(10, 0, 30)
y = c(y1, y2, y3, y4, y5)
```

class_to_regL1

```
x = rbind(x1, x2, x3, x4, x5)
group_index = c(rep(1,10),rep(2,10),rep(3,10),rep(4,10),rep(5,10))
bt1 = boot_het.regL1(x, y, group_index, 1000)
bt1$lambda_mle_het
```

class_to_regL1 Change object class from "rq" to "regL1"

Description

Changing the object's class from "rq" to "regL1" allows you to use functions from the 'diagL1' package normally.

Usage

class_to_regL1(object)

Arguments

object Object from "rq" class.

Value

Object with class "regL1".

See Also

regL1 for fitting linear L1 models. rq for fitting linear L1 models.

class_to_rq Change object class from "regL1" to "rq"

Description

Changing the object's class from "regL1" to "rq" allows you to use functions from the 'quantreg' package normally.

Usage

class_to_rq(object)

Arguments

object Object from "regL1" class.

Object with class "rq".

See Also

regL1 for fitting linear L1 models. rq for fitting linear L1 models.

CookDistance Calculate Cook Distance

Description

Calculate Cook Distance

Usage

CookDistance(model)

Arguments

model Object returned from regL1 representing the fit of the L1 model.

Value

Cook Distance A vector with Cook Distance for each observation.

References

•

Sun, R.-B. and Wei, B.-C. (2004). On influence assessment for lad regression. *Statistics & Probability Letters*, **67**, 97-110. doi:10.1016/j.spl.2003.08.018.

```
set.seed(123)
x = matrix(rnorm(100), ncol = 2)
y = x[, 1] + x[, 2] + rlaplace(50, 0, 5)
# Fits a linear regression L1 model
mod1 = regL1(y ~ x)
CookDistance(mod1)
```

dlaplace

Description

Probability density function (PDF) of the Laplace distribution

Usage

dlaplace(x, location = 0, scale = 1)

Arguments

х	Values for which to calculate the probability density.
location	Location parameter of the Laplace distribution (default = 0).
scale	Scale parameter of the Laplace distribution (default = 1).

Value

Vector of calculated probability densities.

Examples

dlaplace(0, 0, 1)

FD	F Distance

Description

F Distance

Usage

FD(model, norm = 2)

Arguments

model	Object returned from regL1 representing the fit of the L1 model.
norm	Type of norm, there are two types, 1 (norm L1) and 2 (norm L2). The default is norm L2.

Value

.

References

Sun, R.-B. and Wei, B.-C. (2004). On influence assessment for lad regression. *Statistics & Probability Letters*, **67**, 97-110. doi:10.1016/j.spl.2003.08.018.

Examples

```
set.seed(123)
x = matrix(rnorm(100), ncol = 2)
y = x[, 1] + x[, 2] + rlaplace(50, 0, 5)
# Fits a linear regression L1 model
mod1 = regL1(y ~ x)
FD(mod1)
```

Fire

Fire Data

Description

A dataset containing incidence of fire data for 47 residential areas in Chicago for the year 1975.

Usage

data(Fire)

Format

A data frame with 47 rows and 6 variables.

Details

- Fire: fires per 1000 housing units
- log_Fire: log of variable Fire
- Theft: thefts per 1000 residents
- Age: percent of housing units built in or before 1940
- Income: median family income as a multiple of \$1000

References

Birkes, D.and Dodge, Y. (1993). Alternative Methods of Regression. Jonh Wiley & Sons.

Description

This function applies the forward search approach to robust analysis in linear L1 models. This function is based on function fwdlm of package 'forward'.

Usage

```
forwardSearch_regL1(
  formula,
  data,
  nsamp = "best",
  intercept = TRUE,
  trace = TRUE,
  subset,
  weights,
  na.action,
  method = "br",
  model = TRUE,
  contrasts = NULL,
  ...
)
```

Arguments

formula	a formula object, with the response on the left of a \sim operator, and the terms, separated by + operators, on the right.
data	a data.frame in which to interpret the variables named in the formula, or in the subset and the weights argument. If this is missing, then the variables in the formula should be on the search list. This may also be a single number to handle some special cases – see below for details.
nsamp	the initial subset for the forward search in linear regression is found by fitting the regression model with the R function lmsreg. This argument allows to control how many subsets are used in the Least Median of Squares regression. The choices are: the number of samples or "best" (the default) or "exact" or "sample". For details see lmsreg.
intercept	logical for the inclusion of the intercept (if no formula is provided).
trace	logical, if TRUE a message is printed for every ten iterations completed during the forward search.
subset	an optional vector specifying a subset of observations to be used in the fitting process.

weights	vector of observation weights; if supplied, the algorithm fits to minimize the sum of the weights multiplied into the absolute residuals. The length of weights must be the same as the number of observations. The weights must be nonnegative and it is strongly recommended that they be strictly positive, since zero weights are ambiguous.
na.action	a function to filter missing data. This is applied to the model.frame after any subset argument has been used. The default (with na.fail) is to create an error if any missing values are found. A possible alternative is na.omit, which deletes observations that contain one or more missing values.
method	the algorithmic method used to compute the fit. There are several options: "br", "fn", "pfn", "sfn", "fnc", "conquer", "pfnb", "qfnb", "ppro" and "lasso". See rq for more details.
model	if TRUE then the model frame is returned. This is essential if one wants to call summary subsequently.
contrasts	a list giving contrasts for some or all of the factors default = NULL appearing in the model formula. The elements of the list should have the same name as the variable and should be either a contrast matrix (specifically, any full-rank matrix with as many rows as there are levels in the factor), or else a function to compute such a matrix given the number of levels.
	additional arguments for the fitting routines (see rq.fit.br and rq.fit.fnb, etc. and the functions they call).

A fitted forward search in linear L1 regression model object.

References

Atkinson, A.C. and Riani, M. (2000). Robust Diagnostic Regression Analysis. New York: Springer.

Examples

applies the forward search approach to robust analysis in a linear L1 model mod = forwardSearch_regL1(Concentration ~ Age, data = bile)

HV_test

Homogeneity of Variance Tests for Linear L1 Models

Description

Homogeneity of Variance Tests for Linear L1 Models

Usage

HV_test(y, x, groups, alpha = 0.05, tolerance = 0.001, max_iteration = 2000)

HV_test

Arguments

У	A vector with response variables.
х	A matrix with a single explanatory variable.
groups	Vector containing the group index to which the observation belongs.
alpha	Significance level of the test, must be between 0 and 1.
tolerance	threshold that determines when the iterative algorithm should stop (for $regL1_het$).
<pre>max_iteration</pre>	maximum number of iterations (for regL1_het).

Details

The 3 statistics to test homogeneity of variance are discussed in Rodrigues (2024), for more details see this reference. In practice, use the HV_LRT statistic results. If possible, use the HV_LRT statistic with a critical value obtained via bootstrap simulation.

Value

A list with results from 3 homogeneity of variance tests

alpha	alpha argument.
asymptotic_crit	ical_value
	asymptotic alpha-based test critical value.
HV_LRT	LF1 statistic value using MLE (Maximum Likelihood Estimator).
HV_max_lambda_r	ratio
	p-value of LF1 statistic using MLE.
HV_max_log_lamb	da_ratio
	LF1 statistic value using ROS (Residuals Order Statistics).
number_of_group	S
	number of groups.
N	overall sample size.
lambda_heterosc	redastic
	heteroscedastic estimation of the scaling parameters.
lambda_homoceda	stic
	homoscedastic estimation of the scale parameter.

References

Rodrigues, K. A. S. (2024). Analysis of the adjustment of the L1 regression model. Phd dissertation, University of São Paulo, BR.

```
set.seed(123)
x1 = matrix(rnorm(20), ncol = 1)
y1 = x1 + rlaplace(20, 0, 1)
x2 = matrix(rnorm(20), ncol = 1)
```

```
y2 = x2 + rlaplace(20, 0, 1.5)
x3 = matrix(rnorm(20), ncol = 1)
y3 = x3 + rlaplace(20, 0, 2)
x4 = matrix(rnorm(20), ncol = 1)
y4 = x4 + rlaplace(20, 0, 2.5)
x5 = matrix(rnorm(20), ncol = 1)
y5 = x5 + rlaplace(20, 0, 3)
y = c(y1, y2, y3, y4, y5)
x = rbind(x1, x2, x3, x4, x5)
group_index = c(rep(1,20),rep(2,20),rep(3,20),rep(4,20),rep(5,20))
# Application of the homogeneity of variance test
test_result = HV_test(y, x, group_index)
test_result
```

lambda_mle

Function to estimate lambda via MLE

Description

Function to estimate lambda via MLE

Usage

lambda_mle(model)

Arguments

model

A linear model L1 fitted with the rq function from the quantreg package.

Value

lambda MLE (Maximum Likelihood Estimator) estimator.

Examples

```
data(stackloss)
model_L1 = regL1(stack.loss ~ stack.x)
lambda_mle(model_L1)
```

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lambda_ros

Description

Function to compute a robust lambda estimator, which is based on the residuals order statistics.

Usage

lambda_ros(model)

Arguments

model

A linear model L1 fitted with the rq function from the quantreg package.

Value

Robust lambda estimator, which is based on the residuals order statistics.

Examples

```
data(stackloss)
model_L1 = regL1(stack.loss ~ stack.x)
lambda_ros(model_L1)
```

laplace.dist.test Wrapper for the 'laplace.test' function from the 'lawstat' package

Description

This function is a wrapper for the 'laplace.test' function from the 'lawstat' package. The advantage of using this function instead of the 'laplace.test' function of the 'lawstat' package is that this function shows the tables with the critical values of the statistics provided by Puig and Stephens (2000). This makes interpretation of the results easier.

Usage

laplace.dist.test(y, print_tables = TRUE)

Arguments

У	A numeric vector containing the sample data.
print_tables	A boolean variable that indicates whether tables with critical values will be printed or not.

The result of the laplace.test function.

References

Puig, P. and Stephens, M. A. (2000). Tests of fit for the Laplace distribution, with applications. *Technometrics*, **42**(4), 417-424. doi:10.2307/1270952.

See Also

laplace.test Goodness-of-fit Test Statistics for the Laplace Distribution from package lawstat.

Examples

```
normal_sample = rnorm(100, 0, 10)
laplace_sample = rlaplace(100, 0, 10)
laplace.dist.test(normal_sample)
laplace.dist.test(laplace_sample)
```

LF_test

Lack of Fit Tests for Linear L1 Models

Description

Lack of Fit Tests for Linear L1 Models

Usage

 $LF_test(y, x, groups, alpha = 0.05)$

Arguments

У	A vector with response variables.
x	A matrix with a single explanatory variable.
groups	Vector containing the group index to which the observation belongs.
alpha	Significance level of the test, must be between 0 and 1.

Details

The 3 statistics to test lack of fit are discussed in Rodrigues (2024), for more details see this reference. In practice, use the LF1_MLE statistic results. These tests were developed with just one explanatory variable in mind, which is why we include an error if there is more than one explanatory variable.

LF_test

Value

A list with results from 3 lack of fit tests

alpha	alpha argument.
critical_value	alpha-based test critical value.
LF1_MLE	LF1 statistic value using MLE (Maximum Likelihood Estimator).
LF1_MLE	p-value of LF1 statistic using MLE.
LF1_ROS	LF1 statistic value using ROS (Residuals Order Statistics).
LF2	LF2 statistic value.
modelo_H0	model fitted under H0.
modelo_Ha	model fitted under Ha.
MLE	estimation of the scale parameter of the estimator model via MLE.
ROS	estimation of the scale parameter of the estimator model via ROS.
SAE_H0	SAE (Sum of Absolute Errors) of the adjusted model under H0.
SAE_Ha	SAE (Sum of Absolute Errors) of the adjusted model under Ha.
<pre>matrix_mean_x</pre>	average of the explanatory variable per group of observations.
number_of_groups	
	number of groups.

References

Rodrigues, K. A. S. (2024). Analysis of the adjustment of the L1 regression model. Phd dissertation, University of São Paulo, BR.

```
set.seed(123)
x1 = matrix(rnorm(20), ncol = 1)
y1 = x1 + rlaplace(20, 0, 5)
x^2 = matrix(rnorm(20), ncol = 1)
y_2 = x_2 + rlaplace(20, 1, 5)
x3 = matrix(rnorm(20), ncol = 1)
y_3 = x_3 + rlaplace(20, 2, 5)
x4 = matrix(rnorm(20), ncol = 1)
y4 = x4 + rlaplace(20, 3, 5)
x5 = matrix(rnorm(20), ncol = 1)
y5 = x5 + rlaplace(20, 4, 5)
y = c(y1, y2, y3, y4, y5)
x = rbind(x1, x2, x3, x4, x5)
group_index = c(rep(1,20),rep(2,20),rep(3,20),rep(4,20),rep(5,20))
# Application of the lack of fit test
test_result = LF_test(y, x, group_index)
test_result
```

likelihoodCD

Description

Calculate Conditional Likelihood Displacement

Usage

likelihoodCD(model)

Arguments

model

Object returned from regL1 representing the fit of the L1 model.

Value

Likelihood Displacement

A vector with Likelihood Displacement for each observation.

References

.

Elian, S. N., André, C. D. S. and Narula, S. C. (2000). Influence Measure for the *L*1 regression. *Communications in Statistics - Theory and Methods*, **29**(4), 837-849. doi:10.1080/03610920008832518.

Examples

```
set.seed(123)
x = matrix(rnorm(100), ncol = 2)
y = x[, 1] + x[, 2] + rlaplace(50, 0, 5)
# Fits a linear regression L1 model
mod1 = regL1(y ~ x)
likelihoodCD(mod1)
```

likelihoodD Calculate Likelihood Displacement

Description

Calculate Likelihood Displacement

Usage

likelihoodD(model)

Arguments

model

Object returned from regL1 representing the fit of the L1 model.

Value

Likelihood Displacement A vector with Likelihood Displacement for each observation.

References

Elian, S. N., André, C. D. S. and Narula, S. C. (2000). Influence Measure for the *L*1 regression. *Communications in Statistics - Theory and Methods*, **29**(4), 837-849. doi:10.1080/03610920008832518.

Examples

```
set.seed(123)
x = matrix(rnorm(100), ncol = 2)
y = x[, 1] + x[, 2] + rlaplace(50, 0, 5)
```

```
# Fits a linear regression L1 model
mod1 = regL1(y ~ x)
likelihoodD(mod1)
```

PIF

Predictive Influence Function

Description

Predictive Influence Function

Usage

PIF(y, x, w, num_cores = 2)

Arguments

У	A vector with response variables.
х	A matrix with a single explanatory variable.
W	Explanatory variables vector for z, usually explanatory variables averages.
num_cores	Number of cores you want to use for parallel processing (default = 2).

Details

Please, install and load the "foreach" package to use this function. For more details see Rodrigues (2024).

A vector with predictive influence function value for each observation.

References

Rodrigues, K. A. S. (2024). Analysis of the adjustment of the L1 regression model. Phd dissertation, University of São Paulo, BR.

plaplace

Cumulative distribution function (CDF) of the Laplace distribution

Description

Cumulative distribution function (CDF) of the Laplace distribution

Usage

plaplace(q, location = 0, scale = 1)

Arguments

q	Values for which to calculate the cumulative distribution.
location	Location parameter of the Laplace distribution (default = 0).
scale	Scale parameter of the Laplace distribution (default = 1).

Value

Vector of calculated cumulative distributions.

Examples

plaplace(0, 0, 1)

plot.forwardSearch_regL1

Forward Search in Linear L1 Models

Description

This function plots the results of a forward search in linear L1 models.

Usage

```
## S3 method for class 'forwardSearch_regL1'
plot(
    x,
    type.plot = 1:5,
    squared = FALSE,
    scaled = FALSE,
    ylim = NULL,
    xlim = NULL,
    th.Res = 2,
    th.Lev = 0.25,
    sig.Tst = 2.58,
    labels.in.plot = TRUE,
    ...
)
```

Arguments

x	a "forwardSearch_regL1" object.
type.plot	select which plots to draw, by default all. Each graph is addressed by an integer:
	1. scaled residuals
	2. minimum deletion residuals
	3. coefficients
	4. statistics
	5. MAE (Mean Absolute Error) values
squared	logical, if TRUE plots squared residuals.
scaled	logical, if TRUE plots scaled coefficient estimates.
ylim	a two component vector for the min and max of the y axis.
xlim	a two component vector for the min and max of the x axis.
th.Res	numerical, a threshold for labelling the residuals.
th.Lev	numerical, a threshold for labelling the leverages.
sig.Tst	numerical, a value (on the scale of the t statistics) used to draw the confidence interval on the plot of the t statistics.
labels.in.plot	logical, if TRUE units are labelled in the plots when required.
	additional arguments.

Value

No return value, just plots the results of a forward search in linear L1 models.

See Also

forwardSearch_regL1 for apply forward search in linear L1 regression model.

Examples

```
# applies the forward search approach to robust analysis in a linear L1 model
mod = forwardSearch_regL1(Concentration ~ Age, data = bile)
plot(mod, 1)
```

Description

Print an object generated by forwardSearch_regL1

Usage

```
## S3 method for class 'forwardSearch_regL1'
print(x, ...)
```

Arguments

х	Object returned from forwardSearch_regL1.
	Optional arguments.

Value

No return value, called for side effects.

See Also

forwardSearch_regL1 for apply forward search in linear L1 regression model.

Examples

```
# applies the forward search approach to robust analysis in a linear L1 model
mod = forwardSearch_regL1(Concentration ~ Age, data = bile)
mod # or print(mod)
```

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print.regL1

Description

Print an object generated by regL1

Usage

S3 method for class 'regL1'
print(x, ...)

Arguments

х	Object returned from regL1 representing the fit of the L1 model.
	Optional arguments.

Value

No return value, called for side effects.

See Also

regL1 for fitting linear L1 models.

print.summary.forwardSearch_regL1 Print Forward Search in Linear L1 Model Summary Object

Description

Print summary of forward search in linear L1 model object.

Usage

```
## S3 method for class 'summary.forwardSearch_regL1'
print(x, digits = 4, ...)
```

Arguments

Х	This is an object of class "summary" produced by a call to summary.regL1().
digits	Significant digits reported in the printed table.
	Optional arguments.

No return value, called for side effects.

See Also

forwardSearch_regL1 for apply forward search in linear L1 regression model.

Examples

```
# applies the forward search approach to robust analysis in a linear L1 model
mod = forwardSearch_regL1(Concentration ~ Age, data = bile)
summary(mod)
```

print.summary.regL1 Print Linear L1 Regression Summary Object

Description

Print summary of linear L1 regression object.

Usage

```
## S3 method for class 'summary.regL1'
print(x, digits = max(5, .Options$digits - 2), ...)
```

Arguments

х	This is an object of class "summary.regL1" produced by a call to summary.regL1().
digits	Significant digits reported in the printed table.
	Optional arguments.

Value

No return value, called for side effects.

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qlaplace

Description

Quantile function (inverse of the CDF) of the Laplace distribution

Usage

qlaplace(p, location = 0, scale = 1)

Arguments

р	Values for which to calculate quantiles.
location	Location parameter of the Laplace distribution (default = 0).
scale	Scale parameter of the Laplace distribution (default = 1).

Value

Vector of calculated quantiles.

Examples

qlaplace(0.5, 0, 1)

regL1

Fitting Linear L1 Models

Description

This function fits an L1 regression model using the rq function from the 'quantreg' package. L1 regression allows dealing with outliers and non-normal distributions in the data.

Usage

```
regL1(
   formula,
   data,
   subset,
   weights,
   na.action,
   method = "br",
   model = TRUE,
   contrasts = NULL,
   ...
)
```

Arguments

formula	a formula object, with the response on the left of a \sim operator, and the terms, separated by + operators, on the right.
data	a data.frame in which to interpret the variables named in the formula, or in the subset and the weights argument. If this is missing, then the variables in the formula should be on the search list. This may also be a single number to handle some special cases – see below for details.
subset	an optional vector specifying a subset of observations to be used in the fitting process.
weights	vector of observation weights; if supplied, the algorithm fits to minimize the sum of the weights multiplied into the absolute residuals. The length of weights must be the same as the number of observations. The weights must be nonnegative and it is strongly recommended that they be strictly positive, since zero weights are ambiguous.
na.action	a function to filter missing data. This is applied to the model.frame after any subset argument has been used. The default (with na.fail) is to create an error if any missing values are found. A possible alternative is na.omit, which deletes observations that contain one or more missing values.
method	the algorithmic method used to compute the fit. There are several options: "br", "fn", "pfn", "sfn", "fnc", "conquer", "pfnb", "qfnb", "ppro" and "lasso". See rq for more details.
model	if TRUE then the model frame is returned. This is essential if one wants to call summary subsequently.
contrasts	a list giving contrasts for some or all of the factors default = NULL appearing in the model formula. The elements of the list should have the same name as the variable and should be either a contrast matrix (specifically, any full-rank matrix with as many rows as there are levels in the factor), or else a function to compute such a matrix given the number of levels.
	additional arguments for the fitting routines (see rq.fit.br and rq.fit.fnb, etc. and the functions they call).

Details

L1 regression is an important particular case of quantile regression, so this function inherits from the "rq" class of the quantreg package.

Value

A fitted L1 linear regression model object.

```
set.seed(123)
x = matrix(rnorm(100), ncol = 2)
y = x[, 1] + x[, 2] + rlaplace(50, 0, 5)
# Fits a linear regression L1 model
```

regL1_het

 $mod1 = regL1(y \sim x)$

regL1_het

Fitting Heteroscedastic Linear L1 Models

Description

This function fits an groupwise heteroscedastic L1 regression model using the rq function from the 'quantreg' package.

Usage

```
regL1_het(
    x,
    y,
    groups,
    na.action = stats::na.omit,
    method = "br",
    model = TRUE,
    tolerance = 0.001,
    max_iteration = 2000,
    ...
)
```

Arguments

х	the regression design matrix.
У	the regression response vector.
groups	vector with the group index associated with the observation, observations with the same index belong to the same group.
na.action	a function to filter missing data. This is applied to the model.frame after any subset argument has been used. The default (with na.fail) is to create an error if any missing values are found. A possible alternative is na.omit, which deletes observations that contain one or more missing values.
method	the algorithmic method used to compute the fit. There are several options: "br", "fn", "pfn", "sfn", "fnc", "conquer", "pfnb", "qfnb", "ppro" and "lasso". See rq for more details.
model	if TRUE then the model frame is returned. This is essential if one wants to call summary subsequently.
tolerance	threshold that determines when the iterative algorithm should stop.
<pre>max_iteration</pre>	maximum number of iterations.
	additional arguments for the fitting routines (see rq.fit.br and rq.fit.fnb, etc. and the functions they call).

Details

L1 regression is an important particular case of quantile regression, so this function inherits from the "rq" class of the quantreg package.

Value

A fitted heteroscedastic L1 linear regression model object.

Examples

```
set.seed(123)
x1 = matrix(rnorm(20), ncol = 2)
y1 = x1[, 1] + x1[, 2] + rlaplace(10, 0, 5)
x2 = matrix(rnorm(20), ncol = 2)
y_2 = x_2[, 1] + x_2[, 2] + rlaplace(10, 0, 10)
x3 = matrix(rnorm(20), ncol = 2)
y3 = x3[, 1] + x3[, 2] + rlaplace(10, 0, 15)
x4 = matrix(rnorm(20), ncol = 2)
y4 = x4[, 1] + x4[, 2] + rlaplace(10, 0, 20)
x5 = matrix(rnorm(20), ncol = 2)
y5 = x5[, 1] + x5[, 2] + rlaplace(10, 0, 30)
y = c(y1, y2, y3, y4, y5)
x = rbind(x1, x2, x3, x4, x5)
group_index = c(rep(1,10),rep(2,10),rep(3,10),rep(4,10),rep(5,10))
# Fits a heteroscedastic linear regression L1 model
mod1 = regL1_het(x, y, group_index)
```

rlaplace

Function to generate random values from the Laplace distribution

Description

Function to generate random values from the Laplace distribution

Usage

```
rlaplace(n, location = 0, scale = 1)
```

Arguments

n	Number of values to generate.
location	Location parameter of the Laplace distribution (default = 0).
scale	Scale parameter of the Laplace distribution (default = 1).

Value

Vector of generated random values.

SAE

Examples

rlaplace(10, 0, 1)

SAE

Function to calculate SAE

Description

Function to calculate SAE (Sum of Absolute Errors) of the adjusted model.

Usage

SAE(model)

Arguments

model A linear model L1 fitted with the rq function from the quantreg package.

Value

SAE (Sum of Absolute Errors).

Examples

data(stackloss)
model_L1 = regL1(stack.loss ~ stack.x)
SAE(model_L1)

summary.forwardSearch_regL1 Summarizing Fit of Forward Search in Linear L1 Regression

Description

Returns a summary list for a forward search in linear L1 regression fit.

Usage

```
## S3 method for class 'forwardSearch_regL1'
summary(object, steps = "auto", ...)
```

Arguments

object	Object returned from forwardSearch_regL1.
steps	the number of forward steps to show.
	Optional arguments.

No return value, called for side effects.

References

Atkinson, A.C. and Riani, M. (2000). Robust Diagnostic Regression Analysis. New York: Springer.

See Also

forwardSearch_regL1 for apply forward search in linear L1 regression model.

Examples

```
# applies the forward search approach to robust analysis in a linear L1 model
mod = forwardSearch_regL1(Concentration ~ Age, data = bile)
summary(mod)
```

summary.regL1 Summary methods for L1 Regression

Description

Returns a summary list for a L1 regression fit. A null value will be returned if printing is invoked.

Usage

```
## S3 method for class 'regL1'
summary(
   object,
   se = NULL,
   covariance = FALSE,
   hs = TRUE,
   U = NULL,
   gamma = 0.7,
   ...
)
```

Arguments

objectObject returned from regL1 representing the fit of the L1 model.sespecifies the method used to compute standard standard errors. There are currently seven available methods: "rank", "iid", "nid", "ker", "boot", "BLB", "conquer" and "extreme".

summary.regL1

covariance	logical flag to indicate whether the full covariance matrix of the estimated parameters should be returned.
hs	Use Hall Sheather bandwidth for sparsity estimation If false revert to Bofinger bandwidth.
U	Resampling indices or gradient evaluations used for bootstrap, see summary.rq and boot.rq for more details.
gamma	parameter controlling the effective sample size of the 'bag of little bootstrap samples that will be $b = n^{2}$ gamma where n is the sample size of the original model.
	Optional arguments. See summary.rq for more details.

Value

No return value, called for side effects.

See Also

regL1 for fitting linear L1 models. summary.rq summary methods for Quantile Regression.

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