# Package 'MultiATSM'

May 11, 2025

Type Package

Title Multicountry Term Structure of Interest Rates Models

Version 1.3.1

Date 2025-05-11

Description Estimation routines for several classes of affine term structure of interest rates models. All the models are based on the single-country unspanned macroeconomic risk framework from Joslin, Priebsch, and Singleton (2014, JF) <doi:10.1111/jofi.12131>. Multicountry extensions such as the ones of Jotikasthira, Le, and Lundblad (2015, JFE) <doi:10.1016/j.jfineco.2014.09.004>, Candelon and Moura (2023, EM) <doi:10.1016/j.econmod.2023.106453>, and Candelon and Moura (2024, JFEC) <doi:10.1093/jjfinec/nbae008> are also available.

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**Encoding** UTF-8

RoxygenNote 7.2.3

Imports ggplot2

Suggests readxl, cowplot, magic, reshape2, pracma, knitr, rmarkdown, bookdown, kableExtra, neldermead, magrittr, hablar

**Depends** R (>= 4.3.0)

VignetteBuilder knitr

URL https://github.com/rubensmoura87/MultiATSM

BugReports https://github.com/rubensmoura87/MultiATSM/issues

NeedsCompilation no

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**Repository** CRAN

Date/Publication 2025-05-11 04:40:02 UTC

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Bias\_Correc\_VAR

*Estimates an unbiased VAR(1) using stochastic approximation (Bauer, Rudebusch and Wu, 2012)* 

## Description

Estimates an unbiased VAR(1) using stochastic approximation (Bauer, Rudebusch and Wu, 2012)

## Bias\_Correc\_VAR

## Usage

```
Bias_Correc_VAR(
   ModelType,
   BRWinputs,
   RiskFactors,
   N,
   Economies,
   FactorLabels,
   GVARinputs = NULL,
   JLLinputs = NULL,
   ev_restr = 1,
   nargout = 4
)
```

## Arguments

ModelType	A character vector indicating the model type to be estimated.
BRWinputs	A list containing the necessary inputs for the BRW model estimation:
	1. flag_mean: Logical. Determines whether mean- (TRUE) or median- (FALSE) unbiased estimation is desired. Default is TRUE.
	2. gamma: Numeric. Adjustment parameter between 0 and 1. Default is 0.5.
	3. N_iter: Integer. Number of iterations for the stochastic approximation algorithm after burn-in. Default is 5,000.
	4. N_burn: Integer. Number of burn-in iterations. Default is 15
	5. B: Integer. Number of bootstrap samples per iteration for calculating the noisy measure of the OLS estimator's mean or median. Default is 50.
	<ol> <li>check: Logical. Indicates whether to perform a closeness check. Default is TRUE.</li> </ol>
	7. B_check: Integer. Number of bootstrap samples for the closeness check. Default is 100,000.
RiskFactors	A numeric matrix (T x F) representing the time series of risk factors.
Ν	Integer. Number of country-specific spanned factors.
Economies	A character vector containing the names of the economies included in the system.
FactorLabels	A list of character vectors with labels for all variables in the model.
GVARinputs	List. Inputs for GVAR model estimation (see GVAR function). Default is NULL.
JLLinputs	List. Inputs for JLL model estimation (see JLL function). Default is NULL.
ev_restr	Numeric. Restriction on the largest eigenvalue under the P-measure. Default is 1.
nargout	Integer. Number of elements in the output list. Default is 4.

## Value

Bias-corrected VAR parameters based on the framework of Bauer, Rudebusch and Wu (2012). The list contains:

- 1. Phi\_tilde: estimated coefficient matrix (F x F);
- 2. mu\_tilde: estimated intercept (F x 1);
- 3. V\_tilde: estimated variance-covariance matrix (F x F);
- 4. dist: root mean square distance (scalar);
- 5. Phi\_sample: sample estimated variance-covariance matrix used in the checks (F x F x B\_check) this output is reported if nargout is 5.

#### References

Bauer, Rudebusch and, Wu (2012). "Correcting Estimation Bias in Dynamic Term Structure Models"

This function is based on the est\_unb\_var Matlab function available at Cynthia Wu's website (https://sites.google.com/view/jingcynthiawu/).

#### Examples

Bootstrap

Generates the bootstrap-related outputs

#### Description

Generates the bootstrap-related outputs

#### Usage

```
Bootstrap(
ModelType,
ModelParaPE,
NumOutPE,
Economies,
InputsForOutputs,
FactorLabels,
```

#### Bootstrap

```
JLLlist = NULL,
GVARlist = NULL,
WishBC = 0,
BRWlist = NULL
```

## Arguments

)

ModelType	A character vector indicating the model type to be estimated.
ModelParaPE	A list containing the point estimates of the model parameters. For details, refer to the outputs from the Optimization function.
NumOutPE	The point estimate derived from numerical outputs. See the outputs from the NumOutputs function for further information.
Economies	A character vector containing the names of the economies included in the system.
InputsForOutput	ts
	A list containing the necessary inputs for generating IRFs, GIRFs, FEVDs, GFEVDs and Term Premia.
FactorLabels	A list of character vectors with labels for all variables in the model.
JLLlist	List. Inputs for JLL model estimation (see JLL function). Default is NULL.
GVARlist	List. Inputs for GVAR model estimation (see GVAR function). Default is NULL.
WishBC	Whether to estimate the physical parameter model with bias correction, based on the method by Bauer, Rudebusch and Wu (2012) (see Bias_Correc_VAR function). Default is set to 0.
BRWlist	List of necessary inputs for performing the bias-corrected estimation (see Bias_Correc_VAR function).

## Value

List containing the following elements:

- List of model parameters for each draw
- List of numerical outputs (IRFs, GIRFs, FEVDs, GFEVDs and Term Premia) for each draw
- Confidence bounds for the chosen level of significance

#### References

This function is a modified and extended version of the VARirbound function from "A toolbox for VAR analysis" by Ambrogio Cesa-Bianchi (https://github.com/ambropo/VAR-Toolbox)

#### Examples

# See an example of implementation in the vignette file of this package (Section 4).

BR\_jps\_out

## Description

Unspanned macro risk model outputs by Bauer and Rudebusch (2017)

#### Usage

data("BR\_jps\_gro\_R3")

#### Format

Unspanned macro risk model outputs by Bauer and Rudebusch (2017)

est.llk summary list of log-likelihood estimations

M.o time series of unspanned factors

pars additional summary list of log-likelihood estimations

W Weight matrix that results from principal components analysis

- Y time series of bond yields
- N total number of risk factor of the model (spanned and unspanned)
- ${\bf R}\,$  total number of spanned factor of the model

#### References

Bauer, M. and Rudebusch, G. "Resolving the Spanning Puzzle in Macro-Finance Term Structure Models"

DatabasePrep	Gather data of several countries in a list.	Particularly useful for
	GVAR-based setups (Compute "GVARFactors	s")

#### Description

Gather data of several countries in a list. Particularly useful for GVAR-based setups (Compute "GVARFactors")

#### DatabasePrep

#### Usage

```
DatabasePrep(
   t_First,
   t_Last,
   Economies,
   N,
   FactorLabels,
   ModelType,
   Wgvar = NULL,
   DataPathMacro = NULL,
   DataPathYields = NULL
)
```

## Arguments

t_First	Start date of the sample period in the format yyyy-mm-dd.
t_Last	End date of the sample period in the format yyyy-mm-dd.
Economies	A character vector containing the names of the economies included in the system.
Ν	Integer. Number of country-specific spanned factors.
FactorLabels	A list of character vectors with labels for all variables in the model.
ModelType	A character vector indicating the model type to be estimated.
Wgvar	GVAR transition matrix of size C x C, applicable if a GVAR-type model is selected. Default is NULL.
DataPathMacro	File path to the Excel file containing macroeconomic data, if provided. The default path points to the Excel file available within the package.
DataPathYields	File path to the Excel file containing yields data, if provided. The default path points to the Excel file available within the package

#### Value

List containing the risk factor set used in the estimation of the GVAR-based models

## Examples

```
DomVar <- c("Eco_Act", "Inflation")
GlobalVar <- c("GBC", "CPI_OECD")
t0 <- "2006-09-01"
tF <- "2019-01-01"
Economies <- c("China", "Brazil", "Mexico", "Uruguay", "Russia")
N <- 3
ModelType <- "GVAR multi"
FactorLabels <- LabFac(N, DomVar, GlobalVar, Economies, ModelType)
Wgvar <- Transition_Matrix(t_First = "2006", t_Last= "2019", Economies, type = "Sample Mean")</pre>
```

GVARFactors <- DatabasePrep(t0, tF, Economies, N, FactorLabels, ModelType, Wgvar)

DataForEstimation

*Retrieves data from Excel and build the database used in the model estimation* 

#### Description

Retrieves data from Excel and build the database used in the model estimation

#### Usage

```
DataForEstimation(
   t0,
   tF,
   Economies,
   N,
   FactorLabels,
   ModelType,
   DataFrequency,
   W_type = NULL,
   t_First_Wgvar = NULL,
   t_Last_Wgvar = NULL,
   DataPathMacro = NULL,
   DataPathYields = NULL,
   DataPathTrade = NULL
)
```

#### Arguments

tØ	Start date of the sample period in the format yyyy-mm-dd.
tF	End date of the sample period in the format yyyy-mm-dd.
Economies	A character vector containing the names of the economies included in the system.
Ν	Integer. Number of country-specific spanned factors.
FactorLabels	String-list based which contains the labels of all the variables present in the model
ModelType	String-vector containing the label of the model to be estimated
DataFrequency	Character-based-vector. Available options are: "Daily All Days", "Daily Business Days", "Weekly", "Monthly", "Quarterly", "Annually"
W_type	Three possibilities:
	• Full Sample: if one wishes ALL weight matrices of each year from which data is available (it may extrapolate the sample period);

		<ul> <li>Sample Mean: if one wishes a SINGLE weight matrix containing the average of weights over of the entire sample period;</li> <li>Some ways in particular (a.g. "1008" "2005" )</li> </ul>
		• Some year in particular (e.g. "1998", "2005").
t	_First_Wgvar	Sample starting date (year)
t	_Last_Wgvar	Sample last date (year)
D	ataPathMacro	Path of the Excel file containing the macroeconomic data (if any). The default is linked to the excel file present in the package.
D	ataPathYields	Path of the Excel file containing the yields data (if any). The default is linked to the excel file present in the package.
C	ataPathTrade	Path of the Excel file containing the trade data (if any). The default is linked to the excel file present in the package.

#### Value

A list containing the

- 1. time series of the complete set of bond yields (matrix, J x T or CJ x T);
- 2. time series of the complete set risk factors (matrix, K x T);
- 3. 'GVARFactors': list of all variables that are used in the estimation of the VARX (see e.g. CM\_Factors\_GVAR file). If the estimated model type is not GVAR-based, then returns NULL.

#### See Also

InputsForOpt

## Examples

```
DomVar <- c("Eco_Act", "Inflation")
GlobalVar <- c("GBC", "CPI_OECD")
t0 <- "2006-09-01"
tF <- "2019-01-01"
Economies <- c("China", "Brazil", "Mexico", "Uruguay", "Russia")
N <- 2
ModelType <- "JPS original"
FactorLabels <- LabFac(N, DomVar, GlobalVar, Economies, ModelType)
DataFrequency <- "Monthly"</pre>
```

DataModel <- DataForEstimation(t0, tF, Economies, N, FactorLabels, ModelType, DataFrequency)</pre>

DomesticMacroVar

## Description

Risk factors data used in Candelon and Moura (2024, JFEC)

#### Usage

```
data("CM_DomMacroFactors")
```

#### Format

matrix containing the risk factors of the models

#### References

Candelon, B. and Moura, R. (2024) "A Multicountry Model of the Term Structures of Interest Rates with a GVAR". (Journal of Financial Econometrics)

DomMacro

Data: Risk Factors for the GVAR - Candelon and Moura (2023)

## Description

Risk factors data used in the GVAR models - Candelon and Moura (2023)

#### Usage

```
data("CM_DomMacro_2023")
```

#### Format

list containing the variables used in the GVAR models

#### References

Candelon, B. and Moura, R. (2023) "Sovereign yield curves and the COVID-19 in emerging markets". (Economic Modelling)

FactorsGVAR

#### Description

Risk factors data used in the GVAR models - Candelon and Moura (2024, JFEC)

#### Usage

```
data("CM_Factors_GVAR")
```

#### Format

list containing the variables used in the GVAR models

#### References

Candelon, B. and Moura, R. (2024) "A Multicountry Model of the Term Structures of Interest Rates with a GVAR". (Journal of Financial Econometrics)

ForecastYields	Generates forecasts	of bond vields	for all model types

#### Description

Generates forecasts of bond yields for all model types

#### Usage

```
ForecastYields(
   ModelType,
   ModelPara,
   InputsForOutputs,
   FactorLabels,
   Economies,
   JLLlist = NULL,
   GVARlist = NULL,
   WishBRW,
   BRWlist = NULL
)
```

#### Arguments

ModelType	A character vector indicating the model type to be estimated.
ModelPara	A list containing the point estimates of the model parameters. For details, refer to the outputs from the Optimization function.
InputsForOutpu	ts
	A list containing the necessary inputs for generating IRFs, GIRFs, FEVDs, GFEVDs and Term Premia.
FactorLabels	A list of character vectors with labels for all variables in the model.
Economies	A character vector containing the names of the economies included in the system.
JLLlist	A list of necessary inputs for the estimation of JLL-based models (see the JLL function).
GVARlist	A list containing the necessary inputs for the estimation of GVAR-based models (see the GVAR function).
WishBRW	Whether to estimate the physical parameter model with bias correction, based on the method by Bauer, Rudebusch and Wu (2012) (see Bias_Correc_VAR function). Default is set to 0.
BRWlist	List of necessary inputs for performing the bias-corrected estimation (see Bias_Correc_VAR function).

#### Value

An object of class 'ATSMModelForecast' containing the following elements:

- 1. Out-of-sample forecasts of bond yields per forecast horizon
- 2. Out-of-sample forecast errors of bond yields per forecast horizon
- 3. Root mean square errors per forecast horizon

#### **Available Methods**

- 'plot(object)'

### Examples

# See an example of implementation in the vignette file of this package (Section 4).

GlobalMacro

#### Description

Risk factors data used in Candelon and Moura (2023)

#### Usage

```
data("CM_GlobalMacro_2023")
```

#### Format

matrix containing the risk factors of the models

#### References

Candelon, B. and Moura, R. (2023) "Sovereign yield curves and the COVID-19 in emerging markets". (Economic Modelling)

GlobalMacroVar Data: Risk Factors - Candelon and Moura (2024, JFEC)

## Description

Risk factors data used in Candelon and Moura (2024, JFEC)

#### Usage

```
data("CM_GlobalMacroFactors")
```

#### Format

matrix containing the risk factors of the models

#### References

Candelon, B. and Moura, R. (2024) "A Multicountry Model of the Term Structures of Interest Rates with a GVAR". (Journal of Financial Econometrics)

#### Description

Estimates a GVAR(1) and a VARX(1,1,1) models

#### Usage

```
GVAR(GVARinputs, N, CheckInputs = FALSE)
```

#### Arguments

**GVARinputs** List of inputs for GVAR model estimation: 1. Economies: A character vector containing the names of the economies included in the system. 2. GVARFactors: A list of all variables used in the estimation of the VARX model (see e.g. CM\_Factors\_GVAR file for details); 3. VARXtype: A character vector with three possible options: • 'unconstrained': model is estimated without constraints (each equation is estimated individually by ordinary least square); • 'constrained: Spanned Factors': The model is estimated with the restriction that foreign pricing factors do NOT affect (i) domestic economic variables and (ii) domestic pricing factors. (Equations are estimated using restricted least squares) • 'constrained : [factor\_name]': The model is estimated with the restriction that the specified risk factor is influenced only by its own lagged values and the lagged values of its corresponding star variables. (Equations are estimated using restricted least squares.) 4. Wgvar: The GVAR transition matrix (C x C) used in the model solution. (See the output from the Transition\_Matrix function.). Ν Integer. Number of country-specific spanned factors. CheckInputs A logical flag to indicate whether to perform a prior consistency check on the inputs provided in GVARinputs. The default is set to FALSE

#### Value

#### A list containing

- 1. parameters of the country-specific VARX(1,1,1)
  - intercept (M+Nx1);
  - phi\_1 (M+N x M+N);
  - phi\_1^star (M+N x M+N);
  - phi\_g (M+N x M+N);

## GVAR

- Sigma (M+N x G)
- 2. parameters of the GVAR.
  - F0 (F X 1);
  - F1 (F x F);
  - Sigma\_y (F x F)

#### References

Chudik and Pesaran, (2016). "Theory and Practice of GVAR modelling" (Journal of Economic Surveys)

#### Examples

InputsForOpt	Generates inputs necessary to build the likelihood function for the
	ATSM model

#### Description

Generates inputs necessary to build the likelihood function for the ATSM model

#### Usage

```
InputsForOpt(
   InitialSampleDate,
   FinalSampleDate,
   ModelType,
   Yields,
   GlobalMacro,
   DomMacro,
   FactorLabels,
   Economies,
   DataFrequency,
   GVARlist = NULL,
```

```
JLLlist = NULL,
WishBRW = FALSE,
BRWlist = NULL,
UnitYields = "Month",
CheckInputs = TRUE,
BS_Adj = FALSE
)
```

#### Arguments

InitialSampleDate		
	Start date of the sample period in the format "dd-mm-yyyy"	
FinalSampleDat		
	End date of the sample period in the format "dd-mm-yyyy"	
ModelType	A character vector indicating the model type to be estimated. Available options: "JPS original", "JPS global", "GVAR single", "JPS multi", "GVAR multi", "JLL original", "JLL No DomUnit", "JLL joint Sigma".	
Yields	A numerical matrix with time series of yields (JxT or CJ x T)	
GlobalMacro	A numerical matrix with time series of the global risk factors (G x T)	
DomMacro	A numerical matrix with time series of the country-specific risk factors for all C countries (CM x T)	
FactorLabels	A list of character vectors with labels for all variables in the model.	
Economies	A character vector containing the names of the economies included in the system.	
DataFrequency	A character vector specifying the frequency of the data. Available options are: "Daily All Days", "Daily Business Days", "Weekly", "Monthly", "Quarterly", or "Annually".	
GVARlist	A list containing the necessary inputs for the estimation of GVAR-based models	
JLLlist	A list of necessary inputs for the estimation of JLL-based models. If the chosen model is "JLL original" or "JLL joint Sigma", then a dominant unit economy must be chosen. Otherwise, this list must be set as 'None'.	
WishBRW	Logical. Whether to estimate the physical parameter model with bias correction, based on the method by Bauer, Rudebusch and Wu (2012). Default is FALSE.	
BRWlist	List of necessary inputs for performing the bias-corrected estimation.	
UnitYields	A character string indicating the maturity unit of yields. Options are: "Month" for yields expressed in months, or "Year" for yields expressed in years. Default is "Month".	
CheckInputs	Logical. Whether to perform a prior check on the consistency of the provided input list. Default is TRUE.	
BS_Adj	Logical. Whether to adjust the global series for the sepQ models in the Bootstrap setting. Default is FALSE.	

## Value

An object of class 'ATSMModelInputs' containing the necessary inputs for performing the model optimization.

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#### InputsForOpt

#### **Available Methods**

- 'print(object)' - 'summary(object)'

#### Examples

```
# Example 1:
data(CM_GlobalMacroFactors)
data(CM_DomMacroFactors)
data(CM_Yields)
ModelType <- "JPS original"</pre>
Economies <- "Mexico"
t0 <- "01-05-2007" # Initial Sample Date (Format: "dd-mm-yyyy")</pre>
tF <- "01-12-2018" # Final Sample Date (Format: "dd-mm-yyyy")
N < -3
GlobalVar <- c("Gl_Eco_Act") # Global Variables</pre>
DomVar <- c("Eco_Act") # Domestic Variables</pre>
FactorLabels <- LabFac(N, DomVar, GlobalVar, Economies, ModelType)</pre>
DataFreq <- "Monthly"</pre>
ATSMInputs <- InputsForOpt(t0, tF, ModelType, Yields, GlobalMacroVar, DomesticMacroVar,
                               FactorLabels, Economies, DataFreq, CheckInputs = FALSE)
# Example 2:
LoadData("CM_2024")
ModelType <- "GVAR multi"</pre>
Economies <- c("China", "Brazil", "Mexico", "Uruguay")</pre>
t0 <- "01-05-2007" # InitialSampleDate (Format: "dd-mm-yyyy")</pre>
tF <- "01-12-2019" # FinalSampleDate (Format: "dd-mm-yyyy")</pre>
N <- 2
GlobalVar <- c("Gl_Eco_Act", "Gl_Inflation") # Global Variables</pre>
DomVar <- c("Inflation") # Domestic Variables</pre>
FactorLabels <- LabFac(N, DomVar, GlobalVar, Economies, ModelType)</pre>
DataFreq <- "Monthly"</pre>
GVARlist <- list(VARXtype = "unconstrained", W_type = "Sample Mean",
                  t_First_Wgvar = "2007", t_Last_Wgvar = "2019")
ATSMInputs <- InputsForOpt(t0, tF, ModelType, Yields, GlobalMacroVar, DomesticMacroVar,
                         FactorLabels, Economies, DataFreq, GVARlist, CheckInputs = FALSE)
# Example 3:
if (requireNamespace('neldermead', quietly = TRUE)) {
LoadData("CM_2024")
ModelType <- "JLL original"</pre>
Economies <- c("China", "Brazil", "Uruguay")</pre>
t0 <- "01-05-2007" # InitialSampleDate (Format: "dd-mm-yyyy")</pre>
```

```
tF <- "01-12-2019" # FinalSampleDate (Format: "dd-mm-yyyy")
N <- 2
GlobalVar <- c("Gl_Eco_Act", "Gl_Inflation") # Global Variables
DomVar <- c("Eco_Act", "Inflation") # Domestic Variables
FactorLabels <- LabFac(N, DomVar, GlobalVar, Economies, ModelType)
JLLinputs <- list(DomUnit = "China")
DataFrequency <- "Monthly"
ATSMInputs <- InputsForOpt(t0, tF, ModelType, Yields, GlobalMacroVar, DomesticMacroVar,
FactorLabels, Economies, DataFreq, JLLlist = JLLinputs,
CheckInputs = FALSE)
} else {
message("skipping functionality due to missing Suggested dependency")
}
```

InputsForOutputs	Collects the inputs that are used to construct the numerical and the
	graphical outputs

#### Description

Collects the inputs that are used to construct the numerical and the graphical outputs

#### Usage

```
InputsForOutputs(
 ModelType,
 Horiz,
 ListOutputWished,
 OutputLabel,
 WishStationarityQ,
 DataFrequency,
 WishGraphYields = 0,
 WishGraphRiskFactors = 0,
 WishOrthoJLLgraphs = 0,
 WishForwardPremia = 0,
 LimFP = NULL,
 WishBootstrap = 0,
 ListBoot = NULL,
 WishForecast = 0,
 ListForecast = NULL,
 UnitYields = "Month"
)
```

## **InputsForOutputs**

## Arguments

ModelType	A character vector indicating the model type to be estimated.
Horiz	A numeric scalar specifying the desired analysis horizon for the outputs.
ListOutputWish	ed
	A list of desired graphical outputs. Available options are: "Fit", "IRF", "FEVD", "GIRF", "GFEVD", "TermPremia".
OutputLabel	A string for the name of the output label to be stored.
WishStationari	tyQ
	A binary variable $(1 \text{ or } 0)$ indicating whether to impose that the largest eigenvalue under Q is strictly smaller than 1. Set to 1 to impose the restriction, or 0 otherwise.
DataFrequency	A character vector specifying the data frequency. Available options: "Daily All Days", "Daily Business Days", "Weekly", "Monthly", "Quarterly", "Annually".
WishGraphYield	s
	A binary variable (1 or 0) indicating whether the user wishes to generate graphs for yields. Default is 0.
WishGraphRiskF	actors
	A binary variable (1 or 0) indicating whether the user wishes to generate graphs for risk factors. Default is 0.
WishOrthoJLLgr	
	A binary variable (1 or 0) indicating whether the user wishes to generate orthog- onalized JLL-based graphs. Default is 0.
WishForwardPre	
	A binary variable $(1 \text{ or } 0)$ indicating whether the user wishes to generate forward premia graphs. Default is 0.
LimFP	A numeric vector containing the maturities associated with the start and end dates of the loan.
WishBootstrap	A binary variable (1 or 0) indicating whether the user wishes to perform bootstrap- based estimation. Default is 0.
ListBoot	A List containing the following four elements:
	1. methodBS: Desired bootstrap method: (a) 'bs' for standard residual boot- strap, (b) 'wild' for wild bootstrap, or (c) 'block' for block bootstrap.
	<ol> <li>BlockLength: If block bootstrap is chosen, specify the block length (numeric scalar).</li> </ol>
	3. ndraws: Number of bootstrap draws.
	4. pctg: Confidence level expressed in basis points (numeric vector).
WishForecast	A binary variable (1 or 0) indicating whether the user wishes to generate fore- casts. Default is 0.
ListForecast	A list containing the following three elements:
	1. ForHoriz: forecast horizon;
	2. t0Sample: Index of the first variable in the information set.
	3. t0Forecast: Index of the first forecast cut-off date.

	<ol> <li>ForType: A string specifying the desired forecast type. Available options are: "Rolling" or "Expanding".</li> </ol>
UnitYields	A character string indicating the maturity unit of yields. Options are: (i) "Month" for yields expressed in months, or (ii) "Year" for yields expressed in years. Default is "Month".

## Value

List of necessary inputs to generate the graphs of the outputs of the desired model

#### Examples

```
ModelType <- "JPS original"
Horiz <- 100
DesiredOutputGraphs <- c("Fit", "GIRF", "GFEVD")
OutputLabel <- "Test"
WishStationarityQ <- 1
WishGraphRiskFac <- 0
WishGraphYields <- 1
InputsList <- InputsForOutputs(ModelType, Horiz, DesiredOutputGraphs, OutputLabel,</pre>
```

```
WishStationarityQ, WishGraphYields, WishGraphRiskFac)
```

JLL

Estimates	the	P-dyna	mics	from.	JLL	-based	mode	els

#### Description

Estimates the P-dynamics from JLL-based models

## Usage

```
JLL(NonOrthoFactors, N, JLLinputs, CheckInputs = FALSE)
```

## Arguments

NonOrthoFactor	`S
	A numeric matrix (F x T) representing the time series of risk factors before the orthogonalization process.
Ν	Integer. Number of country-specific spanned factors.
JLLinputs	List of necessary inputs to estimate JLL models:
	1. Economies: set of economies that are part of the economic system (string-vector)
	2. DomUnit: A string specifying the name of the economy assigned as the dominant unit.
	If no dominant unit is assigned, set this variable to "None".

	<ol> <li>WishSigmas: Set to "1" if the user wishes to estimate the variance-covariance matrices and Cholesky factorizations (this can take a long time). Set to "0" if not.</li> </ol>
	4. SigmaNonOrtho: A NULL value or an F x F matrix from the non-orthogonalized dynamics.
	5. JLLModelType: A string specifying the type of JLL model. Available op- tions are: "JLL original", "JLL joint Sigma", or "JLL No DomUnit".
CheckInputs	A logical flag to indicate whether to perform a prior consistency check on the inputs provided in JLLinputs. The default is set to FALSE

#### Value

List of model parameters from both the orthogonalized and non-orthogonalized versions of the JLL's based models

#### References

Jotiskhatira, Le and Lundblad (2015). "Why do interest rates in different currencies co-move?" (Journal of Financial Economics)

#### Examples

```
data(CM_Factors)
RF_TS <- RiskFactors</pre>
N <- 3
JLLinputs <- list(Economies = c("China", "Brazil", "Mexico", "Uruguay"), DomUnit = "China",</pre>
                   WishSigmas = 1, SigmaNonOrtho = NULL, JLLModelType = "JLL original")
JLLPara <- JLL(RF_TS, N, JLLinputs)</pre>
```

LabFac

Generates the labels factors

## Description

Generates the labels factors

#### Usage

LabFac(N, DomVar, GlobalVar, Economies, ModelType)

## Arguments

Ν	Integer. Number of country-specific spanned factors.
DomVar	A character vector containing the names of the domestic variables.
GlobalVar	A character vector containing the names of the global variables.
Economies	A character vector containing the names of the economies included in the system.
ModelType	A character vector indicating the model type to be estimated.

#### Value

List containing the risk factor labels

#### Examples

```
N <- 2
DomVar <- c("inflation", "Output gap")
GlobalVar <- "Commodity Prices"
Economies <- c("U.S.", "Canada", "Germany", "Japan")
ModelType <- "JPS original"
VarLabels <- LabFac(N, DomVar, GlobalVar, Economies, ModelType)</pre>
```

LoadData

Loads data sets from several papers

## Description

Loads data sets from several papers

#### Usage

```
LoadData(DataPaper)
```

## Arguments

DataPaper	Available options are BR_2017 (Bauer and Rudebusch, 2017), CM_2023 (Can-
	delon and Moura, 2023), CM_2024 (Candelon and Moura, 2024)

#### Value

Complete set of data from several papers.

#### ModelPara

#### References

- 1. Bauer and Rudebusch (2017). "Resolving the Spanning Puzzle in Macro-Finance Term Structure Models" (Review of Finance)
- 2. Candelon and Moura (2023). "Sovereign yield curves and the COVID-19 in emerging markets" (Economic Modelling)
- 3. Candelon and Moura (2024). "A Multicountry Model of the Term Structures of Interest Rates with a GVAR" (Journal of Financial Econometrics)

#### Examples

#Example 1: LoadData("BR\_2017")

#Example 2: LoadData("CM\_2023")

#Example 3: LoadData("CM\_2024")

ModelPara

#### Replications of the JPS (2014) outputs by the MultiATSM package

## Description

Unspanned macro risk model outputs by the MultiATSM package

#### Usage

data("JPSrep")

#### Format

list of inputs and outputs

inputs general model inputs

ests model parameters estimates (JPS form)

- llk log-likelihood of the observations
- rot model parameters estimates (rotation form)

MultiATSM

## Description

Estimation of several classes of affine term structure of interest rates models.

#### Author(s)

Rubens Moura <rubens.gtmoura@gmail.com>

NumOutputs	Constructs the model numerical outputs (model fit, IRFs, GIR	₹Fs,
	FEVDs, GFEVDs, and risk premia decomposition)	

#### Description

Constructs the model numerical outputs (model fit, IRFs, GIRFs, FEVDs, GFEVDs, and risk premia decomposition)

#### Usage

NumOutputs(ModelType, ModelPara, InputsForOutputs, FactorLabels, Economies)

#### Arguments

ModelType	A character vector indicating the model type to be estimated.
ModelPara	A list containing the point estimates of the model parameters. For details, refer to the outputs from the Optimization function.
InputsForOutput	ts
	A list containing the necessary inputs for generating IRFs, GIRFs, FEVDs, GFEVDs and Term Premia.
FactorLabels	A list of character vectors with labels for all variables in the model.
Economies	A character vector containing the names of the economies included in the system.

## Details

Both IRFs and FEVDs are computed using the Cholesky decomposition method. The risk factors are ordered as follows: (i) global unspanned factors, and (ii) domestic unspanned and spanned factors for each country. The order of countries follows the sequence defined in the Economies vector.

#### Optimization

#### Value

List of the model numerical outputs, namely

- 1. Model fit of bond yields
- 2. IRFs
- 3. FEVDs
- 4. GIRFs
- 5. GFEVDs
- 6. Bond yield decomposition

#### References

Pesaran, H. Hashem, and Shin, Yongcheol. "Generalized impulse response analysis in linear multivariate models." Economics letters 58.1 (1998): 17-29.

#### Examples

# See an example of implementation in the vignette file of this package (Section 4).

•	Perform the optimization of the log-likelihood function of the chosen ATSM
---	--

## Description

Perform the optimization of the log-likelihood function of the chosen ATSM

#### Usage

```
Optimization(
    MLEinputs,
    StatQ,
    DataFreq,
    FactorLabels,
    Economies,
    ModelType,
    tol = 1e-04,
    TimeCount = TRUE,
    BS_outputs = FALSE
)
```

#### Arguments

MLEinputs	A list containing the necessary inputs for building the log-likelihood function (see InputsForOpt function).
StatQ	A binary variable (1 or 0) indicating whether to impose that the largest eigenvalue under Q is strictly smaller than 1. Set to 1 to impose the restriction, or 0 otherwise.
DataFreq	A character vector specifying the data frequency. Available options: "Daily All Days", "Daily Business Days", "Weekly", "Monthly", "Quarterly", "Annually".
FactorLabels	A list of character vectors with labels for all variables in the model.
Economies	A character vector containing the names of the economies included in the system.
ModelType	A character vector indicating the model type to be estimated.
tol	Convergence tolerance (scalar). The default is 1e-4.
TimeCount	Logical. If TRUE, computes the time required for model estimation. Default is TRUE.
BS_outputs	Logical. If TRUE, generates a simplified output list in the bootstrap setting. Default is FALSE.

#### Value

An object of class 'ATSMModelOutputs' containing model outputs after the optimization of the chosen ATSM specification.

#### **Available Methods**

- 'summary(object)'

#### References

This function is partially adapted from the LS\_\_opt function by Le and Singleton (2018). "A Small Package of Matlab Routines for the Estimation of Some Term Structure Models." (Euro Area Business Cycle Network Training School - Term Structure Modelling). Available at: https://cepr.org/40029

## Examples

# See examples in the vignette file of this package (Section 4).

Out

#### Description

Example for illustration used in the package vignette

#### Usage

data("Out\_Example")

#### Format

several model classes

ModelParaList List of parameter estimates of the selected ATSM ATSMinputs General inputs from an ATSM Forecasts List of forecast outputs

pca\_weights\_one\_country

Computes the PCA weights for a single country

#### Description

Computes the PCA weights for a single country

#### Usage

pca\_weights\_one\_country(Yields, Economy)

#### Arguments

Yields	A matrix of bond yields (J x T) for a single country, where J is the number of
	maturities and T is the time series length.
Economy	A character string indicating the name of the economy.

#### Value

A matrix (J x J) that corresponds to the eigenvectors of the variance-covariance matrix of yields

## Examples

```
data(CM_Yields)
Economy <- "Mexico"
pca_weights <- pca_weights_one_country(Yields, Economy)</pre>
```

plot.ATSMModelForecast

Plot method for ATSMModelForecast objects

## Description

Plot method for ATSMModelForecast objects

#### Usage

```
## S3 method for class 'ATSMModelForecast'
plot(x, ...)
```

#### Arguments

х	An object of class ATSMModelForecast
	Additional arguments (not used)

print.ATSMModelInputs Print method for ATSMModelInputs objects

#### Description

Print method for ATSMModelInputs objects

## Usage

```
## S3 method for class 'ATSMModelInputs'
print(x, ...)
```

## Arguments

х	An object of class 'ATSMModelInputs'
	Additional arguments (not used)

RiskFactors

#### Description

Risk factors data used in Candelon and Moura (2024, JFEC)

#### Usage

```
data("CM_Factors")
```

#### Format

matrix containing the risk factors of the models

## References

Candelon, B. and Moura, R. (2024) "A Multicountry Model of the Term Structures of Interest Rates with a GVAR". (Journal of Financial Econometrics)

Spanned\_Factors Computes the country-specific spanned factors

### Description

Computes the country-specific spanned factors

#### Usage

Spanned\_Factors(Yields, Economies, N)

#### Arguments

Yields	A matrix (J x T), where J is the number of maturities and T is the length of the time series.
Economies	A character vector containing the names of the economies included in the system.
Ν	Scalar representing the desired number of country-specific spanned factors (maximum allowed is $N = J$ ).

#### Value

Matrix containing the N spanned factors for all the countries of the system (CJ x T)

## Examples

```
data(CM_Yields)
Economies <- c("China", "Brazil", "Mexico", "Uruguay")
N <- 3
SpaFact_TS <- Spanned_Factors(Yields, Economies, N)</pre>
```

StarFactors Generates the star variables necessary for the GVAR estimation

## Description

Generates the star variables necessary for the GVAR estimation

## Usage

StarFactors(RiskFactors, Economies, W)

#### Arguments

RiskFactors	time series of the risk factors (F x T)
Economies	string-vector containing the names of the economies which are part of the economic system
W	GVAR transition matrix (C x C)

#### Value

List containg the star factors of each country of the economic system

#### Examples

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summary.ATSMModelInputs

Summary method for ATSMModelInputs objects

## Description

Summary method for ATSMModelInputs objects

#### Usage

```
## S3 method for class 'ATSMModelInputs'
summary(object, ...)
```

## Arguments

object	An object of class 'ATSMModelInputs'
	Additional arguments (not used)

```
summary.ATSMModelOutputs
```

Summary method for ATSMModelOutputs objects

## Description

Summary method for ATSMModelOutputs objects

## Usage

```
## S3 method for class 'ATSMModelOutputs'
summary(object, ...)
```

#### Arguments

object	An object of class 'ATSMModelOutputs'
	Additional arguments (not used)

TradeFlows

#### Description

Trade Flows data used in Candelon and Moura (2024, JFEC)

#### Usage

```
data("CM_Trade")
```

#### Format

list containing the bilateral trade flows

#### References

Candelon, B. and Moura, R. (2024) "A Multicountry Model of the Term Structures of Interest Rates with a GVAR". (Journal of Financial Econometrics)

Trade\_Flows

Data: Trade Flows - Candelon and Moura (2023)

## Description

Trade Flows data used in Candelon and Moura (2023)

#### Usage

data("CM\_Trade")

#### Format

list containing the bilateral trade flows

#### References

Candelon, B. and Moura, R. (2023) "Sovereign yield curves and the COVID-19 in emerging markets". (Economic Modelling)

Transition\_Matrix

## Description

Computes the transition matrix required in the estimation of the GVAR model

#### Usage

```
Transition_Matrix(
  t_First,
  t_Last,
  Economies,
  type,
  DataConnectedness = NULL,
  DataPath = NULL
)
```

## Arguments

t_First	Sample starting date (in the format: yyyy).
t_Last	Sample ending date (in the format: yyyy).
Economies	A character vector containing the names of the economies included in the system.
type	A character string indicating the method for computing interdependence. Possible options include:
	• Time-varying: Computes time-varying interdependence and returns the weight matrices for each year based on available data (may extrapolate the sample period).
	• Sample Mean: Returns a single weight matrix containing the average weights over the entire sample period, suitable for time-invariant interdependence.
	• A specific year (e.g., "1998", "2005"): Used to compute time-invariant in- terdependence for the specified year.
DataConnectedness	
	Data used to compute the transition matrix. Default is set to NULL.
DataPath	Path to the Excel file containing the data (if applicable). The default is linked to the Excel file available in the package.

## Details

If there is missing data for any country of the system for that particularly year, then the transition matrix will include only NAs.

#### Value

matrix or list of matrices

## Examples

```
data(CM_Trade)
```

```
t_First <- "2006"
t_Last <- "2019"
Economies <- c("China", "Brazil", "Mexico", "Uruguay")
type <- "Sample Mean"
W_mat <- Transition_Matrix(t_First, t_Last, Economies, type, DataConnectedness = TradeFlows)</pre>
```

VAR

Estimates a standard VAR(1)

#### Description

Estimates a standard VAR(1)

#### Usage

VAR(RiskFactors, VARtype, Bcon = NULL)

#### Arguments

RiskFactors	A numeric matrix (FTx T) representing the time series of risk factors.
VARtype	String vector with two possible values: 'unconstrained' or 'constrained'.
Bcon	Constraints matrix (F+1 x N), which includes an intercept. If $Bcon(i,j) = NA$ , then $B(i,j)$ is treated as a free parameter. Default is set to NULL.

#### Value

intercept, feedback matrix and the variance-covariance matrix of a VAR(1)

#### Examples

```
data("CM_Factors")
# Example 1: unconstrained case
VAR(RiskFactors, VARtype= 'unconstrained')
```

```
# Example 2: constrained case
K <- nrow(RiskFactors)
Bcon <- matrix(0, nrow = K, ncol = K+1)
Bcon[, 1:3] <- NaN
VAR(RiskFactors, VARtype= 'constrained', Bcon)</pre>
```

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Yields

#### Description

Yields data used in Candelon and Moura (2024, JFEC) Bond yield data used in Candelon and Moura (2023)

#### Usage

```
data("CM_Yields")
```

data("CM\_Yields\_2023")

#### Format

matrix containing the Yields of the models matrix containing the Yields of the models

#### References

Candelon, B. and Moura, R. (Forthcoming) "A Multicountry Model of the Term Structures of Interest Rates with a GVAR". (Journal of Financial Econometrics)

Candelon, B. and Moura, R. (2023) "Sovereign yield curves and the COVID-19 in emerging markets". (Economic Modelling)

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