Package 'RCAL'

January 20, 2025

Title Regularized Calibrated Estimation

Version 2.0

Author Zhiqiang Tan, Baoluo Sun

Maintainer Zhiqiang Tan <ztan@stat.rutgers.edu>

URL http://www.stat.rutgers.edu/~ztan

Description

Regularized calibrated estimation for causal inference and missing-data problems with highdimensional data, based on Tan (2020a) <doi:10.1093/biomet/asz059>, Tan (2020b) <doi:10.1214/19-AOS1824> and Sun and Tan (2020) <arXiv:2009.09286>.

Depends R (>= 3.5.0), trust

License GPL (>= 2)

Encoding UTF-8

LazyData true

RoxygenNote 7.1.1

NeedsCompilation no

Repository CRAN

Date/Publication 2020-11-05 14:40:02 UTC

Contents

CAL-package
e.aipw
e.ipw
e.nreg
e.regu.cv
e.regu.path
m.nreg
m.regu
m.regu.cv
m.regu.path
te.aipw

late.nreg	19
late.regu.cv	21
late.regu.path	23
mn.aipw	25
mn.ipw	
mn.nreg	
mn.regu.cv	
mn.regu.path	
simu.data	
simu.iv.data	34
	37

Index

RCAL-package RCAL: Regularized calibrated estimation

Description

Regularized calibrated estimation for causal inference and missing-data problems with high-dimensional data.

Details

The R package RCAL - version 2.0 can be used for two main tasks:

- to estimate the mean of an outcome in the presence of missing data,
- to estimate the average treatment effects (ATE) and local average treatment effects (LATE) in causal inference.

There are 3 high-level functions provided for the first task:

- mn.nreg: inference using non-regularized calibrated estimation,
- mn.regu.cv: inference using regularized calibrated estimation based on cross validation,
- mn.regu.path: inference using regularized calibrated estimation along a regularization path.

The first function mn.nreg is appropriate only in relatively low-dimensional settings, whereas the functions mn.regu.cv and mn.regu.path are designed to deal with high-dimensional data (namely, the number of covariates close to or greater than the sample size). In parallel, there are 3 functions for estimating the average treatment effect in the second task, ate.nreg, ate.regu.cv, and ate.regu.path. These functions can also be used to perform inference for the average treatment effects on the treated or on the untreated. Currently, the treatment is assumed to be binary (i.e., untreated or treated). There are also 3 functions for estimating the local average treatment effect using instrumental variables, late.nreg, late.regu.cv, and late.regu.path. Currently both the treatment and instrumental variable are assumed to be binary. Extensions to multi-valued treatments and instrumental variables will be incorporated in later versions.

The package also provides lower-level functions, including glm.nreg to implement non-regularized M-estimation and glm.regu to implement Lasso regularized M-estimation for fitting generalized linear models currently with continuous or binary outcomes. The latter function glm.regu uses an

ate.aipw

active-set descent algorithm, which enjoys a finite termination property for solving least-squares Lasso problems.

See the the vignettes for more details.

ate.aipw

Augmented inverse probability weighted estimation of population means

Description

This function implements augmented inverse probability weighted (IPW) estimation of average treatment effects (ATEs), provided both fitted propensity scores and fitted values from outcome regression.

Usage

ate.aipw(y, tr, mfp, mfo, off = NULL)

Arguments

У	An $n \ge 1$ vector of observed outcomes.
tr	An $n \ge 1$ vector of treatment indicators (=1 if treated or 0 if untreated).
mfp	An $n \ge 2$ matrix of fitted propensity scores for untreated (first column) and treated (second column).
mfo	An $n \ge 2$ matrix of fitted values from outcome regression, for untreated (first column) and treated (second column).
off	A 2 x 1 vector of offset values (e.g., the true values in simulations) used to calculate the z-statistics.

Value

one	A 2 x 1 vector of direct IPW estimates of 1.
ipw	A 2 x 1 vector of ratio IPW estimates of means.
or	A 2 x 1 vector of outcome regression estimates of means.
est	A 2 x 1 vector of augmented IPW estimates of means.
var	The estimated variances associated with the augmented IPW estimates of means.
ze	The z-statistics for the augmented IPW estimates of means, compared to off.
diff	The augmented IPW estimate of ATE.
diff.var	The estimated variance associated with the augmented IPW estimate of ATE.
diff.ze	The z-statistic for the augmented IPW estimate of ATE.

References

Tan, Z. (2020a) Regularized calibrated estimation of propensity scores with model misspecification and high-dimensional data, *Biometrika*, 107, 137–158.

Tan, Z. (2020b) Model-assisted inference for treatment effects using regularized calibrated estimation with high-dimensional data, *Annals of Statistics*, 48, 811–837.

ate.ipw

Inverse probability weighted estimation of average treatment effects

Description

This function implements inverse probability weighted (IPW) estimation of average treatment effects (ATEs), provided fitted propensity scores.

Usage

ate.ipw(y, tr, mfp)

Arguments

У	An $n \ge 1$ vector of observed outcomes.
tr	An $n \ge 1$ vector of treatment indicators (=1 if treated or 0 if untreated).
mfp	An $n \ge 2$ matrix of fitted propensity scores for untreated (first column) and treated (second column).

Value

one	The direct IPW estimates of 1.
est	The ratio IPW estimates of means
diff	The ratio IPW estimate of ATE.

References

Tan, Z. (2020a) Regularized calibrated estimation of propensity scores with model misspecification and high-dimensional data, *Biometrika*, 107, 137–158.

Tan, Z. (2020b) Model-assisted inference for treatment effects using regularized calibrated estimation with high-dimensional data, *Annals of Statistics*, 48, 811–837. ate.nreg

Description

This function implements model-assisted inference for average treatment effects, using non-regularized calibrated estimation.

Usage

```
ate.nreg(y, tr, x, ploss = "cal", yloss = "gaus", off = NULL)
```

Arguments

У	An $n \ge 1$ vector of observed outcomes.
tr	An $n \ge 1$ vector of treatment indicators (=1 if treated or 0 if untreated).
x	An $n \ge p$ matix of covariates, used in both propensity score and outcome regression models.
ploss	A loss function used in propensity score estimation (either "ml" or "cal").
yloss	A loss function used in outcome regression (either "gaus" for continuous out- comes or "ml" for binary outcomes).
off	A 2 x 1 vector of offset values (e.g., the true values in simulations) used to calculate the z-statistics from augmented IPW estimation.

Details

For calibrated estimation, two sets of propensity scores are separately estimated for the untreated and treated as discussed in Tan (2020a, 2020b). See also **Details** for mn.nreg.

Value

ps	A list containing the results from fitting the propensity score model by glm.nreg.
mfp	An $n \ge 2$ matrix of fitted propensity scores for untreated (first column) and treated (second column).
or	A list containing the results from fitting the outcome regression model by glm.nreg.
mfo	An $n \ge 2$ matrix of fitted values from outcome regression, for untreated (first column) and treated (second column).
est	A list containing the results from augmented IPW estimation by ate.aipw.

References

Tan, Z. (2020a) Regularized calibrated estimation of propensity scores with model misspecification and high-dimensional data, *Biometrika*, 107, 137–158.

Tan, Z. (2020b) Model-assisted inference for treatment effects using regularized calibrated estimation with high-dimensional data, *Annals of Statistics*, 48, 811–837.

Examples

```
data(simu.data)
n <- dim(simu.data)[1]
p <- dim(simu.data)[2]-2

y <- simu.data[,1]
tr <- simu.data[,2]
x <- simu.data[,2+1:p]
x <- scale(x)

# include only 10 covariates
x2 <- x[,1:10]
ate.cal <- ate.nreg(y, tr, x2, ploss="cal", yloss="gaus")
matrix(unlist(ate.cal$est), ncol=2, byrow=TRUE,
dimnames=list(c("one", "ipw", "or", "est", "var", "ze",
 "diff.est", "diff.var", "diff.ze"), c("untreated", "treated")))</pre>
```

ate.regu.cv	Model-assisted inference for average treatment effects based on cross
	validation

Description

This function implements model-assisted inference for average treatment effects, using regularized calibrated estimation based on cross validation.

Usage

```
ate.regu.cv(fold, nrho = NULL, rho.seq = NULL, y, tr, x, ploss = "cal",
yloss = "gaus", off = NULL, ...)
```

Arguments

fold	A vector of length 2 giving the fold numbers for cross validation in propensity score estimation and outcome regression respectively.
nrho	A vector of length 2 giving the numbers of tuning parameters searched in cross validation.
rho.seq	A list of two vectors giving the tuning parameters in propensity score estimation (first vector) and outcome regression (second vector).
У	An $n \ge 1$ vector of observed outcomes.
tr	An $n \ge 1$ vector of treatment indicators (=1 if treated or 0 if untreated).
x	An $n \ge p$ matix of covariates, used in both propensity score and outcome regression models.
ploss	A loss function used in propensity score estimation (either "ml" or "cal").

6

ate.regu.cv

yloss	A loss function used in outcome regression (either "gaus" for continuous outcomes or "ml" for binary outcomes).
off	A 2 x 1 vector of offset values (e.g., the true values in simulations) used to calculate the z-statistics from augmented IPW estimation.
	Additional arguments to glm. regu. cv.

Details

For calibrated estimation, two sets of propensity scores are separately estimated for the untreated and treated as discussed in Tan (2020a, 2020b). See also **Details** for mn.regu.cv.

Value

ps	A list containing the results from fitting the propensity score model by glm.regu.cv.
mfp	An $n \ge 2$ matrix of fitted propensity scores for untreated (first column) and treated (second column).
or	A list containing the results from fitting the outcome regression model by $glm.regu.cv$.
mfo	An $n \ge 2$ matrix of fitted values from outcome regression, for untreated (first column) and treated (second column).
est	A list containing the results from augmented IPW estimation by ate.aipw.

References

Tan, Z. (2020a) Regularized calibrated estimation of propensity scores with model misspecification and high-dimensional data, *Biometrika*, 107, 137–158.

Tan, Z. (2020b) Model-assisted inference for treatment effects using regularized calibrated estimation with high-dimensional data, *Annals of Statistics*, 48, 811–837.

Examples

ate.regu.path

Description

This function implements model-assisted inference for average treatment effects, using regularized calibrated estimation along regularization paths for propensity score (PS) estimation while based on cross validation for outcome regression (OR).

Usage

```
ate.regu.path(fold, nrho = NULL, rho.seq = NULL, y, tr, x, ploss = "cal",
yloss = "gaus", off = NULL, ...)
```

Arguments

fold	A vector of length 2, with the second component giving the fold number for cross validation in outcome regression. The first component is not used.
nrho	A vector of length 2 giving the number of tuning parameters in a regularization path for PS estimation and that in cross validation for OR.
rho.seq	A list of two vectors giving the tuning parameters for propensity score estimation (first vector) and outcome regression (second vector).
У	An $n \ge 1$ vector of observed outcomes.
tr	An $n \ge 1$ vector of treatment indicators (=1 if treated or 0 if untreated).
x	An $n \ge p$ matix of covariates, used in both propensity score and outcome regression models.
ploss	A loss function used in propensity score estimation (either "ml" or "cal").
yloss	A loss function used in outcome regression (either "gaus" for continuous outcomes or "ml" for binary outcomes).
off	A 2 x 1 vector of offset values (e.g., the true values in simulations) used to calculate the z-statistics from augmented IPW estimation.
	Additional arguments to glm.regu.cv and glm.regu.path.

Details

See **Details** for ate.regu.cv.

Value

ps	A list of 2 objects, giving the results from fitting the propensity score model by glm.regu.path for untreated (first) and treated (second).
mfp	A list of 2 matrices of fitted propensity scores, along the PS regularization path, for untreated (first matrix) and treated (second matrix).

glm.nreg

or	A list of 2 lists of objects for untreated (first) and treated (second), where each object gives the results from fitting the outcome regression model by glm.regu.cv for a PS tuning parameter.
mfo	A list of 2 matrices of fitted values from outcome regression based on cross val- idation, along the PS regularization path, for untreated (first matrix) and treated (second matrix).
est	A list containing the results from augmented IPW estimation by ate.aipw.
rho	A vector of tuning parameters leading to converged results in propensity score estimation.

References

Tan, Z. (2020a) Regularized calibrated estimation of propensity scores with model misspecification and high-dimensional data, *Biometrika*, 107, 137–158.

Tan, Z. (2020b) Model-assisted inference for treatment effects using regularized calibrated estimation with high-dimensional data, *Annals of Statistics*, 48, 811–837.

Examples

glm.nreg

Non-regularied M-estimation for fitting generalized linear models

Description

This function implements non-regularized M-estimation for fitting generalized linear models with continuous or binary responses, including maximum likelihood, calibrated estimation, and covariate-balancing estimation in the latter case of fitting propensity score models.

Usage

glm.nreg(y, x, iw = NULL, loss = "cal", init = NULL)

Arguments

У	An $n \ge 1$ response vector.
x	An $n \ge p$ matix of covariates, excluding a constant.
iw	An $n \ge 1$ weight vector.
loss	A loss function used, which can be specified as "gaus" for continuous responses, or "ml", "cal", or "bal" for binary responses.
init	A $(p + 1) \ge 1$ vector of initial values (the intercept and coefficients).

Details

Least squares estimation is implemented by calling 1m for continuous responses (loss="gaus"). For binary responses, maximum likelihood estimation (loss="ml") is implemented by calling g1m. Calibrated estimation (loss="cal") is implemented by using a trust-region algorithm in the R package **trust** to minimize the calibration loss, i.e., (6) in Tan (2020). Covariate-balancing estimation (loss="bal") in Imai and Ratkovic (2014) is implemented by using **trust** to minimize (36) in Tan (2020a).

Value

coef	The $(p+1) \ge 1$ vector of estimated intercept and coefficients.
fit	The $n \ge 1$ vector of fitted values.
conv	Logical; 1 if loss="gaus" for continuous responses or convergence is obtained within 1000 iterations by glm with loss="ml" or trust with loss="cal" or "bal" for binary responses.

References

Imai, K. and Ratkovic, M. (2014) Covariate balancing propensity score, *Journal of the Royal Statistical Society*, Ser. B, 76, 243-263.

Tan, Z. (2020) Regularized calibrated estimation of propensity scores with model misspecification and high-dimensional data, *Biometrika*, 107, 137–158.

Examples

```
data(simu.data)
n <- dim(simu.data)[1]
p <- dim(simu.data)[2]-2

y <- simu.data[,1]
tr <- simu.data[,2]
x <- simu.data[,2+1:p]
x <- scale(x)

# include only 10 covariates
x2 <- x[,1:10]
ps.ml <- glm.nreg(y=tr, x=x2, loss="ml")
check.ml <- mn.ipw(x2, tr, ps.ml$fit)</pre>
```

glm.regu

```
check.ml
ps.cal <- glm.nreg(y=tr, x=x2, loss="cal")
check.cal <- mn.ipw(x2, tr, ps.cal$fit)
check.cal # should be numerically 0
ps.bal <- glm.nreg(y=tr, x=x2, loss="bal")
check.bal <- mn.ipw(x2, tr, ps.bal$fit)
check.bal</pre>
```

glm.regu	Regularied M-estimation for fitting generalized linear models with a
	fixed tuning parameter

Description

This function implements regularized M-estimation for fitting generalized linear models with continuous or binary responses for a fixed choice of tuning parameters.

Usage

```
glm.regu(y, x, iw = NULL, loss = "cal", init = NULL, rhos, test = NULL,
offs = NULL, id = NULL, Wmat = NULL, Rmat = NULL, zzs = NULL,
xxs = NULL, n.iter = 100, eps = 1e-06, bt.lim = 3, nz.lab = NULL,
pos = 10000)
```

Arguments

у	An $n \ge 1$ response vector.
х	An $n \ge p$ matix of covariates, excluding a constant.
iw	An $n \ge 1$ weight vector.
loss	A loss function, which can be specified as "gaus" for continuous responses, or "ml" or "cal" for binary respones.
init	A $(p + 1)$ x 1 vector of initial values (the intercept and coefficients).
rhos	A $p \ge 1$ vector of Lasso tuning parameters, usually a constant vector, associated with the p coefficients.
test	A vector giving the indices of observations between 1 and n which are included in the test set.
offs	An $n \ge 1$ vector of offset values, similarly as in glm.
id	An argument which can be used to speed up computation.
Wmat	An argument which can be used to speed up computation.
Rmat	An argument which can be used to speed up computation.
zzs	An argument which can be used to speed up computation.

XXS	An argument which can be used to speed up computation.
n.iter	The maximum number of iterations allowed. An iteration is defined by comput- ing an quadratic approximation and solving a least-squares Lasso problem.
eps	The tolerance at which the difference in the objective (loss plus penalty) values is considered close enough to 0 to declare convergence.
bt.lim	The maximum number of backtracking steps allowed.
nz.lab	A $p \ge 1$ logical vector (useful for simulations), indicating which covariates are included when calculating the number of nonzero coefficients. If nz.lab=NULL, then nz.lab is reset to a vector of 0s.
pos	A value which can be used to facilitate recording the numbers of nonzero coefficients with or without the restriction by nz.lab. If nz.lab=NULL, then pos is reset to 1.

Details

For continuous responses, this function uses an active-set descent algorithm (Osborne et al. 2000; Yang and Tan 2018) to solve the least-squares Lasso problem. For binary responses, regularized calibrated estimation is implemented using the Fisher scoring descent algorithm in Tan (2020), whereas regularized maximum likelihood estimation is implemented in a similar manner based on quadratic approximation as in the R package **glmnet**.

Value

iter	The number of iterations performed up to n.iter.
conv	1 if convergence is obtained, 0 if exceeding the maximum number of iterations, or -1 if exceeding maximum number of backtracking steps.
nz	A value defined as $(nz0 * pos + nz1)$ to record the numbers of nonzero coefficients without or with the restriction (denoted as $nz0$ and $nz1$) by $nz.lab$. If $nz.lab=NULL$, then $nz1$ is 0, pos is 1, and hence nz is $nz0$.
inter	The estimated intercept.
bet	The $p \ge 1$ vector of estimated coefficients, excluding the intercept.
fit	The vector of fitted values in the training set.
eta	The vector of linear predictors in the training set.
tau	The $p \ge 1$ vector of generalized signs, which should be -1 or 1 for a negative or positive estimate and between -1 and 1 for a zero estimate.
obj.train	The average loss in the training set.
pen	The Lasso penalty of the estimates.
obj	The average loss plus the Lasso penalty.
fit.test	The vector of fitted values in the test set.
eta.test	The vector of linear predictors in the test set.
obj.test	The average loss in the test set.
id	This can be re-used to speed up computation.
Wmat	This can be re-used to speed up computation.

glm.regu

Rmat	This can be re-used to speed up computation.
ZZS	This can be re-used to speed up computation.
xxs	This can be re-used to speed up computation.

References

Osborne, M., Presnell, B., and Turlach, B. (2000) A new approach to variable selection in least squares problems, *IMA Journal of Numerical Analysis*, 20, 389-404.

Yang, T. and Tan, Z. (2018) Backfitting algorithms for total-variation and empirical-norm penalized additive modeling with high-dimensional data, *Stat*, 7, e198.

Tibshirani, R. (1996) Regression shrinkage and selection via the Lasso, *Journal of the Royal Statistical Society*, Ser. B, 58, 267-288.

Tan, Z. (2020) Regularized calibrated estimation of propensity scores with model misspecification and high-dimensional data, *Biometrika*, 107, 137–158.

Examples

```
data(simu.data)
n <- dim(simu.data)[1]</pre>
p <- dim(simu.data)[2]-2</pre>
y <- simu.data[,1]</pre>
tr <- simu.data[,2]</pre>
x <- simu.data[,2+1:p]</pre>
x \leftarrow scale(x)
### Example 1: linear regression
# rhos should be a vector of length p, even though a constant vector
out.rgaus <- glm.regu(y[tr==1], x[tr==1,], rhos=rep(.05,p), loss="gaus")</pre>
# the intercept
out.rgaus$inter
# the estimated coefficients and generalized signs; the first 10 are shown
cbind(out.rgaus$bet, out.rgaus$tau)[1:10,]
# the number of nonzero coefficients
out.rgaus$nz
### Example 2: logistic regression using likelihood loss
out.rml <- glm.regu(tr, x, rhos=rep(.01,p), loss="ml")</pre>
out.rml$inter
cbind(out.rml$bet, out.rml$tau)[1:10,]
out.rml$nz
### Example 3: logistic regression using calibration loss
out.rcal <- glm.regu(tr, x, rhos=rep(.05,p), loss="cal")</pre>
out.rcal$inter
cbind(out.rcal$bet, out.rcal$tau)[1:10,]
out.rcal$nz
```

glm.regu.cv

Description

This function implements regularized M-estimation for fitting generalized linear models with binary or contiunous responses based on cross validation.

Usage

```
glm.regu.cv(fold, nrho = NULL, rho.seq = NULL, y, x, iw = NULL,
loss = "cal", n.iter = 100, eps = 1e-06, tune.fac = 0.5,
tune.cut = TRUE, ann.init = TRUE, nz.lab = NULL, permut = NULL)
```

Arguments

fold	A fold number used for cross validation.
nrho	The number of tuning parameters searched in cross validation.
rho.seq	A vector of tuning parameters searched in cross validation. If both nrho and rho.seq are specified, then rho.seq overrides nrho.
У	An $n \ge 1$ response vector.
х	An $n \ge p$ matix of covariates, excluding a constant.
iw	An $n \ge 1$ weight vector.
loss	A loss function, which can be specified as "gaus" for continuous responses, or "ml" or "cal" for binary respones.
n.iter	The maximum number of iterations allowed as in glm.regu.
eps	The tolerance used to declare convergence as in glm.regu.
tune.fac	The multiplier (factor) used to define rho.seq if only nrho is specified.
tune.cut	Logical; if TRUE, all smaller tuning parameters are skipped once non-convergence is found with a tuning parameter.
ann.init	Logical; if TRUE, the estimates from the previous tuning parameter are used as the inital values when fitting with the current tuning parameter.
nz.lab	A $p \ge 1$ logical vector (useful for simulations), indicating which covariates are included when calculating the number of nonzero coefficients.
permut	An $n \ge 1$ vector, giving a random permutation of the integers from 1 to n , which is used in cross validation.

Details

Cross validation is performed as described in Tan (2020a, 2020b). If not specified by users, the sequence of tuning parameters searched is defined as a geometric series of length nrho, starting from the value which yields a zero solution, and then decreasing by a factor tune. fac successively.

After cross validation, two tuning parameters are selected. The first and default choice is the value yielding the smallest average test loss. The second choice is the largest value giving the average test loss within one standard error of the first choice (Hastie, Tibshirani, and Friedman 2016).

glm.regu.cv

Value

permut	An $n \ge 1$ vector, giving the random permutation used in cross validation.
rho	The vector of tuning parameters, searched in cross validation.
non.conv	A vector indicating the non-convergene status found or imputed if tune.cut=TRUE, for the tuning parameters in cross validation. For each tuning parameter, 0 indicates convergence, 1 non-convergence if exceeding n.iter, 2 non-convergence if exceeding bt.lim.
err.ave	A vector giving the averages of the test losses in cross validation.
err.sd	A vector giving the standard deviations of the test losses in cross validation.
sel.rho	A vector of two selected tuning parameters by cross validation; see Details.
sel.nz	A vector of numbers of nonzero coefficients estimated for the selected tuning parameters.
sel.bet	The $(p+1) \ge 2$ vector of estimated intercept and coefficients.
sel.fit	The $n \ge 2$ vector of fitted values.

References

Hastie, T., Tibshirani, R., and Friedman. J. (2016) *The Elements of Statistical Learning* (second edition), Springer: New York.

Tan, Z. (2020a) Regularized calibrated estimation of propensity scores with model misspecification and high-dimensional data, *Biometrika*, 107, 137–158.

Tan, Z. (2020b) Model-assisted inference for treatment effects using regularized calibrated estimation with high-dimensional data, *Annals of Statistics*, 48, 811–837.

Examples

```
data(simu.data)
n <- dim(simu.data)[1]</pre>
p <- dim(simu.data)[2]-2</pre>
y <- simu.data[,1]</pre>
tr <- simu.data[,2]</pre>
x <- simu.data[,2+1:p]</pre>
x < - scale(x)
### Example 1: Regularized maximum likelihood estimation of propensity scores
ps.cv.rml <- glm.regu.cv(fold=5, nrho=1+10, y=tr, x=x, loss="ml")</pre>
ps.cv.rml$rho
ps.cv.rml$err.ave
ps.cv.rml$err.sd
ps.cv.rml$sel.rho
ps.cv.rml$sel.nz
fp.cv.rml <- ps.cv.rml $sel.fit[,1]</pre>
check.cv.rml <- mn.ipw(x, tr, fp.cv.rml)</pre>
check.cv.rml$est
```

```
### Example 2: Regularized calibrated estimation of propensity scores
ps.cv.rcal <- glm.regu.cv(fold=5, nrho=1+10, y=tr, x=x, loss="cal")
ps.cv.rcal$rho
ps.cv.rcal$err.ave
ps.cv.rcal$sel.rho
ps.cv.rcal$sel.nz
fp.cv.rcal <- ps.cv.rcal $sel.fit[,1]
check.cv.rcal <- mn.ipw(x, tr, fp.cv.rcal)
check.cv.rcal$est</pre>
```

glm.regu.path	Regularied M-estimation for fitting generalized linear models along a
	regularization path

Description

This function implements regularized M-estimation for fitting generalized linear models with binary or contiunous responses along a regularization path.

Usage

```
glm.regu.path(nrho = NULL, rho.seq = NULL, y, x, iw = NULL,
loss = "cal", n.iter = 100, eps = 1e-06, tune.fac = 0.5,
tune.cut = TRUE, ann.init = TRUE, nz.lab = NULL)
```

Arguments

nrho	The number of tuning parameters in a regularization path.
rho.seq	A vector of tuning parameters in a regularization path. If both nrho and rho.seq are specified, then rho.seq overrides nrho.
У	An $n \ge 1$ response vector.
х	An $n \ge p$ matix of covariates, excluding a constant.
iw	An $n \ge 1$ weight vector.
loss	A loss function, which can be specified as "gaus" for continuous responses, or "ml" or "cal" for binary respones.
n.iter	The maximum number of iterations allowed as in glm.regu.
eps	The tolerance used to declare convergence as in glm.regu.
tune.fac	The multiplier (factor) used to define rho.seq if only nrho is specified.
tune.cut	Logical; if TRUE, all smaller tuning parameters are skipped once non-convergence is found with a tuning parameter.

16

glm.regu.path

ann.init	Logical; if TRUE, the estimates from the previous tuning parameter are used as the initial value when fitting with the current tuning parameter.
nz.lab	A $p \ge 1$ logical vector (useful for simulations), indicating which covariates are included when calculating the number of nonzero coefficients.

Details

If not specified by users, the sequence of tuning parameters (i.e., the regularization path) is defined as a geometric series of length nrho, starting from the value which yields a zero solution, and then decreasing by a factor tune.fac successively.

Value

rho	The vector of tuning parameters included in the regularization path.
non.conv	A vector indicating the non-convergene status found or imputed if tune.cut=TRUE, along the regularization path. For each tuning parameter, 0 indicates convergence, 1 non-convergence if exceeding n.iter, 2 non-convergence if exceeding bt.lim.
nz.all	A vector giving the numbers of nonzero coefficients estimated, along the regularization path.
bet.all	A matrix giving estimated intercept and coefficients, column by column, along the regularization path.
fit.all	A matrix giving fitted values, column by column, along the regularization path.

References

Tan, Z. (2020a) Regularized calibrated estimation of propensity scores with model misspecification and high-dimensional data, *Biometrika*, 107, 137–158.

Tan, Z. (2020b) Model-assisted inference for treatment effects using regularized calibrated estimation with high-dimensional data, *Annals of Statistics*, 48, 811–837.

Examples

```
### Example 2: logistic regression using likelihood loss
out.rml.path <- glm.regu.path(rho.seq=c(.002, .005, .01, .02, .05, .1), y=tr, x=x, loss="ml")
out.rml.path$bet.all[1:10,]
### Example 3: logistic regression using calibration loss
out.rcal.path <- glm.regu.path(rho.seq=c(.005, .01, .02, .05, .1, .2), y=tr, x=x, loss="cal")
out.rcal.path$bet.all[1:10,]
```

late.aipw

Augmented inverse probability weighted estimation of local average treatment effects

Description

This function implements augmented inverse probability weighted (IPW) estimation of local average treatment effects (LATEs) as proposed in Tan (2006), provided the fitted instrument propensity scores and fitted values from both treatment and outcome regressions.

Usage

late.aipw(y, tr, iv, mfp, mft, mfo, off = NULL)

Arguments

у	An $n \ge 1$ vector of observed outcomes.
tr	An $n \ge 1$ vector of treatment indicators (=1 if treated or 0 if untreated).
iv	An $n \ge 1$ vector of instruments (0 or 1).
mfp	An $n \ge 2$ matrix of fitted instrument propensity scores for $iv=0$ (first column) and $iv=1$ (second column).
mft	An $n \ge 2$ matrix of fitted values from treatment regression, for $iv=0$ (first column) and $iv=1$ (second column).
mfo	An $n \ge 4$ matrix of fitted values from outcome regression, for iv=0, tr=0 (first column), iv=0, tr=1 (second column), iv=1, tr=0 (third column) and iv=1, tr=1 (fourth column).
off	A 2 x 1 vector of offset values (e.g., the true values in simulations) used to calculate the z-statistics.

Details

The individual expectations $\theta_d = E(Y(d)|D(1) > D(0))$ are estimated separately for $d \in \{0, 1\}$ using inverse probability weighting ("ipw"), treatment and outcome regressions ("or") and augmented IPW methods as proposed in Tan (2006). The population LATE is defined as $\theta_1 - \theta_0$.

18

late.nreg

Value

ipw	A 2 x 1 vector of IPW estimates of θ_1 and θ_0 ; see Details .
or	A 2 x 1 vector of regression estimates of θ_1 and θ_0 ; see Details .
est	A 2 x 1 vector of augmented IPW estimates of θ_1 and θ_0 ; see Details .
var	The estimated variances associated with the augmented IPW estimates of θ_1 and θ_0 .
ze	The z-statistics for the augmented IPW estimates of θ_1 and θ_0 , compared to off.
late.est	The augmented IPW estimate of LATE.
late.var	The estimated variance associated with the augmented IPW estimate of LATE.
late.ze	The z-statistic for the augmented IPW estimate of LATE, compared to off.

References

Tan, Z. (2006) Regression and weighting methods for causal inference using instrumental variables, Journal of the American Statistical Association, 101, 1607–1618.

late.nreg	Model-assisted inference for local average treatment effects without
	regularization

Description

This function implements model-assisted inference for local average treatment effects, using non-regularized calibrated estimation.

Usage

```
late.nreg(y, tr, iv, fx, gx, hx, arm = 2, d1 = NULL, d2 = NULL,
ploss = "cal", yloss = "gaus", off = NULL)
```

Arguments

У	An $n \ge 1$ vector of observed outcomes.
tr	An $n \ge 1$ vector of treatment indicators (=1 if treated or 0 if untreated).
iv	An $n \ge 1$ vector of instruments (0 or 1).
fx	An $n \ge p$ matix of covariates, used in the instrument propensity score model.
gx	An $n \ge q_1$ matix of covariates, used in the treatment regression models.
hx	An $n \ge q_2$ matix of covariates, used in the outcome regression models.
arm	An integer 0, 1 or 2 indicating whether θ_0 , θ_1 or both are computed; see Details for late.aipw.
d1	Degree of truncated polynomials of fitted values from treatment regression to be included as regressors in the outcome regression (NULL: no adjustment, 0: piecewise constant, 1: piecewise linear etc).

d2	Number of knots of fitted values from treatment regression to be included as regressors in the outcome regression, with knots specified as the $i/(d2+1)$ -quantiles for $i=1,,d2$.
ploss	A loss function used in instrument propensity score estimation (either "ml" for likelihood estimation or "cal" for calibrated estimation).
yloss	A loss function used in outcome regression (either "gaus" for continuous outcomes or "ml" for binary outcomes).
off	A $2 \ge 1$ vector of offset values (e.g., the true values in simulations) used to calculate the z-statistics from augmented IPW estimation.

Details

For ploss="cal", calibrated estimation of the instrument propensity score (IPS) and weighted likelihood estimation of the treatment and outcome regression models are performed, similarly as in Sun and Tan (2020), but without regularization. See also **Details** for mn.nreg.

Value

ips	A list containing the results from fitting the instrument propensity score models by glm.nreg.
mfp	An $n \ge 2$ matrix of fitted instrument propensity scores for iv=0 (first column) and iv=1 (second column).
tps	A list containing the results from fitting the treatment regression models by glm.nreg.
mft	An $n \ge 2$ matrix of fitted treatment regression models for iv=0 (first column) and iv=1 (second column).
or	A list containing the results from fitting the outcome regression models by glm.nreg.
mfo	An $n \ge 4$ matrix of fitted outcome regression models for for iv=0, tr=0 (first column), iv=0, tr=1 (second column), iv=1, tr=0 (third column) and iv=1, tr=1 (fourth column). Two columns are set to NA if arm=0 or 1.
est	A list containing the results from augmented IPW estimation by late.aipw.

References

Tan, Z. (2006) Regression and weighting methods for causal inference using instrumental variables, Journal of the American Statistical Association, 101, 1607–1618.

Sun, B. and Tan, Z. (2020) High-dimensional model-assisted inference for local average treatment effects with instrumental variables, arXiv:2009.09286.

Examples

```
data(simu.iv.data)
n <- dim(simu.iv.data)[1]
p <- dim(simu.iv.data)[2]-3
y <- simu.iv.data[,1]</pre>
```

late.regu.cv

late.regu.cv

Model-assisted inference for local average treatment effects (LATEs) with instrumental variables based on cross validation

Description

This function implements model-assisted inference for LATEs with instrumental variables, using regularized calibrated estimation based on cross validation.

Usage

late.regu.cv(fold, nrho = NULL, rho.seq = NULL, y, tr, iv, fx, gx, hx, arm = 2, d1 = NULL, d2 = NULL, ploss = "cal", yloss = "gaus", off = NULL, ...)

Arguments

fold	A vector of length 3 giving the fold numbers for cross validation in instrument propensity score estimation, treatment and outcome regressions respectively.
nrho	A vector of length 3 giving the numbers of tuning parameters searched in cross validation.
rho.seq	A list of three vectors giving the tuning parameters in instrument propensity score estimation (first vector), treatment (second vector) and outcome (third vector) regressions.
У	An $n \ge 1$ vector of observed outcomes.
tr	An $n \ge 1$ vector of treatment indicators (=1 if treated or 0 if untreated).
iv	An $n \ge 1$ vector of instruments (0 or 1).
fx	An $n \ge p$ matix of covariates, used in the instrument propensity score model.
gx	An $n \ge q_1$ matix of covariates, used in the treatment regression models. In theory, gx should be a subvector of gx, hence $p \le q_1$.

hx	An $n \ge q_2$ matix of covariates, used in the outcome regression models. In theory, hx should be a subvector of hx, hence $p \le q_2$.
arm	An integer 0, 1 or 2 indicating whether θ_0 , θ_1 or both are computed; see Details for late.aipw.
d1	Degree of truncated polynomials of fitted values from treatment regression to be included as regressors in the outcome regression (NULL: no adjustment, 0: piecewise constant, 1: piecewise linear etc.).
d2	Number of knots of fitted values from treatment regression to be included as regressors in the outcome regression, with knots specified as the $i/(d2+1)$ -quantiles for $i=1,,d2$.
ploss	A loss function used in instrument propensity score estimation (either "ml" for likelihood estimation or "cal" for calibrated estimation).
yloss	A loss function used in outcome regression (either "gaus" for continuous outcomes or "ml" for binary outcomes).
off	A 2 x 1 vector of offset values (e.g., the true values in simulations) used to calculate the z-statistics from augmented IPW estimation.
	Additional arguments to glm. regu. cv.

Details

For ploss="cal", regularized calibrated estimation of the instrument propensity score (IPS) and regularized weighted likelihood estimation of the treatment and outcome regression models are performed. The method leads to model-assisted inference for LATE, in which condidence intervals are valid with high-dimensional data if the IPS model is correctly specified, but the treatment and outcome regression models may be misspecified (Sun and Tan 2020). For ploss="ml", regularized maximum likelihood estimation is used (Chernozhukov et al. 2018). In this case, standard errors are only shown to be valid if the IPS, treatment and outcome models are all correctly specified.

Value

ips	A list containing the results from fitting the instrument propensity score models by glm.regu.cv.
mfp	An $n \ge 2$ matrix of fitted instrument propensity scores for iv=0 (first column) and iv=1 (second column).
tps	A list containing the results from fitting the treatment regression models by $glm.regu.cv.$
mft	An $n \ge 2$ matrix of fitted treatment regression models for iv=0 (first column) and iv=1 (second column).
or	A list containing the results from fitting the outcome regression models by glm.regu.cv.
mfo	An $n \ge 4$ matrix of fitted outcome regression models for for iv=0, tr=0 (first column), iv=0, tr=1 (second column), iv=1, tr=0 (third column) and iv=1, tr=1 (fourth column). Two columns are set to NA if arm=0 or 1.
est	A list containing the results from augmented IPW estimation by late.aipw.

late.regu.path

References

Chernozhukov, V., Chetverikov, D., Demirer, M., Duflo, E., Hansen, C., Newey, W. and Robins, J.M. (2018) Double/debiased machine learning for treatment and structural parameters, *The Econometrics Journal*, 21, C1–C68.

Sun, B. and Tan, Z. (2020) High-dimensional model-assisted inference for local average treatment effects with instrumental variables, arXiv:2009.09286.

Examples

late.regu.path

Model-assisted inference for local average treatment effects along regularization paths

Description

This function implements model-assisted inference for local average treatment effects (LATEs) using regularized calibrated estimation along regularization paths for instrument propensity score (IPS) estimation, while based on cross validation for the treatment and outcome regressions.

Usage

```
late.regu.path(fold, nrho = NULL, rho.seq = NULL, y, tr, iv, fx, gx, hx,
arm = 2, d1 = NULL, d2 = NULL, ploss = "cal", yloss = "gaus",
off = NULL, ...)
```

Arguments

fold	A vector of length 3, with the second and third components giving the fold num- ber for cross validation in the treatment and outcome regressions respectively. The first component is not used.
nrho	A vector of length 3 giving the number of tuning parameters in a regularization path for IPS estimation and that in cross validation for the treatment and outcome regressions.
rho.seq	A list of two vectors giving the tuning parameters for IPS estimation (first vec- tor), treatment (second vector) and outcome (third vector) regressions.
У	An $n \ge 1$ vector of observed outcomes.
tr	An $n \ge 1$ vector of treatment indicators (=1 if treated or 0 if untreated).
iv	An $n \ge 1$ vector of instruments (0 or 1).
fx	An $n \ge p$ matix of covariates, used in the instrument propensity score model.
gx	An $n \ge q_1$ matix of covariates, used in the treatment regression models. In theory, gx should be a subvector of gx, hence $p \le q_1$.
hx	An $n \ge q_2$ matix of covariates, used in the outcome regression models. In theory, hx should be a subvector of gx, hence $p \le q_2$.
arm	An integer 0, 1 or 2 indicating whether θ_0 , θ_1 or both are computed; see Details for late.aipw.
d1	Degree of truncated polynomials of fitted values from treatment regression to be included as regressors in the outcome regression (NULL: no adjustment, 0: piecewise constant, 1: piecewise linear etc.).
d2	Number of knots of fitted values from treatment regression to be included as regressors in the outcome regression, with knots specified as the $i/(d2+1)$ -quantiles for $i=1,,d2$.
ploss	A loss function used in instrument propensity score estimation (either "ml" for likelihood estimation or "cal" for calibrated estimation).
yloss	A loss function used in outcome regression (either "gaus" for continuous out- comes or "ml" for binary outcomes).
off	A 2 x 1 vector of offset values (e.g., the true values in simulations) used to calculate the z-statistics from augmented IPW estimation.
	Additional arguments to glm.regu.cv and glm.regu.path.
Value	
ips	A list of 2 objects, giving the results from fitting the IPS models by $glm.regu.path$ for $iv=0$ (first) and $iv=1$ (second).
mfp	A list of 2 matrices of fitted instrument propensity scores, along the IPS regular- ization path, for $iv=0$ (first matrix) and $iv=1$ (second matrix).
tps	A list of 2 lists of objects for $iv=0$ (first) and $iv=1$ (second), where each object gives the results from fitting the treatment regression models by glm.regu.cv for an IPS tuning parameter.

mn.aipw

mft	A list of 2 matrices of fitted treatment regression models based on cross valida- tion, along the IPS regularization path, for $iv=0$ (first matrix) and $iv=1$ (second matrix).
or	A list of 4 lists of objects for iv=0, tr=0 (first), iv=0, tr=1 (second), iv=1, tr=0 (third) and iv=1, tr=1 (fourth), containing the results from fitting the outcome regression models by glm.regu.cv.
mfo	A list of 4 matrices of fitted outcome regression models based on cross vali- dation, along the IPS regularization path, for $iv=0$, $tr=0$ (first), $iv=0$, $tr=1$ (second), $iv=1$, $tr=0$ (third) and $iv=1$, $tr=1$ (fourth). Two matrices are set to NA if arm=0 or 1.
est	A list containing the results from augmented IPW estimation by late.aipw.
rho	A vector of tuning parameters leading to converged results in IPS estimation.

References

Sun, B. and Tan, Z. (2020) High-dimensional model-assisted inference for local average treatment effects with instrumental variables, arXiv:2009.09286.

Examples

Augmented inverse probability weighted estimation of population means

Description

mn.aipw

This function implements augmented inverse probability weighted (IPW) estimation of population means with missing data, provided both fitted propensity scores and fitted values from outcome regression.

Usage

mn.aipw(y, tr, fp, fo, off = 0)

Arguments

У	An $n \ge 1$ vector of outcomes with missing data.
tr	An $n \ge 1$ vector of non-missing indicators (=1 if y is observed or 0 if y is missing).
fp	An $n \ge 1$ vector of fitted propensity scores.
fo	An $n \ge 1$ vector of fitted values from outcome regression.
off	An offset value (e.g., the true value in simulations) used to calculate the z-statistic.

Value

one	The direct IPW estimate of 1.
ipw	The ratio IPW estimate.
or	The outcome regression estimate.
est	The augmented IPW estimate.
var	The estimated variance associated with the augmented IPW estimate.
ze	The z-statistic for the augmented IPW estimate, compared to off.

References

Tan, Z. (2020a) Regularized calibrated estimation of propensity scores with model misspecification and high-dimensional data, *Biometrika*, 107, 137–158.

Tan, Z. (2020b) Model-assisted inference for treatment effects using regularized calibrated estimation with high-dimensional data, *Annals of Statistics*, 48, 811–837.

mn.ipw

Inverse probability weighted estimation of population means

Description

This function implements inverse probability weighted (IPW) estimation of population means with missing data, provided fitted propensity scores.

Usage

mn.ipw(y, tr, fp)

mn.nreg

Arguments

У	An $n \ge 1$ vector of outcomes with missing data.
tr	An $n \ge 1$ vector of non-missing indicators (=1 if y is observed or 0 if y is miss-
	ing).
fp	An $n \ge 1$ vector of fitted propensity scores.

Details

The ratio IPW estimate is the direct IPW estimate divided by that with y replaced by a vector of 1s. The latter is referred to as the direct IPW estimate of 1.

Value

one	The direct IPW estimate of 1.
est	The ratio IPW estimate.

References

Tan, Z. (2020a) Regularized calibrated estimation of propensity scores with model misspecification and high-dimensional data, *Biometrika*, 107, 137–158.

Tan, Z. (2020b) Model-assisted inference for treatment effects using regularized calibrated estimation with high-dimensional data, *Annals of Statistics*, 48, 811–837.

mn.nreg

Model-assisted inference for population means without regularization

Description

This function implements model-assisted inference for population means with missing data, using non-regularized calibrated estimation.

Usage

mn.nreg(y, tr, x, ploss = "cal", yloss = "gaus", off = 0)

Arguments

У	An $n \ge 1$ vector of outcomes with missing data.
tr	An $n \ge 1$ vector of non-missing indicators (=1 if y is observed or 0 if y is missing).
x	An $n \ge p$ matix of covariates (excluding a constant), used in both propensity score and outcome regression models.
ploss	A loss function used in propensity score estimation (either "ml" or "cal").
yloss	A loss function used in outcome regression (either "gaus" for continuous outcomes or "ml" for binary outcomes).
off	An offset value (e.g., the true value in simulations) used to calculate the z- statistic from augmented IPW estimation.

Details

Two steps are involved in this function: first fitting propensity score and outcome regression models and then applying the augmented IPW estimator for a population mean. For ploss="cal", calibrated estimation is performed similarly as in Tan (2020a, 2020b), but without regularization. The method then leads to model-assisted inference, in which confidence intervals are valid if the propensity score model is correctly specified but the outcome regression model may be misspecified. With linear outcome models, the inference is also doubly robust (Kim and Haziza 2014; Vermeulen and Vansteelandt 2015). For ploss="ml", maximum likelihood estimation is used (Robins et al. 1994). In this case, standard errors are in general conservative if the propensity score model is correctly specified but the outcome regression model may be misspecified.

Value

ps	A list containing the results from fitting the propensity score model by glm.nreg.
fp	The $n \ge 1$ vector of fitted propensity scores.
or	A list containing the results from fitting the outcome regression model by glm.nreg.
fo	The $n \ge 1$ vector of fitted values from outcome regression.
est	A list containing the results from augmented IPW estimation by mn.aipw.

References

Kim, J.K. and Haziza, D. (2014) Doubly robust inference with missing data in survey sampling, *Statistica Sinica*, 24, 375-394.

Robins, J.M., Rotnitzky, A., and Zhao, L.P. (1994) Estimation of regression coefficients when some regressors are not always observed, *Journal of the American Statistical Association*, 89, 846-866.

Vermeulen, K. and Vansteelandt, S. (2015) Bias-reduced doubly robust estimation, *Journal of the American Statistical Association*, 110, 1024-1036.

Tan, Z. (2020a) Regularized calibrated estimation of propensity scores with model misspecification and high-dimensional data, *Biometrika*, 107, 137–158.

Tan, Z. (2020b) Model-assisted inference for treatment effects using regularized calibrated estimation with high-dimensional data, *Annals of Statistics*, 48, 811–837.

Examples

```
data(simu.data)
n <- dim(simu.data)[1]
p <- dim(simu.data)[2]-2
y <- simu.data[,1]
tr <- simu.data[,2]
x <- simu.data[,2+1:p]
x <- scale(x)
# missing data
y[tr==0] <- NA</pre>
```

include only 10 covariates

mn.regu.cv

x2 <- x[,1:10]
mn.cal <- mn.nreg(y, tr, x2, ploss="cal", yloss="gaus")
unlist(mn.cal\$est)</pre>

mn.regu.cv	Model-assisted inference for population means based on cross valida-
	tion

Description

This function implements model-assisted inference for population means with missing data, using regularized calibrated estimation based on cross validation.

Usage

```
mn.regu.cv(fold, nrho = NULL, rho.seq = NULL, y, tr, x, ploss = "cal",
yloss = "gaus", off = 0, ...)
```

Arguments

fold	A vector of length 2 giving the fold numbers for cross validation in propensity score estimation and outcome regression respectively.
nrho	A vector of length 2 giving the numbers of tuning parameters searched in cross validation.
rho.seq	A list of two vectors giving the tuning parameters in propensity score estimation (first vector) and outcome regression (second vector).
У	An $n \ge 1$ vector of outcomes with missing data.
tr	An $n \ge 1$ vector of non-missing indicators (=1 if y is observed or 0 if y is missing).
x	An $n \ge p$ matix of covariates, used in both propensity score and outcome regression models.
ploss	A loss function used in propensity score estimation (either "ml" or "cal").
yloss	A loss function used in outcome regression (either "gaus" for continuous outcomes or "ml" for binary outcomes).
off	An offset value (e.g., the true value in simulations) used to calculate the z- statistic from augmented IPW estimation.
	Additional arguments to glm. regu. cv.

Details

Two steps are involved in this function: first fitting propensity score and outcome regression models and then applying the augmented IPW estimator for a population mean. For ploss="cal", regularized calibrated estimation is performed with cross validation as described in Tan (2020a, 2020b). The method then leads to model-assisted inference, in which confidence intervals are valid with high-dimensinoal data if the propensity score model is correctly specified but the outcome regression model may be misspecified. With linear outcome models, the inference is also doubly robust. For ploss="ml", regularized maximum likelihood estimation is used (Belloni et al. 2014; Farrell 2015). In this case, standard errors are only shown to be valid if both the propensity score model and the outcome regression model are correctly specified.

Value

ps	A list containing the results from fitting the propensity score model by glm.regu.cv.
fp	The $n \ge 1$ vector of fitted propensity scores.
or	A list containing the results from fitting the outcome regression model by glm.regu.cv.
fo	The $n \ge 1$ vector of fitted values from outcome regression.
est	A list containing the results from augmented IPW estimation by mn.aipw.

References

Belloni, A., Chernozhukov, V., and Hansen, C. (2014) Inference on treatment effects after selection among high-dimensional controls, *Review of Economic Studies*, 81, 608-650.

Farrell, M.H. (2015) Robust inference on average treatment effects with possibly more covariates than observations, *Journal of Econometrics*, 189, 1-23.

Tan, Z. (2020a) Regularized calibrated estimation of propensity scores with model misspecification and high-dimensional data, *Biometrika*, 107, 137–158.

Tan, Z. (2020b) Model-assisted inference for treatment effects using regularized calibrated estimation with high-dimensional data, *Annals of Statistics*, 48, 811–837.

Examples

30

mn.regu.path

Model-assisted inference for population means along a regularization path

Description

This function implements model-assisted inference for population means with missing data, using regularized calibrated estimation along a regularization path for propensity score (PS) estimation while based on cross validation for outcome regression (OR).

Usage

```
mn.regu.path(fold, nrho = NULL, rho.seq = NULL, y, tr, x, ploss = "cal",
yloss = "gaus", off = 0, ...)
```

Arguments

fold	A vector of length 2, with the second component giving the fold number for cross validation in outcome regression. The first component is not used.
nrho	A vector of length 2 giving the number of tuning parameters in a regularization path for PS estimation and that in cross validation for OR.
rho.seq	A list of two vectors giving the tuning parameters for propensity score estimation (first vector) and outcome regression (second vector).
У	An $n \ge 1$ vector of outcomes with missing data.
tr	An $n \ge 1$ vector of non-missing indicators (=1 if y is observed or 0 if y is missing).
x	An $n \ge p$ matix of covariates, used in both propensity score and outcome regression models.
ploss	A loss function used in propensity score estimation (either "ml" or "cal").
yloss	A loss function used in outcome regression (either "gaus" for continuous outcomes or "ml" for binary outcomes).
off	An offset value (e.g., the true value in simulations) used to calculate the z- statistic from augmented IPW estimation.
	Additional arguments to glm.regu.cv and glm.regu.path.

Details

See **Details** for mn.regu.cv.

Value

ps	A list containing the results from fitting the propensity score model by glm.regu.path.
fp	The matrix of fitted propensity scores, column by column, along the PS regular- ization path.
or	A list of objects, each giving the results from fitting the outcome regression model by glm.regu.cv for a PS tuning parameter.
fo	The matrix of fitted values from outcome regression based on cross validation, column by column, along the PS regularization path.
est	A list containing the results from augmented IPW estimation by mn.aipw.
rho	A vector of tuning parameters leading to converged results in propensity score estimation.

References

Tan, Z. (2020a) Regularized calibrated estimation of propensity scores with model misspecification and high-dimensional data, *Biometrika*, 107, 137–158.

Tan, Z. (2020b) Model-assisted inference for treatment effects using regularized calibrated estimation with high-dimensional data, *Annals of Statistics*, 48, 811–837.

Examples

simu.data

Simulated data

Description

A dataset simulated as in Tan (2020), Section 4.

simu.data

Usage

data(simu.data)

Format

A data matrix with 800 rows and 202 columns.

Details

The dataset is generated as follows, where y, tr, and x represent an outcome, a treatment, and covariates respectively.

```
library(MASS)
###
mt0 <- 1-pnorm(-1)</pre>
mt1 <- dnorm(-1)</pre>
mt2 <- -(2*pnorm(-1)-1)/2 - dnorm(-1) +1/2
mt3 <- 3*dnorm(-1)</pre>
mt4 <- -3/2*(2*pnorm(-1)-1) - 4*dnorm(-1) +3/2
m.z1 <- mt0 + 2*mt1 + mt2
v.z1 <- mt0 + 4*mt1 + 6*mt2 + 4*mt3 + mt4
v.z1 < v.z1 + 1 + 2*(mt1 + 2*mt2 + mt3)
sd.z1 <- sqrt(v.z1 -m.z1^2)</pre>
###
set.seed(123)
n <- 800
p <- 200
noise <- rnorm(n)</pre>
covm <- matrix(1,p,p)</pre>
for (i1 in 1:p)
  for (i2 in 1:p) {
    covm[i1,i2] <- 2^(-abs(i1-i2))</pre>
  }
x <- mvrnorm(n, mu=rep(0,p), Sigma=covm)</pre>
# transformation
z <- x
for (i in 1:4) {
  z[,i] <- ifelse(x[,i]>-1,x[,i]+(x[,i]+1)^2,x[,i])
  z[,i] \leftarrow (z[,i]-m.z1) / sd.z1 \# standardized
}
```

```
# treatment
eta <- 1+ c( z[,1:4] %*% c(1, .5, .25, .125) )
tr <- rbinom(n, size=1, prob=expit(eta))
# outcome
eta.y <- c( z[,1:4] %*% c(1, .5, .25, .125) )
y <- eta.y + noise
# save; if using main effects of x, then both the propensity score
# and outcome regression models are misspecified
simu.data <- cbind(y, tr, x)
save(simu.data, file="simu.data.rda")
```

References

Tan, Z. (2020) Model-assisted inference for treatment effects using regularized calibrated estimation with high-dimensional data, *Annals of Statistics*, 48, 811–837.

simu.iv.data

Simulated instrumental variable data

Description

A dataset simulated as in Sun and Tan (2020), Section 4.

Usage

data(simu.iv.data)

Format

A data matrix with 800 rows and 203 columns.

Details

The dataset is generated as follows, where y, iv, tr and x represent an outcome, an instrumental variable, a treatment, and covariates respectively.

```
g<-function(z) {
1/(1+exp(z/b))^2*dnorm(z)
}
rnorm.trunct <- function(n, mu, sig, lft, rgt) {
    x <- rep(0,n)
    for (i in 1:n) {
        x[i] <- rnorm(1,mu,sig)
</pre>
```

```
while (x[i]<=lft | x[i]>rgt)
         x[i] <- rnorm(1,mu,sig)</pre>
   }
   return(x)
}
### covariate mean and variance computed as in preprint of Tan (2020)
a<- 2.5;
c<- 2*pnorm(a)-1;</pre>
b<- sqrt(1-2*a*dnorm(a)/c)</pre>
m1<- exp(1/(8*b^2))*(pnorm(a-1/(2*b))-pnorm(-a-1/(2*b)))/c
v1<- exp(1/(2*b^2))*(pnorm(a-1/b)-pnorm(-a-1/b))/c-m1^2;
m2<- 10;
v2<- 1/c*integrate(g,-a,a)$value #by numerical integration
m3 <- 3/(25<sup>2</sup>)*0.6+(0.6)<sup>3</sup>;
mu4 <-(1/(b^4*c))*((3/2*(2*pnorm(a)-1)-a*(a^2+3)*dnorm(a))</pre>
-(3/2*(2*pnorm(-a)-1)-(-a)*((-a)^2+3)*dnorm(-a)))
mu6 <-(1/(b^6*c))*((15/2*(2*pnorm(a)-1)-a*(a^4+5*a^2+15)*dnorm(a))</pre>
-(15/2*(2*pnorm(-a)-1)-(-a)*((-a)^4+5*(-a)^2+15)*dnorm(-a)))
v3 <-mu6^2/25^6+15*mu4^2/25^4*0.6^2+15/25^2*0.6^4+0.6^6-m3^2
m4<- 2+20^2;
v4<- (2*mu4+6)+6*2*20^2+20^4-m4^2
###
set.seed(120)
n<- 800
p<- 200
# covariates
x<- matrix(rnorm.trunct(p*n, 0, 1, -a, a),n,p)/b</pre>
# transformation
z<- x
z[,1] <- (exp(0.5*x[,1])-m1)/sqrt(v1);</pre>
z[,2] <- (10+x[,2]/(1+exp(x[,1]))-m2)/sqrt(v2);</pre>
z[,3] <- ((0.04*x[,1]*x[,3]+0.6)^3-m3)/sqrt(v3);</pre>
z[,4] <- ((x[,2]+x[,4]+20)^2-m4)/sqrt(v4);</pre>
```

instrumental variable

```
eta<- z[,1:4]
iv<- rbinom(n,1,prob=expit(eta));
# unmeasured confounder in latent index model
u<- rlogis(n, location = 0, scale = 1);
# treatment
eta.d<- 1+cbind(iv,z[,1:4])
tr<- as.numeric(eta.d >=u);
# outcome
late <- 1
eta.y <- late*tr +z[,1:4]
y <- rnorm(n, mean=eta.y, sd=1)
# save; if using main effects of x, then both the instrument propensity score
# and outcome models are misspecified
simu.iv.data <- cbind(y,tr,iv,x)
save(simu.iv.data, file="simu.iv.data.rda")
```

References

Tan, Z. (2020) Model-assisted inference for treatment effects using regularized calibrated estimation with high-dimensional data, *Annals of Statistics*, 48, 811–837.

Sun, B. and Tan, Z. (2020) High-dimensional model-assisted inference for local average treatment effects with instrumental variables, arXiv:2009.09286.

36

Index

ate.aipw, 3, 5, 7, 9 ate.ipw,4 ate.nreg, 5ate.regu.cv, 6, 8ate.regu.path,8 glm.nreg, 5, 9, 20, 28 glm.regu, 11, 14, 16 glm.regu.cv, 7-9, 14, 22, 24, 25, 29-32 glm.regu.path, 8, 16, 24, 31, 32 late.aipw, 18, 19, 20, 22, 24, 25 late.nreg, 19 late.regu.cv, 21 late.regu.path, 23 mn.aipw, 25, 28, 30, 32 mn.ipw, 26 mn.nreg, 5, 20, 27 mn.regu.cv, 7, 29, 31 mn.regu.path, 31RCAL (RCAL-package), 2 RCAL-package, 2 simu.data, 32

simu.iv.data, 34