Package 'bgms'

October 4, 2025

```
Type Package
Title Bayesian Analysis of Networks of Binary and/or Ordinal Variables
Version 0.1.6.1
Date 2025-10-03
Maintainer Maarten Marsman <m.marsman@uva.nl>
Description Bayesian variable selection methods for analyzing the structure of a Markov ran-
     dom field model for a network of binary and/or ordinal variables.
Copyright Includes datasets 'ADHD' and 'Boredom', which are licensed
     under CC-BY 4. See individual data documentation for license
     and citation.
License GPL (>= 2)
URL https://Bayesian-Graphical-Modelling-Lab.github.io/bgms/
BugReports https://github.com/Bayesian-Graphical-Modelling-Lab/bgms/issues
Imports Rcpp (>= 1.0.7), RcppParallel, Rdpack, methods, coda,
     lifecycle
RdMacros Rdpack
LinkingTo Rcpp, RcppArmadillo, RcppParallel, dqrng, BH
RoxygenNote 7.3.3
Depends R (>= 3.5)
LazyData true
Encoding UTF-8
Suggests ggplot2, knitr, parallel, qgraph, rmarkdown, testthat (>=
     3.0.0)
VignetteBuilder knitr
Config/testthat/edition 3
Config/Needs/website tidyverse/tidytemplate
NeedsCompilation yes
```

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```
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Repository CRAN

Date/Publication 2025-10-04 09:20:02 UTC

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ADHD

ADHD Symptom Checklist for Children Aged 6-8 Years

Description

This dataset includes ADHD symptom ratings for 355 children aged 6 to 8 years from the Children's Attention Project (CAP) cohort (Silk et al. 2019). The sample consists of 146 children diagnosed with ADHD and 209 without a diagnosis. Symptoms were assessed through structured interviews with parents using the NIMH Diagnostic Interview Schedule for Children IV (DISC-IV) (Shaffer et al. 2000). The checklist includes 18 items: 9 Inattentive (I) and 9 Hyperactive/Impulsive (HI). Each item is binary (1 = present, 0 = absent).

Usage

```
data("ADHD")
```

ADHD 3

Format

A matrix with 355 rows and 19 columns.

group ADHD diagnosis: 1 = diagnosed, 0 = not diagnosed

avoid Often avoids, dislikes, or is reluctant to engage in tasks that require sustained mental effort (I)

closeatt Often fails to give close attention to details or makes careless mistakes in schoolwork, work, or other activities (I)

distract Is often easily distracted by extraneous stimuli (I)

forget Is often forgetful in daily activities (I)

instruct Often does not follow through on instructions and fails to finish schoolwork, chores, or duties in the workplace (I)

listen Often does not seem to listen when spoken to directly (I)

loses Often loses things necessary for tasks or activities (I)

org Often has difficulty organizing tasks and activities (I)

susatt Often has difficulty sustaining attention in tasks or play activities (I)

blurts Often blurts out answers before questions have been completed (HI)

fidget Often fidgets with hands or feet or squirms in seat (HI)

interrupt Often interrupts or intrudes on others (HI)

motor Is often "on the go" or often acts as if "driven by a motor" (HI)

quiet Often has difficulty playing or engaging in leisure activities quietly (HI)

runs Often runs about or climbs excessively in situations in which it is inappropriate (HI)

seat Often leaves seat in classroom or in other situations in which remaining seated is expected (HI)

talks Often talks excessively (HI)

turn Often has difficulty awaiting turn (HI)

Source

Silk et al. (2019). Data retrieved from doi:10.1371/journal.pone.0211053.s004. Licensed under the CC-BY 4.0: https://creativecommons.org/licenses/by/4.0/

References

Shaffer D, Fisher P, Lucas CP, Dulcan MK, Schwab-Stone ME (2000). "NIMH Diagnostic Interview Schedule for Children Version IV (NIMH DISC-IV): description, differences from previous versions, and reliability of some common diagnoses." *Journal of the American Academy of Child & Adolescent Psychiatry*, **39**, 28–38. doi:10.1097/0000458320000100000014, PMID: 10638065.

Silk TJ, Malpas CB, Beare R, Efron D, Anderson V, Hazell P, Jongeling B, Nicholson JM, Sciberras E (2019). "A network analysis approach to ADHD symptoms: More than the sum of its parts." *PLOS ONE*, **14**(1), e0211053. doi:10.1371/journal.pone.0211053.

bgm

Bayesian Estimation or Edge Selection for Markov Random Fields

Description

The bgm function estimates the pseudoposterior distribution of category thresholds (main effects) and pairwise interaction parameters of a Markov Random Field (MRF) model for binary and/or ordinal variables. Optionally, it performs Bayesian edge selection using spike-and-slab priors to infer the network structure.

Usage

```
bgm(
  variable_type = "ordinal",
 baseline_category,
  iter = 1000,
 warmup = 1000,
  pairwise_scale = 2.5,
 main_alpha = 0.5,
 main_beta = 0.5,
  edge_selection = TRUE,
  edge_prior = c("Bernoulli", "Beta-Bernoulli", "Stochastic-Block"),
  inclusion_probability = 0.5,
  beta_bernoulli_alpha = 1,
  beta_bernoulli_beta = 1,
  dirichlet_alpha = 1,
  lambda = 1,
  na_action = c("listwise", "impute"),
  update_method = c("nuts", "adaptive-metropolis", "hamiltonian-mc"),
  target_accept,
  hmc_num_leapfrogs = 100,
  nuts_max_depth = 10,
  learn_mass_matrix = FALSE,
  chains = 4,
  cores = parallel::detectCores(),
  display_progress = c("per-chain", "total", "none"),
  seed = NULL,
  interaction_scale,
  burnin,
  save,
  threshold_alpha,
  threshold_beta
)
```

Arguments

Х

A data frame or matrix with n rows and p columns containing binary and ordinal responses. Variables are automatically recoded to non-negative integers (0, 1, ..., m). For regular ordinal variables, unobserved categories are collapsed; for Blume-Capel variables, all categories are retained.

variable_type

Character or character vector. Specifies the type of each variable in x. Allowed values: "ordinal" or "blume-capel". Binary variables are automatically treated as "ordinal". Default: "ordinal".

baseline_category

Integer or vector. Baseline category used in Blume-Capel variables. Can be a single integer (applied to all) or a vector of length p. Required if at least one variable is of type "blume-capel".

iter

Integer. Number of post-burn-in iterations (per chain). Default: 1e3.

warmup

Integer. Number of warmup iterations before collecting samples. A minimum of 1000 iterations is enforced, with a warning if a smaller value is requested. Default: 1e3.

pairwise_scale Double. Scale of the Cauchy prior for pairwise interaction parameters. Default: 2.5.

main_alpha, main_beta

Double. Shape parameters of the beta-prime prior for threshold parameters. Must be positive. If equal, the prior is symmetric. Defaults: main_alpha = 0.5 and main_beta = 0.5.

edge_selection Logical. Whether to perform Bayesian edge selection. If FALSE, the model estimates all edges. Default: TRUE.

edge_prior

Character. Specifies the prior for edge inclusion. Options: "Bernoulli", "Beta-Bernoulli", or "Stochastic-Block". Default: "Bernoulli".

inclusion_probability

Numeric scalar. Prior inclusion probability of each edge (used with the Bernoulli prior). Default: 0.5.

beta_bernoulli_alpha, beta_bernoulli_beta

Double. Shape parameters for the beta distribution in the Beta–Bernoulli and the Stochastic-Block priors. Must be positive. Defaults: beta_bernoulli_alpha = 1 and beta_bernoulli_beta = 1.

dirichlet_alpha

Double. Concentration parameter of the Dirichlet prior on block assignments (used with the Stochastic Block model). Default: 1.

lambda

Double. Rate of the zero-truncated Poisson prior on the number of clusters in the Stochastic Block Model. Default: 1.

na_action

Character. Specifies missing data handling. Either "listwise" (drop rows with missing values) or "impute" (perform single imputation during sampling). Default: "listwise".

update_method

Character. Specifies how the MCMC sampler updates the model parameters:

"adaptive-metropolis" Componentwise adaptive Metropolis—Hastings with Robbins-Monro proposal adaptation.

"hamiltonian-mc" Hamiltonian Monte Carlo with fixed path length (number of leapfrog steps set by hmc_num_leapfrogs).

"nuts" The No-U-Turn Sampler, an adaptive form of HMC with dynamically chosen trajectory lengths.

Default: "nuts".

target_accept

Numeric between 0 and 1. Target acceptance rate for the sampler. Defaults are set automatically if not supplied: 0.44 for adaptive Metropolis, 0.65 for HMC, and 0.60 for NUTS.

hmc_num_leapfrogs

Integer. Number of leapfrog steps for Hamiltonian Monte Carlo. Must be positive. Default: 100.

 $nuts_max_depth \quad Integer. \ Maximum \ tree \ depth \ in \ NUTS. \ Must \ be \ positive. \ Default: \ 10.$

learn_mass_matrix

Logical. If TRUE, adapt a diagonal mass matrix during warmup (HMC/NUTS only). If FALSE, use the identity matrix. Default: FALSE.

chains Integer. Number of parallel chains to run. Default: 4.

cores Integer. Number of CPU cores for parallel execution. Default: parallel::detectCores().

display_progress

Logical. Whether to show a progress bar during sampling. Default: TRUE.

seed Optional integer. Random seed for reproducibility. Must be a single non-

negative integer.

interaction_scale, burnin, save, threshold_alpha, threshold_beta

'r lifecycle::badge("deprecated")' Deprecated arguments as of **bgms 0.1.6.0**. Use 'pairwise_scale', 'warmup', 'main_alpha', and 'main_beta' instead.

Details

This function models the joint distribution of binary and ordinal variables using a Markov Random Field, with support for edge selection through Bayesian variable selection. The statistical foundation of the model is described in Marsman et al. (2025), where the ordinal MRF model and its Bayesian estimation procedure were first introduced. While the implementation in **bgms** has since been extended and updated (e.g., alternative priors, parallel chains, HMC/NUTS warmup), it builds on that original framework.

Key components of the model are described in the sections below.

Value

A list of class "bgms" with posterior summaries, posterior mean matrices, and access to raw MCMC draws. The object can be passed to print(), summary(), and coef().

Main components include:

- posterior_summary_main: Data frame with posterior summaries (mean, sd, MCSE, ESS, Rhat) for category threshold parameters.
- posterior_summary_pairwise: Data frame with posterior summaries for pairwise interaction parameters.

• posterior_summary_indicator: Data frame with posterior summaries for edge inclusion indicators (if edge_selection = TRUE).

- posterior_mean_main: Matrix of posterior mean thresholds (rows = variables, cols = categories or parameters).
- posterior_mean_pairwise: Symmetric matrix of posterior mean pairwise interaction strengths.
- posterior_mean_indicator: Symmetric matrix of posterior mean inclusion probabilities (if edge selection was enabled).
- Additional summaries returned when edge_prior = "Stochastic-Block". For more details about this prior see Sekulovski et al. (2025).
 - posterior_summary_pairwise_allocations: Data frame with posterior summaries (mean, sd, MCSE, ESS, Rhat) for the pairwise cluster co-occurrence of the nodes. This serves to indicate whether the estimated posterior allocations,co-clustering matrix and posterior cluster probabilities (see blow) have converged.
 - posterior_coclustering_matrix: a symmetric matrix of pairwise proportions of occurrence of every variable. This matrix can be plotted to visually inspect the estimated number of clusters and visually inspect nodes that tend to switch clusters.
 - posterior_mean_allocations: A vector with the posterior mean of the cluster allocations of the nodes. This is calculated using the method proposed in Dahl (2009).
 - posterior_mode_allocations: A vector with the posterior mode of the cluster allocations of the nodes.
 - posterior_num_blocks: A data frame with the estimated posterior inclusion probabilities for all the possible number of clusters.
- raw_samples: A list of raw MCMC draws per chain:

main List of main effect samples.

pairwise List of pairwise effect samples.

indicator List of indicator samples (if edge selection enabled).

allocations List of cluster allocations (if SBM prior used).

nchains Number of chains.

niter Number of post-warmup iterations per chain.

parameter_names Named lists of parameter labels.

• arguments: A list of function call arguments and metadata (e.g., number of variables, warmup, sampler settings, package version).

The summary() method prints formatted posterior summaries, and coef() extracts posterior mean matrices.

NUTS diagnostics (tree depth, divergences, energy, E-BFMI) are included in fit*nuts_diag if update_method = "nuts".

Ordinal Variables

The function supports two types of ordinal variables:

Regular ordinal variables: Assigns a category threshold parameter to each response category except the lowest. The model imposes no additional constraints on the distribution of category responses.

Blume-Capel ordinal variables: Assume a baseline category (e.g., a "neutral" response) and score responses by distance from this baseline. Category thresholds are modeled as:

$$\mu_c = \alpha \cdot c + \beta \cdot (c - b)^2$$

where:

- μ_c : category threshold for category c
- α : linear trend across categories
- β : preference toward or away from the baseline
 - If β < 0, the model favors responses near the baseline category;
 - if $\beta > 0$, it favors responses farther away (i.e., extremes).
- b: baseline category

Edge Selection

When edge_selection = TRUE, the function performs Bayesian variable selection on the pairwise interactions (edges) in the MRF using spike-and-slab priors.

Supported priors for edge inclusion:

- Bernoulli: Fixed inclusion probability across edges.
- Beta-Bernoulli: Inclusion probability is assigned a Beta prior distribution.
- Stochastic-Block: Cluster-based edge priors with Beta, Dirichlet, and Poisson hyperpriors.

All priors operate via binary indicator variables controlling the inclusion or exclusion of each edge in the MRF.

Prior Distributions

- Pairwise effects: Modeled with a Cauchy (slab) prior.
- Main effects: Modeled using a beta-prime distribution.
- Edge indicators: Use either a Bernoulli, Beta-Bernoulli, or Stochastic-Block prior (as above).

Sampling Algorithms and Warmup

Parameters are updated within a Gibbs framework, but the conditional updates can be carried out using different algorithms:

- Adaptive Metropolis—Hastings: Componentwise random—walk updates for main effects and pairwise effects. Proposal standard deviations are adapted during burn—in via Robbins—Monro updates toward a target acceptance rate.
- Hamiltonian Monte Carlo (HMC): Joint updates of all parameters using fixed—length leapfrog trajectories. Step size is tuned during warmup via dual—averaging; the diagonal mass matrix can also be adapted if learn_mass_matrix = TRUE.
- No-U-Turn Sampler (NUTS): An adaptive extension of HMC that dynamically chooses trajectory lengths. Warmup uses a staged adaptation schedule (fast-slow-fast) to stabilize step size and, if enabled, the mass matrix.

When edge_selection = TRUE, updates of edge—inclusion indicators are carried out with Metropolis—Hastings steps. These are switched on after the core warmup phase, ensuring that graph updates occur only once the samplers' tuning parameters (step size, mass matrix, proposal SDs) have stabilized.

After warmup, adaptation is disabled. Step size and mass matrix are fixed at their learned values, and proposal SDs remain constant.

Warmup and Adaptation

The warmup procedure in bgm is based on the multi-stage adaptation schedule used in Stan (Stan Development Team 2023). Warmup iterations are split into several phases:

- Stage 1 (fast adaptation): A short initial interval where only step size (for HMC/NUTS) is adapted, allowing the chain to move quickly toward the typical set.
- Stage 2 (slow windows): A sequence of expanding, memoryless windows where both step size and, if learn_mass_matrix = TRUE, the diagonal mass matrix are adapted. Each window ends with a reset of the dual—averaging scheme for improved stability.
- Stage 3a (final fast interval): A short interval at the end of the core warmup where the step size is adapted one final time.
- Stage 3b (proposal–SD tuning): Only active when edge_selection = TRUE under HMC/NUTS. In this phase, Robbins–Monro adaptation of proposal standard deviations is performed for the Metropolis steps used in edge–selection moves.
- Stage 3c (graph selection warmup): Also only relevant when edge_selection = TRUE. At the start of this phase, a random graph structure is initialized, and Metropolis–Hastings updates for edge inclusion indicators are switched on.

When edge_selection = FALSE, the total number of warmup iterations equals the user—specified burnin. When edge_selection = TRUE and update_method is "nuts" or "hamiltonian-mc", the schedule automatically appends additional Stage-3b and Stage-3c intervals, so the total warmup is strictly greater than the requested burnin.

After all warmup phases, the sampler transitions to the sampling phase with adaptation disabled. Step size and mass matrix (for HMC/NUTS) are fixed at their learned values, and proposal SDs remain constant.

This staged design improves stability of proposals and ensures that both local parameters (step size) and global parameters (mass matrix, proposal SDs) are tuned before collecting posterior samples.

For adaptive Metropolis–Hastings runs, step size and mass matrix adaptation are not relevant. Proposal SDs are tuned continuously during burn–in using Robbins–Monro updates, without staged fast/slow intervals.

Missing Data

If na_action = "listwise", observations with missing values are removed. If na_action = "impute", missing values are imputed during Gibbs sampling.

References

Dahl DB (2009). "Modal clustering in a class of product partition models." *Bayesian Analysis*, **4**(2), 243–264. doi:10.1214/09BA409.

Marsman M, van den Bergh D, Haslbeck JMB (2025). "Bayesian analysis of the ordinal Markov random field." *Psychometrika*, **90**, 146—182.

Sekulovski N, Arena G, Haslbeck JMB, Huth KBS, Friel N, Marsman M (2025). "A Stochastic Block Prior for Clustering in Graphical Models." *Retrieved from* https://osf.io/preprints/psyarxiv/29p3m_v1. OSF preprint.

Stan Development Team (2023). *Stan Modeling Language Users Guide and Reference Manual*. Version 2.33, https://mc-stan.org/docs/.

See Also

```
vignette("intro", package = "bgms") for a worked example.
```

Examples

```
# Run bgm on subset of the Wenchuan dataset
fit = bgm(x = Wenchuan[, 1:5])
# Posterior inclusion probabilities
summary(fit)$indicator
# Posterior pairwise effects
summary(fit)$pairwise
```

 ${\tt bgmCompare}$

Bayesian Estimation and Variable Selection for Group Differences in Markov Random Fields

Description

The bgmCompare function estimates group differences in category threshold parameters (main effects) and pairwise interactions (pairwise effects) of a Markov Random Field (MRF) for binary and ordinal variables. Groups can be defined either by supplying two separate datasets (x and y) or by a group membership vector. Optionally, Bayesian variable selection can be applied to identify differences across groups.

Usage

```
bgmCompare(
   x,
   y,
```

```
group_indicator,
  difference_selection = TRUE,
  variable_type = "ordinal",
  baseline_category,
  difference_scale = 1,
  difference_prior = c("Bernoulli", "Beta-Bernoulli"),
  difference_probability = 0.5,
  beta_bernoulli_alpha = 1,
  beta_bernoulli_beta = 1,
  pairwise_scale = 2.5,
 main_alpha = 0.5,
 main_beta = 0.5,
  iter = 1000,
 warmup = 1000,
  na_action = c("listwise", "impute"),
  update_method = c("nuts", "adaptive-metropolis", "hamiltonian-mc"),
  target_accept,
  hmc_num_leapfrogs = 100,
  nuts_max_depth = 10,
  learn_mass_matrix = FALSE,
  chains = 4,
  cores = parallel::detectCores(),
  display_progress = c("per-chain", "total", "none"),
  seed = NULL,
 main_difference_model,
  reference_category,
 main_difference_scale,
  pairwise_difference_scale,
  pairwise_difference_prior,
 main_difference_prior,
  pairwise_difference_probability,
 main_difference_probability,
  pairwise_beta_bernoulli_alpha,
  pairwise_beta_bernoulli_beta,
 main_beta_bernoulli_alpha,
 main_beta_bernoulli_beta,
  interaction_scale,
  threshold_alpha,
  threshold_beta,
 burnin,
  save
)
```

Arguments

Х

A data frame or matrix of binary and ordinal responses for Group 1. Variables should be coded as nonnegative integers starting at 0. For ordinal variables, unused categories are collapsed; for Blume–Capel variables, all categories are retained.

y Optional data frame or matrix for Group 2 (two-group designs). Must have the same variables (columns) as x.

group_indicator

Optional integer vector of group memberships for rows of x (multi-group designs). Ignored if y is supplied.

difference_selection

Logical. If TRUE, spike-and-slab priors are applied to difference parameters. Default: TRUE.

variable_type Character vector specifying type of each variable: "ordinal" (default) or "blume-capel". baseline_category

Integer or vector giving the baseline category for Blume-Capel variables.

difference_scale

Double. Scale of the Cauchy prior for difference parameters. Default: 1.

difference_prior

Character. Prior for difference inclusion: "Bernoulli" or "Beta-Bernoulli". Default: "Bernoulli".

difference_probability

Numeric. Prior inclusion probability for differences (Bernoulli prior). Default: 0.5.

beta_bernoulli_alpha, beta_bernoulli_beta

Doubles. Shape parameters of the Beta prior for inclusion probabilities in the Beta–Bernoulli model. Defaults: 1.

pairwise_scale Double. Scale of the Cauchy prior for baseline pairwise interactions. Default: 2.5.

main_alpha, main_beta

Doubles. Shape parameters of the beta-prime prior for baseline threshold parameters. Defaults: 0.5.

iter Integer. Number of post–warmup iterations per chain. Default: 1e3.
warmup Integer. Number of warmup iterations before sampling. Default: 1e3.

na_action Character. How to handle missing data: "listwise" (drop rows) or "impute" (impute within Gibbs). Default: "listwise".

update_method Character. Sampling algorithm: "adaptive-metropolis", "hamiltonian-mc",

target_accept Numeric between 0 and 1. Target acceptance rate. Defaults: 0.44 (Metropolis), 0.65 (HMC), 0.60 (NUTS).

hmc_num_leapfrogs

Integer. Leapfrog steps for HMC. Default: 100.

nuts_max_depth Integer. Maximum tree depth for NUTS. Default: 10.

or "nuts". Default: "nuts".

learn_mass_matrix

Logical. If TRUE, adapt the mass matrix during warmup (HMC/NUTS only). Default: FALSE.

chains Integer. Number of parallel chains. Default: 4.

cores Integer. Number of CPU cores. Default: parallel::detectCores().

```
display_progress
```

Character. Controls progress reporting: "per-chain", "total", or "none". Default: "per-chain".

seed

Optional integer. Random seed for reproducibility.

'r lifecycle::badge("deprecated")' Deprecated arguments as of **bgms 0.1.6.0**. Use 'difference_scale', 'difference_prior', 'difference_probability', 'beta_bernoulli_alpha', 'beta_bernoulli_beta', 'baseline_category', 'pairwise_scale', and 'warmup' instead.

Details

This function extends the ordinal MRF framework Marsman et al. (2025) to multiple groups. The basic idea of modeling, analyzing, and testing group differences in MRFs was introduced in Marsman et al. (2024), where two–group comparisons were conducted using adaptive Metropolis sampling. The present implementation generalizes that approach to more than two groups and supports additional samplers (HMC and NUTS) with staged warmup adaptation.

Key components of the model:

Value

A list of class "bgmCompare" containing posterior summaries, posterior mean matrices, and raw MCMC samples:

- posterior_summary_main_baseline, posterior_summary_pairwise_baseline: summaries of baseline thresholds and pairwise interactions.
- posterior_summary_main_differences, posterior_summary_pairwise_differences: summaries of group differences in thresholds and pairwise interactions.
- posterior_summary_indicator: summaries of inclusion indicators (if difference_selection = TRUE).
- posterior_mean_main_baseline, posterior_mean_pairwise_baseline: posterior mean matrices (legacy style).
- raw_samples: list of raw draws per chain for main, pairwise, and indicator parameters.
- arguments: list of function call arguments and metadata.

The summary() method prints formatted summaries, and coef() extracts posterior means.

NUTS diagnostics (tree depth, divergences, energy, E-BFMI) are included in fit*nuts_diag if update_method = "nuts".

Pairwise Interactions

For variables i and j, the group-specific interaction is represented as:

$$\theta_{ij}^{(g)} = \phi_{ij} + \delta_{ij}^{(g)},$$

where ϕ_{ij} is the baseline effect and $\delta_{ij}^{(g)}$ are group differences constrained to sum to zero.

Ordinal Variables

Regular ordinal variables: category thresholds are decomposed into a baseline plus group differences for each category.

Blume–Capel variables: category thresholds are quadratic in the category index, with both the linear and quadratic terms split into a baseline plus group differences.

Variable Selection

When difference_selection = TRUE, spike-and-slab priors are applied to difference parameters:

- · Bernoulli: fixed prior inclusion probability.
- Beta-Bernoulli: inclusion probability given a Beta prior.

Sampling Algorithms and Warmup

Parameters are updated within a Gibbs framework, using the same sampling algorithms and staged warmup scheme described in bgm:

- Adaptive Metropolis—Hastings: componentwise random—walk proposals with Robbins—Monro adaptation of proposal SDs.
- **Hamiltonian Monte Carlo (HMC)**: joint updates with fixed leapfrog trajectories; step size and optionally the mass matrix are adapted during warmup.
- **No–U–Turn Sampler (NUTS)**: an adaptive HMC variant with dynamic trajectory lengths; warmup uses the same staged adaptation schedule as HMC.

For details on the staged adaptation schedule (fast–slow–fast phases), see bgm. In addition, when difference_selection = TRUE, updates of inclusion indicators are delayed until late warmup. In HMC/NUTS, this appends two extra phases (Stage-3b and Stage-3c), so that the total number of warmup iterations exceeds the user-specified warmup.

After warmup, adaptation is disabled: step size and mass matrix are fixed at their learned values, and proposal SDs remain constant.

References

Marsman M, Waldorp LJ, Sekulovski N, Haslbeck JMB (2024). "Bayes factor tests for group differences in ordinal and binary graphical models." *Retrieved from https://osf.io/preprints/osf/f4pk9*. OSF preprint.

Marsman M, van den Bergh D, Haslbeck JMB (2025). "Bayesian analysis of the ordinal Markov random field." *Psychometrika*, **90**, 146—182.

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See Also

```
vignette("comparison", package = "bgms") for a worked example.
```

Examples

```
## Not run:
# Run bgmCompare on subset of the Boredom dataset
x = Boredom[Boredom$language == "fr", 2:6]
y = Boredom[Boredom$language != "fr", 2:6]

fit <- bgmCompare(x, y)

# Posterior inclusion probabilities
summary(fit)$indicator

# Bayesian model averaged main effects for the groups
coef(fit)$main_effects_groups

# Bayesian model averaged pairwise effects for the groups
coef(fit)$pairwise_effects_groups

## End(Not run)</pre>
```

Boredom

Short Boredom Proneness Scale Responses

Description

This dataset includes responses to the 8-item Short Boredom Proneness Scale (SBPS), a self-report measure of an individual's susceptibility to boredom (Martarelli et al. 2023). Items were rated on a 7-point Likert scale ranging from 1 ("strongly disagree") to 7 ("strongly agree"). The scale was administered in either English (Struk et al. 2015) or French (translated by (Martarelli et al. 2023)).

Usage

```
data("Boredom")
```

Format

A matrix with 986 rows and 9 columns. Each row corresponds to a respondent.

language Language in which the SBPS was administered: "en" = English, "fr" = French

loose_ends I often find myself at "loose ends," not knowing what to do.

entertain I find it hard to entertain myself.

repetitive Many things I have to do are repetitive and monotonous.

stimulation It takes more stimulation to get me going than most people.

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motivated I don't feel motivated by most things that I do.

keep_interest In most situations, it is hard for me to find something to do or see to keep me interested.

sit_around Much of the time, I just sit around doing nothing.

half_dead_dull Unless I am doing something exciting, even dangerous, I feel half-dead and dull.

Source

Martarelli et al. (2023). Data retrieved from https://osf.io/qhux8. Licensed under the CC-BY 4.0: https://creativecommons.org/licenses/by/4.0/

References

Martarelli CS, Baillifard A, Audrin C (2023). "A Trait-Based Network Perspective on the Validation of the French Short Boredom Proneness Scale." *European Journal of Psychological Assessment*, **39**(6), 390–399. doi:10.1027/10155759/a000718.

Struk AA, Carriere JSA, Cheyne JA, Danckert J (2015). "A Short Boredom Proneness Scale: Development and Psychometric Properties." *Assessment*, **24**(3), 346–359. doi:10.1177/1073191115609996.

coef.bgmCompare

Extract Coefficients from a bgmCompare Object

Description

Returns posterior means for raw parameters (baseline + differences) and group-specific effects from a bgmCompare fit, as well as inclusion indicators.

Usage

```
## S3 method for class 'bgmCompare'
coef(object, ...)
```

Arguments

object An object of class bgmCompare.
... Ignored.

Value

A list with components:

main_effects_raw Posterior means of the raw main-effect parameters (variables x [baseline + differences]).

pairwise_effects_raw Posterior means of the raw pairwise-effect parameters (pairs x [baseline +
differences]).

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main_effects_groups Posterior means of group-specific main effects (variables x groups), computed as baseline plus projected differences.

pairwise_effects_groups Posterior means of group-specific pairwise effects (pairs x groups), computed as baseline plus projected differences.

indicators Posterior mean inclusion probabilities as a symmetric matrix, with diagonals corresponding to main effects and off-diagonals to pairwise effects.

coef.bgms

Extract Coefficients from a bgms Object

Description

Returns the posterior mean thresholds, pairwise effects, and edge inclusion indicators from a bgms model fit.

Usage

```
## S3 method for class 'bgms'
coef(object, ...)
```

Arguments

object An object of class bgms.
... Ignored.

Value

A list with the following components:

main Posterior mean of the category threshold parameters.

pairwise Posterior mean of the pairwise interaction matrix.

indicator Posterior mean of the edge inclusion indicators (if available).

mrfSampler

Sample observations from the ordinal MRF

Description

This function samples states from the ordinal MRF using a Gibbs sampler. The Gibbs sampler is initiated with random values from the response options, after which it proceeds by simulating states for each variable from a logistic model using the other variable states as predictor variables.

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Usage

```
mrfSampler(
  no_states,
  no_variables,
  no_categories,
  interactions,
  thresholds,
  variable_type = "ordinal",
  reference_category,
  iter = 1000
)
```

Arguments

no_states The number of states of the ordinal MRF to be generated.

no_variables The number of variables in the ordinal MRF.

no_categories Either a positive integer or a vector of positive integers of length no_variables.

The number of response categories on top of the base category: no_categories

= 1 generates binary states.

interactions A symmetric no_variables by no_variables matrix of pairwise interactions.

Only its off-diagonal elements are used.

thresholds A no_variables by max(no_categories) matrix of category thresholds. The

elements in row i indicate the thresholds of variable i. If no_categories is a vector, only the first no_categories[i] elements are used in row i. If the Blume-Capel model is used for the category thresholds for variable i, then row i requires two values (details below); the first is α , the linear contribution of the

Blume-Capel model and the second is β , the quadratic contribution.

variable_type What kind of variables are simulated? Can be a single character string specify-

ing the variable type of all p variables at once or a vector of character strings of length p specifying the type for each variable separately. Currently, bgm supports "ordinal" and "blume-capel". Binary variables are automatically treated

as "ordinal". Defaults to variable_type = "ordinal".

reference_category

An integer vector of length no_variables specifying the reference_category category that is used for the Blume-Capel model (details below). Can be any

integer value between 0 and no_categories (or no_categories[i]).

iter The number of iterations used by the Gibbs sampler. The function provides the

last state of the Gibbs sampler as output. By default set to 1e3.

Details

There are two modeling options for the category thresholds. The default option assumes that the category thresholds are free, except that the first threshold is set to zero for identification. The user then only needs to specify the thresholds for the remaining response categories. This option is useful for any type of ordinal variable and gives the user the most freedom in specifying their model.

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The Blume-Capel option is specifically designed for ordinal variables that have a special type of reference_category category, such as the neutral category in a Likert scale. The Blume-Capel model specifies the following quadratic model for the threshold parameters:

$$\mu_{\rm c} = \alpha \times {\rm c} + \beta \times ({\rm c} - {\rm r})^2$$

where μ_c is the threshold for category c (which now includes zero), α offers a linear trend across categories (increasing threshold values if $\alpha > 0$ and decreasing threshold values if $\alpha < 0$), if $\beta < 0$, it offers an increasing penalty for responding in a category further away from the reference_category category r, while $\beta > 0$ suggests a preference for responding in the reference_category category.

Value

A no_states by no_variables matrix of simulated states of the ordinal MRF.

Examples

```
# Generate responses from a network of five binary and ordinal variables.
no_variables = 5
no_categories = sample(1:5, size = no_variables, replace = TRUE)
Interactions = matrix(0, nrow = no_variables, ncol = no_variables)
Interactions[2, 1] = Interactions[4, 1] = Interactions[3, 2] =
  Interactions[5, 2] = Interactions[5, 4] = .25
Interactions = Interactions + t(Interactions)
Thresholds = matrix(0, nrow = no_variables, ncol = max(no_categories))
x = mrfSampler(no_states = 1e3,
               no variables = no variables.
               no_categories = no_categories,
               interactions = Interactions,
               thresholds = Thresholds)
# Generate responses from a network of 2 ordinal and 3 Blume-Capel variables.
no_variables = 5
no_categories = 4
Interactions = matrix(0, nrow = no_variables, ncol = no_variables)
Interactions[2, 1] = Interactions[4, 1] = Interactions[3, 2] =
  Interactions[5, 2] = Interactions[5, 4] = .25
Interactions = Interactions + t(Interactions)
Thresholds = matrix(NA, no_variables, no_categories)
Thresholds[, 1] = -1
Thresholds[, 2] = -1
Thresholds[3, ] = sort(-abs(rnorm(4)), decreasing = TRUE)
Thresholds[5, ] = sort(-abs(rnorm(4)), decreasing = TRUE)
x = mrfSampler(no_states = 1e3,
               no_variables = no_variables,
               no_categories = no_categories,
               interactions = Interactions,
```

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```
thresholds = Thresholds,
variable_type = c("b","b","o","o","b","o"),
reference_category = 2)
```

print.bgmCompare

Print method for 'bgmCompare' objects

Description

Minimal console output for 'bgmCompare' fit objects.

Usage

```
## S3 method for class 'bgmCompare' print(x, ...)
```

Arguments

x An object of class 'bgmCompare'.

... Ignored.

print.bgms

Print method for 'bgms' objects

Description

Minimal console output for 'bgms' fit objects.

Usage

```
## S3 method for class 'bgms'
print(x, ...)
```

Arguments

x An object of class 'bgms'.

... Ignored.

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summary.bgmCompare

Summary method for 'bgmCompare' objects

Description

Returns posterior summaries and diagnostics for a fitted 'bgmCompare' model.

Usage

```
## S3 method for class 'bgmCompare'
summary(object, ...)
```

Arguments

object An object of class 'bgmCompare'.
... Currently ignored.

Value

An object of class 'summary.bgmCompare' with posterior summaries.

summary.bgms

Summary method for 'bgms' objects

Description

Returns posterior summaries and diagnostics for a fitted 'bgms' model.

Usage

```
## S3 method for class 'bgms'
summary(object, ...)
```

Arguments

```
object An object of class 'bgms'.
... Currently ignored.
```

Value

An object of class 'summary.bgms' with posterior summaries.

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Wenchuan

PTSD Symptoms in Wenchuan Earthquake Survivors Who Lost a Child

Description

This dataset contains responses to 17 items assessing symptoms of post-traumatic stress disorder (PTSD) in Chinese adults who survived the 2008 Wenchuan earthquake and lost at least one child in the disaster (McNally et al. 2015). Participants completed the civilian version of the Posttraumatic Checklist, with each item corresponding to a DSM-IV PTSD symptom. Items were rated on a 5-point Likert scale from "not at all" to "extremely," indicating the degree to which the symptom bothered the respondent in the past month.

Usage

```
data("Wenchuan")
```

Format

A matrix with 362 rows and 17 columns. Each row represents a participant.

intrusion Repeated, disturbing memories, thoughts, or images of a stressful experience from the past?

dreams Repeated, disturbing dreams of a stressful experience from the past?

flash Suddenly acting or feeling as if a stressful experience were happening again (as if you were reliving it)?

upset Feeling very upset when something reminded you of a stressful experience from the past?

physior Having physical reactions (e.g., heart pounding, trouble breathing, sweating) when something reminded you of a stressful experience from the past?

avoidth Avoiding thinking about or talking about a stressful experience from the past or avoiding having feelings related to it?

avoidact Avoiding activities or situations because they reminded you of a stressful experience from the past?

amnesia Trouble remembering important parts of a stressful experience from the past?

lossint Loss of interest in activities that you used to enjoy?

distant Feeling distant or cut off from other people?

numb Feeling emotionally numb or being unable to have loving feelings for those close to you?

future Feeling as if your future will somehow be cut short?

sleep Trouble falling or staying asleep?

anger Feeling irritable or having angry outbursts?

concen Having difficulty concentrating?

hyper Being "super-alert" or watchful or on guard?

startle Feeling jumpy or easily startled?

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Source

https://psychosystems.org/wp-content/uploads/2014/10/Wenchuan.csv

References

McNally RJ, Robinaugh DJ, Wu GWY, Wang L, Deserno MK, Borsboom D (2015). "Mental disorders as causal systems: A network approach to posttraumatic stress disorder." *Clinical Psychological Science*, **6**, 836–849. doi:10.1177/2167702614553230.

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