

# Package ‘JSparO’

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**Title** Joint Sparse Optimization via Proximal Gradient Method for Cell Fate Conversion

**Version** 1.5.0

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**Description** Implementation of joint sparse optimization (JSparO) to infer the gene regulatory network for cell fate conversion. The proximal gradient method is implemented to solve different low-order regularization models for JSparO.

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**License** GPL (>= 3)

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demo\_JSparO

*demo\_JSparO - The demo of JSparO package*

## Description

This is the main function of JSparO aimed to solve the low-order regularization models with  $l_{p,q}$  norm.

## Usage

```
demo_JSparO(A, B, X, s, p, q, maxIter = 200)
```

## Arguments

A	Gene expression data of transcriptome factors (i.e. feature matrix in machine learning). The dimension of A is m * n.
B	Gene expression data of target genes (i.e. observation matrix in machine learning). The dimension of B is m * t.
X	Gene expression data of Chromatin immunoprecipitation or other matrix (i.e. initial iterative point in machine learning). The dimension of X is n * t.
s	joint sparsity level
p	value for $l_{p,q}$ norm (i.e., p = 1 or 2)
q	value for $l_{p,q}$ norm (i.e., 0 <= q <= 1)
maxIter	maximum iteration

## Details

The demo\_JSparO function is used to solve joint sparse optimization problem via different algorithms. Based on  $l_{p,q}$  norm, functions with different p and q are implemented to solve the problem:

$$\min \|AX - B\|_F^2 + \lambda\|X\|_{p,q}$$

to obtain s-joint sparse solution.

## Value

The solution of proximal gradient method with  $l_{p,q}$  regularizer.

## Author(s)

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## Examples

```
m <- 256; n <- 1024; t <- 5; maxIter0 <- 50
A0 <- matrix(rnorm(m * n), nrow = m, ncol = n)
B0 <- matrix(rnorm(m * t), nrow = m, ncol = t)
X0 <- matrix(0, nrow = n, ncol = t)
res_JSpar0 <- demo_JSpar0(A0, B0, X0, s = 10, p = 2, q = 'half', maxIter = maxIter0)
```

L1HalfThr

*L1HalfThr - Iterative Half Thresholding Algorithm based on  $l_1, l_{1/2}$  norm*

## Description

The function aims to solve  $l_{1,1/2}$  regularized least squares.

## Usage

```
L1HalfThr(A, B, X, s, maxIter = 200)
```

## Arguments

A	Gene expression data of transcriptome factors (i.e. feature matrix in machine learning). The dimension of A is m * n.
B	Gene expression data of target genes (i.e. observation matrix in machine learning). The dimension of B is m * t.
X	Gene expression data of Chromatin immunoprecipitation or other matrix (i.e. initial iterative point in machine learning). The dimension of X is n * t.
s	joint sparsity level
maxIter	maximum iteration

## Details

The L1HalfThr function aims to solve the problem:

$$\min \|AX - B\|_F^2 + \lambda \|X\|_{1,1/2}$$

to obtain s-joint sparse solution.

## Value

The solution of proximal gradient method with  $l_{1,1/2}$  regularizer.

## Author(s)

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## Examples

```
m <- 256; n <- 1024; t <- 5; maxIter0 <- 50
A0 <- matrix(rnorm(m * n), nrow = m, ncol = n)
B0 <- matrix(rnorm(m * t), nrow = m, ncol = t)
X0 <- matrix(0, nrow = n, ncol = t)
NoA <- norm(A0, '2'); A0 <- A0/NoA; B0 <- B0/NoA
res_L1half <- L1HalfThr(A0, B0, X0, s = 10, maxIter = maxIter0)
```

L1HardThr

*L1HardThr - Iterative Hard Thresholding Algorithm based on  $l_{1,0}$  norm*

## Description

The function aims to solve  $l_{1,0}$  regularized least squares.

## Usage

```
L1HardThr(A, B, X, s, maxIter = 200)
```

## Arguments

A	Gene expression data of transcriptome factors (i.e. feature matrix in machine learning). The dimension of A is m * n.
B	Gene expression data of target genes (i.e. observation matrix in machine learning). The dimension of B is m * t.
X	Gene expression data of Chromatin immunoprecipitation or other matrix (i.e. initial iterative point in machine learning). The dimension of X is n * t.
s	joint sparsity level
maxIter	maximum iteration

## Details

The L1HardThr function aims to solve the problem:

$$\min \|AX - B\|_F^2 + \lambda\|X\|_{1,0}$$

to obtain s-joint sparse solution.

## Value

The solution of proximal gradient method with  $l_{1,0}$  regularizer.

## Author(s)

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## Examples

```
m <- 256; n <- 1024; t <- 5; maxIter0 <- 50
A0 <- matrix(rnorm(m * n), nrow = m, ncol = n)
B0 <- matrix(rnorm(m * t), nrow = m, ncol = t)
X0 <- matrix(0, nrow = n, ncol = t)
NoA <- norm(A0, '2'); A0 <- A0/NoA; B0 <- B0/NoA
res_L10 <- L1HardThr(A0, B0, X0, s = 10, maxIter = maxIter0)
```

L1normFun

L1normFun

## Description

The function aims to compute the  $l_1$  norm.

## Usage

```
L1normFun(x)
```

## Arguments

x	vector
---	--------

## Details

The L1normFun aims to compute the  $l_1$  norm:  $\sum_i^n |x_i|$

## Value

The  $l_1$  norm of vector x

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L1SoftThr

*L1SoftThr - Iterative Soft Thresholding Algorithm based on  $l_{1,1}$  norm*

## Description

The function aims to solve  $l_{1,1}$  regularized least squares.

## Usage

```
L1SoftThr(A, B, X, s, maxIter = 200)
```

## Arguments

A	Gene expression data of transcriptome factors (i.e. feature matrix in machine learning). The dimension of A is m * n.
B	Gene expression data of target genes (i.e. observation matrix in machine learning). The dimension of B is m * t.
X	Gene expression data of Chromatin immunoprecipitation or other matrix (i.e. initial iterative point in machine learning). The dimension of X is n * t.
s	joint sparsity level
maxIter	maximum iteration

## Details

The L1SoftThr function aims to solve the problem:

$$\min \|AX - B\|_F^2 + \lambda\|X\|_{1,1}$$

to obtain s-joint sparse solution.

## Value

The solution of proximal gradient method with  $l_{1,1}$  regularizer.

## Author(s)

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## Examples

```
m <- 256; n <- 1024; t <- 5; maxIter0 <- 50
A0 <- matrix(rnorm(m * n), nrow = m, ncol = n)
B0 <- matrix(rnorm(m * t), nrow = m, ncol = t)
X0 <- matrix(0, nrow = n, ncol = t)
NoA <- norm(A0, '2'); A0 <- A0/NoA; B0 <- B0/NoA
res_L11 <- L1SoftThr(A0, B0, X0, s = 10, maxIter = maxIter0)
```

---

L1twothirdsThr	<i>L1twothirdsThr - Iterative Thresholding Algorithm based on l_1,2/3 norm</i>
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**Description**

The function aims to solve  $l_{1,2/3}$  regularized least squares.

**Usage**

```
L1twothirdsThr(A, B, X, s, maxIter = 200)
```

**Arguments**

A	Gene expression data of transcriptome factors (i.e. feature matrix in machine learning). The dimension of A is m * n.
B	Gene expression data of target genes (i.e. observation matrix in machine learning). The dimension of B is m * t.
X	Gene expression data of Chromatin immunoprecipitation or other matrix (i.e. initial iterative point in machine learning). The dimension of X is n * t.
s	joint sparsity level
maxIter	maximum iteration

**Details**

The L1twothirdsThr function aims to solve the problem:

$$\min \|AX - B\|_F^2 + \lambda\|X\|_{1,2/3}$$

to obtain s-joint sparse solution.

**Value**

The solution of proximal gradient method with  $l_{1,2/3}$  regularizer.

**Author(s)**

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**Examples**

```
m <- 256; n <- 1024; t <- 5; maxIter0 <- 50
A0 <- matrix(rnorm(m * n), nrow = m, ncol = n)
B0 <- matrix(rnorm(m * t), nrow = m, ncol = t)
X0 <- matrix(0, nrow = n, ncol = t)
NoA <- norm(A0, '2'); A0 <- A0/NoA; B0 <- B0/NoA
res_L1twothirds <- L1twothirdsThr(A0, B0, X0, s = 10, maxIter = maxIter0)
```

L2HalfThr

*L2HalfThr - Iterative Half Thresholding Algorithm based on l\_2,1/2 norm*

## Description

The function aims to solve  $l_{2,1/2}$  regularized least squares.

## Usage

```
L2HalfThr(A, B, X, s, maxIter = 200)
```

## Arguments

A	Gene expression data of transcriptome factors (i.e. feature matrix in machine learning). The dimension of A is m * n.
B	Gene expression data of target genes (i.e. observation matrix in machine learning). The dimension of B is m * t.
X	Gene expression data of Chromatin immunoprecipitation or other matrix (i.e. initial iterative point in machine learning). The dimension of X is n * t.
s	joint sparsity level
maxIter	maximum iteration

## Details

The L2HalfThr function aims to solve the problem:

$$\min \|AX - B\|_F^2 + \lambda\|X\|_{2,1/2}$$

to obtain s-joint sparse solution.

## Value

The solution of proximal gradient method with  $l_{2,1/2}$  regularizer.

## Author(s)

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## Examples

```
m <- 256; n <- 1024; t <- 5; maxIter0 <- 50
A0 <- matrix(rnorm(m * n), nrow = m, ncol = n)
B0 <- matrix(rnorm(m * t), nrow = m, ncol = t)
X0 <- matrix(0, nrow = n, ncol = t)
NoA <- norm(A0, '2'); A0 <- A0/NoA; B0 <- B0/NoA
res_L2half <- L2HalfThr(A0, B0, X0, s = 10, maxIter = maxIter0)
```

---

L2HardThr*L2HardThr - Iterative Hard Thresholding Algorithm based on l\_2,0 norm*

---

## Description

The function aims to solve  $l_{2,0}$  regularized least squares.

## Usage

```
L2HardThr(A, B, X, s, maxIter = 200)
```

## Arguments

A	Gene expression data of transcriptome factors (i.e. feature matrix in machine learning). The dimension of A is m * n.
B	Gene expression data of target genes (i.e. observation matrix in machine learning). The dimension of B is m * t.
X	Gene expression data of Chromatin immunoprecipitation or other matrix (i.e. initial iterative point in machine learning). The dimension of X is n * t.
s	joint sparsity level
maxIter	maximum iteration

## Details

The L2HardThr function aims to solve the problem:

$$\min \|AX - B\|_F^2 + \lambda\|X\|_{2,0}$$

to obtain s-joint sparse solution.

## Value

The solution of proximal gradient method with  $l_{2,0}$  regularizer.

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## Examples

```
m <- 256; n <- 1024; t <- 5; maxIter0 <- 50
A0 <- matrix(rnorm(m * n), nrow = m, ncol = n)
B0 <- matrix(rnorm(m * t), nrow = m, ncol = t)
X0 <- matrix(0, nrow = n, ncol = t)
NoA <- norm(A0, '2'); A0 <- A0/NoA; B0 <- B0/NoA
res_L20 <- L2HardThr(A0, B0, X0, s = 10, maxIter = maxIter0)
```

---

**L2NewtonThr***L2NewtonThr - Iterative Thresholding Algorithm based on l\_2, q norm with Newton method*

---

## Description

The function aims to solve  $l_{2,q}$  regularized least squares, where the proximal optimization subproblems will be solved by Newton method.

## Usage

```
L2NewtonThr(A, B, X, s, q, maxIter = 200, innMaxIter = 30, innEps = 1e-06)
```

## Arguments

A	Gene expression data of transcriptome factors (i.e. feature matrix in machine learning). The dimension of A is m * n.
B	Gene expression data of target genes (i.e. observation matrix in machine learning). The dimension of B is m * t.
X	Gene expression data of Chromatin immunoprecipitation or other matrix (i.e. initial iterative point in machine learning). The dimension of X is n * t.
s	joint sparsity level
q	value for $l_{2,q}$ norm (i.e., $0 < q < 1$ )
maxIter	maximum iteration
innMaxIter	maximum iteration in Newton step
innEps	criterion to stop inner iteration

## Details

The L2NewtonThr function aims to solve the problem:

$$\min \|AX - B\|_F^2 + \lambda\|X\|_{2,q}$$

to obtain s-joint sparse solution.

## Value

The solution of proximal gradient method with  $l_{2,q}$  regularizer.

## Author(s)

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Yaohua Hu [mayhhu@szu.edu.cn](mailto:mayhhu@szu.edu.cn)

## Examples

```
m <- 256; n <- 1024; t <- 5; maxIter0 <- 50
A0 <- matrix(rnorm(m * n), nrow = m, ncol = n)
B0 <- matrix(rnorm(m * t), nrow = m, ncol = t)
X0 <- matrix(0, nrow = n, ncol = t)
NoA <- norm(A0, '2'); A0 <- A0/NoA; B0 <- B0/NoA
res_L2q <- L2NewtonThr(A0, B0, X0, s = 10, q = 0.2, maxIter = maxIter0)
```

L2SoftThr

*L2SoftThr - Iterative Soft Thresholding Algorithm based on  $l_{2,1}$  norm*

## Description

The function aims to solve  $l_{2,1}$  regularized least squares.

## Usage

```
L2SoftThr(A, B, X, s, maxIter = 200)
```

## Arguments

A	Gene expression data of transcriptome factors (i.e. feature matrix in machine learning). The dimension of A is m * n.
B	Gene expression data of target genes (i.e. observation matrix in machine learning). The dimension of B is m * t.
X	Gene expression data of Chromatin immunoprecipitation or other matrix (i.e. initial iterative point in machine learning). The dimension of X is n * t.
s	joint sparsity level
maxIter	maximum iteration

## Details

The L2SoftThr function aims to solve the problem:

$$\min \|AX - B\|_F^2 + \lambda\|X\|_{2,1}$$

to obtain s-joint sparse solution.

## Value

The solution of proximal gradient method with  $l_{2,1}$  regularizer.

## Author(s)

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Yaohua Hu [mayhhu@szu.edu.cn](mailto:mayhhu@szu.edu.cn)

## Examples

```
m <- 256; n <- 1024; t <- 5; maxIter0 <- 50
A0 <- matrix(rnorm(m * n), nrow = m, ncol = n)
B0 <- matrix(rnorm(m * t), nrow = m, ncol = t)
X0 <- matrix(0, nrow = n, ncol = t)
NoA <- norm(A0, '2'); A0 <- A0/NoA; B0 <- B0/NoA
res_L21 <- L2SoftThr(A0, B0, X0, s = 10, maxIter = maxIter0)
```

L2twothirdsThr

*L2twothirdsThr - Iterative Thresholding Algorithm based on  $l_2, 2/3$  norm*

## Description

The function aims to solve  $l_{2,2/3}$  regularized least squares.

## Usage

```
L2twothirdsThr(A, B, X, s, maxIter = 200)
```

## Arguments

A	Gene expression data of transcriptome factors (i.e. feature matrix in machine learning). The dimension of A is m * n.
B	Gene expression data of target genes (i.e. observation matrix in machine learning). The dimension of B is m * t.
X	Gene expression data of Chromatin immunoprecipitation or other matrix (i.e. initial iterative point in machine learning). The dimension of X is n * t.
s	joint sparsity level
maxIter	maximum iteration

## Details

The L2twothirdsThr function aims to solve the problem:

$$\min \|AX - B\|_F^2 + \lambda\|X\|_{2,2/3}$$

to obtain s-joint sparse solution.

## Value

The solution of proximal gradient method with  $l_{2,2/3}$  regularizer.

## Author(s)

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Yaohua Hu [mayhhu@szu.edu.cn](mailto:mayhhu@szu.edu.cn)

**Examples**

```
m <- 256; n <- 1024; t <- 5; maxIter0 <- 50
A0 <- matrix(rnorm(m * n), nrow = m, ncol = n)
B0 <- matrix(rnorm(m * t), nrow = m, ncol = t)
X0 <- matrix(0, nrow = n, ncol = t)
NoA <- norm(A0, '2'); A0 <- A0/NoA; B0 <- B0/NoA
res_L2twothirds <- L2twothirdsThr(A0, B0, X0, s = 10, maxIter = maxIter0)
```

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