# Package 'BMS'

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**Depends** methods, stats, graphics, R (>= 2.10)

**Description** Bayesian Model Averaging for linear models with a wide choice of (customizable) priors. Built-in priors include coefficient priors (fixed, hyper-g and empirical pri-

ors), 5 kinds of model priors, moreover model sampling by enumeration or various MCMC approaches. Post-processing functions allow for inferring posterior inclusion and model probabilities, various moments, coefficient and predictive densities. Plotting functions available for posterior model size, MCMC convergence, predictive and coefficient densities, best models representation, BMA comparison. Also includes Bayesian normal-conjugate linear model with Zellner's g prior, and assorted methods.

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as.zlm

Extract a Model from a bma Object

# Description

Extracts a model out of a bma object's saved models and converts it to a zlm linear model

# Usage

as.zlm(bmao, model = 1)

#### as.zlm

# Arguments

bmao	A bma object, e.g. resulting from a call to bms
model	The model index, in one of the following forms: An integer, denoting the rank of the model (1 for best, 2 for second-best,) A numeric or logical vector of length K describing which covariates are con- tained in the model
	A hexcode character describing which covariates are contained in the model

# Details

A bma object stores several 'best' models it encounters (cf. argument nmodel in bms). as.zlm extracts a single model and converts it to an object of class zlm, which represents a linear model estimated under Zellner's g prior.

The utility model.frame allows to transfrom a zlm model into an OLS model of class lm.

# Value

a list of class zlm

#### Author(s)

Stefan Zeugner

#### See Also

bms for creating bma objects, zlm for creating zlm objects, pmp.bma for displaying the topmodels in a bma object

Check http://bms.zeugner.eu for additional help.

### Examples

```
data(datafls)
```

mm=bms(datafls[,1:6],mcmc="enumeration") # do a small BMA chain topmodels.bma(mm)[,1:5] #display the best 5 models

m2a=as.zlm(mm,4) #extract the fourth best model
summary(m2a)

```
# Bayesian Model Selection:
# transform the best model into an OLS model:
lm(model.frame(as.zlm(mm)))
```

```
# extract the model only containing the 5th regressor m2b=as.zlm(mm,c(0,0,0,0,1))
```

```
# extract the model only containing the 5th regressor in hexcode
print(bin2hex(c(0,0,0,0,1)))
m2c=as.zlm(mm,"01")
```

beta.draws.bma Coefficients of the Best Models

# Description

Returns a matrix whose columns are the (expected value or standard deviations of) coefficients for the best models in a bma object.

#### Usage

beta.draws.bma(bmao, stdev = FALSE)

### Arguments

bmao	a 'bma' object (as e.g. resulting from bms)
stdev	if stdev=FALSE then beta.draws.bma returns the (conditional) posterior expected values of the coefficients (i.e. 'Bayesian coefficients'). If stdev=TRUE it returns their posterior standard deviations.

# Value

Each column presents the coefficients for the model indicated by its column name. The zero coefficients are the excluded covariates per model. Note that the coefficients returned are only those of the best (100) models encountered by the bma object (cf. argument nmodels of bms).

For aggregate coefficients please refer to coef.bma.

#### Note

Note that the elements of beta.draws.bma(bmao) correspond to bmao\$topmod\$betas()

### See Also

bms for creating bms objects, coef.bma for aggregate coefficients Check http://bms.zeugner.eu for additional help.

# Examples

```
#sample a bma object:
data(datafls)
mm=bms(datafls,burn=500,iter=5000,nmodel=20)
#coefficients for all
beta.draws.bma(mm)
```

# bma-class

#standard deviations for the fourth- to eight best models beta.draws.bma(mm[4:8],TRUE);

bma-class

Class "bma"

# Description

A list holding results from a BMA iteration chain

# **Objects from the Class**

Objects can be created via calls to bms, but indirectly also via c.bma A bma object is a list whose elements hold information on input and output for a Bayesian Model Averaging iteration chain, such as from a call to bms:

# Author(s)

Martin Feldkircher and Stefan Zeugner

### References

http://bms.zeugner.eu

# See Also

bms for creating bma objects, or topmod for the topmod object

# Examples

```
data(datafls)
mm=bms(datafls)
#show posterior model size
print(mm$info$msize/mm$info$cumsumweights)
#is the same number as in
summary(mm)
```

# Description

Given data and prior information, this function samples all possible model combinations via MC3 or enumeration and returns aggregate results.

# Usage

```
bms(
 X.data,
 burn = 1000,
  iter = NA,
 nmodel = 500,
 mcmc = "bd",
 g = "UIP",
 mprior = "random",
 mprior.size = NA,
 user.int = TRUE,
  start.value = NA,
  g.stats = TRUE,
  logfile = FALSE,
  logstep = 10000,
  force.full.ols = FALSE,
  fixed.reg = numeric(0)
)
```

# Arguments

X.data	a data frame or a matrix, with the dependent variable in the first column, fol- lowed by the covariates (alternatively, X.data can also be provided as a formula). Note that bms automatically estimates a constant, therefore including constant terms is not necessary.
burn	The (positive integer) number of burn-in draws for the MC3 sampler, defaults to 1000. (Not taken into account if mcmc="enumerate")
iter	If mcmc is set to an MC3 sampler, then this is the number of iteration draws to be sampled (ex burn-ins), default 3000 draws. If mcmc="enumerate", then iter is the number of models to be sampled, starting from 0 (defaults to $2^{K} - 1$ ) - cf. start.value.
nmodel	<ul><li>the number of best models for which information is stored (default 500). Best models are used for convergence analysis between likelihoods and MCMC frequencies, as well as likelihood-based inference.</li><li>Note that a very high value for nmodel slows down the sampler significantly. Set nmodel=0 to speed up sampling (if best model information is not needed).</li></ul>

# bms

bms

mcmc	a character denoting the model sampler to be used. The MC3 sampler mcmc="bd" corresponds to a birth/death MCMC algogrithm. mcmc="rev.jump" enacts a reversible jump algorithm adding a "swap" step to the birth / death steps from "bd". Alternatively, the entire model space may be fully enumerated by setting mcmc="enumerate" which will iterate all possible regressor combinations (Note: consider that this means $2^{K}$ iterations, where K is the number of covariates.) Default is full enumeration (mcmc="enumerate") with less then 15 covariates, and the birth-death MC3 sampler (mcmc="bd") with 15 covariates or more. Cf. section 'Details' for more options.
g	the hyperparameter on Zellner's g-prior for the regression coefficients. g="UIP" corresponds to $g = N$ , the number of observations (default); g="BRIC" corresponds to the benchmark prior suggested by Fernandez, Ley and Steel (2001), i.e $g = max(N, K^2)$ , where K is the total number of covariates; $g="RIC"$ sets $g = K^2$ and conforms to the risk inflation criterion by George and Foster (1994)
	g="HQ" sets $g = log(N)^3$ and asymptotically mimics the Hannan-Quinn criterion with $C_{HQ} = 3$ (cf. Fernandez, Ley and Steel, 2001, p.395) g="EBL" estimates a local empirical Bayes g-parameter (as in Liang et al. (2008)); g="hyper" takes the 'hyper-g' prior distribution (as in Liang et al., 2008) with the default hyper-parameter $a$ set such that the prior expected shrinkage factor conforms to 'UIP'; This hyperparameter $a$ can be adjusted (between $2 < a <= 4$ ) by setting g="hyper=2.9", for instance. Alternatively, g="hyper=UIP" sets the prior expected value of the shrinkage fac- tor equal to that of UIP (default), g="hyper=BRIC" sets it according to BRIC cf section 'Details' fro more on the hyper-g prior
mprior	a character denoting the model prior choice, defaulting to "random": mprior="fixed" denotes fixed common prior inclusion probabilities for each regressor as e.g. in Sala-i-Martin, Doppelhofer, and Miller(2004) - for their fine-tuning, cf. mprior.size. Preferable to mcmc="random" if strong prior in- formation on model size exists; mprior="random" (default) triggers the 'random theta' prior by Ley and Steel (2008), who suggest a binomial-beta hyperprior on the a priori inclusion proba- bility; mprior="uniform" employs the uniform model prior; mprior="customk" allows for custom model size priors (cf. mprior.size); mprior="pip" allows for custom prior inclusion probabilities (cf. mprior.size); Note that the prior on models with more than N-3 regressors is automatically zero: these models will not be sampled.
mprior.size	if mprior is "fixed" or "random", mprior.size is a scalar that denotes the prior expected value of the model size prior (default K/2). If mprior="customk" then a custom model size prior can be provided as a K+1 vector detailing the priors from model size 0 to K (e.g. rep(1,K+1) for the uni- form model prior); if mprior="pip", then custom prior inclusion probabilities can be provided as a vector of size K, with elements in the interval (0,1)
user.int	'interactive mode': print out results to console after ending the routine and plots

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#### a chart (default TRUE).

start.value	specifies the starting model of the iteration chain. For instance a specific model by the corresponding column indices (e.g. starting.model=numeric(K) starts from the null model including solely a constant term) or start.value=c(3,6) for a starting model only including covariates 3 and 6. If start.model is set to an integer (e.g. start.model=15) then that number of covariates (here: 15 covariates) is randomly chosen and the starting model is identified by those regressors with an OLS t-statistic>0.2. The default value start.value=NA corresponds to start.value=min(ncol(X.data),nrow(X.data)-3 Note that start.value=0 or start.value=NULL starts from the null model. If mcmc="enumerate" then start.value is the index to start the iteration (de- fault: 0, the null model). Any number between 0 and $K^2 - 1$ is admissible.
g.stats	TRUE if statistics on the shrinkage factor $g/(1+g)$ should be collected, defaulting to TRUE (Note: set g.stats=FALSE for faster iteration.)
logfile	setting logfile=TRUE produces a logfile named "test.log" in your current working directory, in order to keep track of the sampling procedure. logfile equal to some filepath (like logfile="subfolder/log.txt") puts the logfile into that specified position. (default: logfile=FALSE). Note that logfile="" implies log printouts on the console.
logstep	specifies at which number of posterior draws information is written to the log file; default: 10 000 iterations
force.full.ols	default FALSE. If force.full.ols=TRUE, the OLS estimation part of the sam- pling procedure relies on slower matrix inversion, instead of streamlined rou- tines.force.full.ols=TRUE can slow down sampling but may deal better with highly collinear data
fixed.reg	indices or variable names of X.data that are fixed regressors to be always in- cluded in every sampled model. Note: the parameter mprior.size refers to prior model size including these fixed regressors.

# Details

Ad mcmc:

Interaction sampler: adding an ".int" to an MC3 sampler (e.g. "mcmc="bd.int") provides for special treatment of interaction terms. Interaction terms will only be sampled along with their component variables: In the colnumn names of X.data, interaction terms need to be denominated by names consisting of the base terms separated by # (e.g. an interaction term of base variables "A", "B" and "C" needs column name "A#B#C"). Then variable "A#B#C" will only be included in a model if all of the component variables ("A", "B", and "C") are included.

The MC3 samplers "bd", "rev.jump", "bd.int" and "rev.jump.int", iterate away from a starting model by adding, dropping or swapping (only in the case of rev.jump) covariates.

In an MCMC fashion, they thus randomly draw a candidate model and then move to it in case its marginal likelihood (marg.lik.) is superior to the marg.lik. of the current model.

In case the candidate's marg.lik is inferior, it is randomly accepted or rejected according to a probability formed by the ratio of candidate marg.lik over current marg.lik. Over time, the sampler should thus converge to a sensible distribution. For aggregate results based on these MC3 frequencies, the first few iterations are typically disregarded (the 'burn-ins'). Ad g and the hyper-g prior: The hyper-g prior introduced by Liang et al. (2008) puts a prior distribution on the shrinkage factor g/(1+g), namely a Beta distribution Beta(1, 1/2 - 1) that is governed by the parameter a. a = 4 means a uniform prior distribution of the shrinkage factor, while a > 2 close to 2 concentrates the prior shrinkage factor close to one.

The prior expected value is E(g/1+g)) = 2/a. In this sense g="hyper=UIP" and g="hyper=BRIC" set the prior expected shrinkage such that it conforms to a fixed UIP-g (eqng=N) or BRIC-g ( $g = max(K^2, N)$ ).

### Value

A list of class bma, that may be displayed using e.g. summary.bma or coef.bma. The list contains the following elements:

info	a list of aggregate statistics: iter is the number of iterations, burn the number of burn-ins.
	The following have to be divided by cumsumweights to get posterior expected values: inccount are the posterior inclusion probabilities, b1mo and b2mo the
	first and second moment of coefficients, add.otherstats other statistics of in- terest (typically the moments of the shrinkage factor), msize is the post. ex- pected model size, k.vec the posterior model size distribution, pos.sign the unconditional post. probability of positive coefficients, corr.pmp is the correla- tion between the best models' MCMC frequencies and their marg. likelihoods. timed is the time that was needed for MCMC sampling, cons is the posterior expected value of the constant. K and N are the maximum number of covariates and the sample size, respectively.
arguments	a list of the evaluated function arguments provided to bms (see above)
topmod	a 'topmod' object containing the best drawn models. see topmod for more details
start.pos	the positions of the starting model. If bmao is a'bma' object this corresponds to covariates bmao\$reg.names[bmao\$start.pos]. If bmao is a chain that resulted from several starting models (cf. c.bma, then start.pos is a list detailing all of them.
gprior.info	a list of class gprior-class, detailing information on the g-prior: gtype corre- sponds to argument g above, is.constant is FALSE if gtype is either "hyper" or "EBL", return.g.stats corresponds to argument g.stats above, shrinkage.moments contains the first and second moments of the shrinkage factor (only if return.g.stats==TRUE), g details the fixed g (if is.constant==TRUE), hyper.parameter corresponds to the hyper-g parameter <i>a</i> as in Liang et al. (2008)
mprior.info	a list of class mprior-class, detailing information on the model prior: origargs lists the original arguments to mprior and mprior.size above; mp.msize denotes the prior mode size; mp.Kdist is a (K+1) vector with the prior model size distribution from 0 to K
X.data	data.frame or matrix: corresponds to argument X.data above, possibly cleaned for NAs
reg.names	character vector: the covariate names to be used for X.data (corresponds to variable.names.bma
bms.call	the original call to the bms function

#### **Theoretical background**

The models analyzed are Bayesian normal-gamma conjugate models with improper constant and variance priors akin to Fernandez, Ley and Steel (2001): A model M can be described as follows, with  $\epsilon \sim N(0, \sigma^2 I)$ :

#### latex

$$f(\beta|\sigma, M, g) N(0, g\sigma^2 (X'X)^{-1})$$

Moreover, the (improper) prior on the constant  $f(\alpha)$  is put proportional to 1. Similarly, the variance prior  $f(\sigma)$  is proportional to  $1/\sigma$ .

#### Note

There are several ways to speed-up sampling: nmodel=10 saves only the ten best models, at most a marginal improvement. nmodels=0 does not save the best (500) models, however then posterior convergence and likelihood-based inference are not possible. the best models, but not their coefficients, which renders the use of image.bma and the paramer exact=TRUE in functions such as coef.bma infeasible. g.stats=FALSE saves some time by not retaining the shrinkage factors for the MC3 chain (and the best models). force.fullobject=TRUE in contrast, slows sampling down significantly if mcmc=""

#### Author(s)

Martin Feldkircher, Paul Hofmarcher, and Stefan Zeugner

#### References

http://bms.zeugner.eu: BMS package homepage with help and tutorials

Feldkircher, M. and S. Zeugner (2015): Bayesian Model Averaging Employing Fixed and Flexible Priors: The BMS Package for R, Journal of Statistical Software 68(4).

Feldkircher, M. and S. Zeugner (2009): Benchmark Priors Revisited: On Adaptive Shrinkage and the Supermodel Effect in Bayesian Model Averaging, IMF Working Paper 09/202.

Fernandez, C. E. Ley and M. Steel (2001): Benchmark priors for Bayesian model averaging. Journal of Econometrics 100(2), 381–427

Ley, E. and M. Steel (2008): On the Effect of Prior Assumptions in Bayesian Model Averaging with Applications to Growth Regressions. working paper

Liang, F., Paulo, R., Molina, G., Clyde, M. A., and Berger, J. O. (2008). Mixtures of g Priors for Bayesian Variable Selection. Journal of the American Statistical Association 103, 410-423.

Sala-i-Martin, X. and G. Doppelhofer and R.I. Miller (2004): Determinants of long-term growth: a Bayesian averaging of classical estimates (BACE) approach. American Economic Review 94(4), 813–835

#### See Also

coef.bma, plotModelsize and density.bma for some operations on the resulting 'bma' object, c.bma for integrating separate MC3 chains and splitting of sampling over several runs.

Check http://bms.zeugner.eu for additional help.

#### c.bma

### Examples

```
data(datafls)
#estimating a standard MC3 chain with 1000 burn-ins and 2000 iterations and uniform model priors
bma1 = bms(datafls,burn=1000, iter=2000, mprior="uniform")
##standard coefficients based on exact likelihoods of the 100 best models:
coef(bma1,exact=TRUE, std.coefs=TRUE)
#suppressing user-interactive output, using a customized starting value, and not saving the best
# ...models for only 19 observations (but 41 covariates)
bma2 = bms(datafls[20:39,],burn=1000, iter=2000, nmodel=0, start.value=c(1,4,7,30),
   user.int=FALSE)
coef(bma2)
#MC3 chain with a hyper-g prior (custom coefficient a=2.1), saving only the 20 best models,
# ...and an alternative sampling procedure; putting a log entry to console every 1000th step
bma3 = bms(datafls,burn=1000, iter=5000, nmodel=20, g="hyper=2.1", mcmc="rev.jump",
    logfile="",logstep=1000)
image(bma3) #showing the coefficient signs of the 20 best models
#enumerating with 10 covariates (= 1024 models), keeping the shrinkage factors
# ... of the best 200 models
bma4 = bms(datafls[,1:11],mcmc="enumerate",nmodel=200,g.stats=TRUE)
#using an interaction sampler for two interaction terms
dataint=datafls
dataint=cbind(datafls,datafls$LifeExp*datafls$Abslat/1000,
      datafls$Protestants*datafls$Brit-datafls$Muslim)
names(dataint)[ncol(dataint)-1]="LifeExp#Abslat"
names(dataint)[ncol(dataint)]="Protestants#Brit#Muslim"
bma5 = bms(X.data=dataint,burn=1000,iter=9000,start.value=0,mcmc="bd.int")
density(bma5,reg="English") # plot posterior density for covariate "English"
# a matrix as X.data argument
bms(matrix(rnorm(1000),100,10))
# keeping a set of fixed regressors:
bms(datafls, mprior.size=7, fixed.reg = c("PrScEnroll", "LifeExp", "GDP60"))
# Note that mprior.size=7 means prior model size of 3 fixed to 4 'uncertain' regressors
```

c.bma

Concatenate bma objects

#### Description

Combines bma objects (resulting from bms). Can be used to split estimation over several machines, or combine the MCMC results obtained from different starting points.

### Usage

```
## S3 method for class 'bma'
c(..., recursive = FALSE)
```

### Arguments

	At least two 'bma' objects (cf. bms)
recursive	retained for compatibility with c method

#### Details

Aggregates the information obtained from several chains. The result is a 'bma' object (cf. 'Values' in bms) that can be used just as a standard 'bma' object.

Note that combine\_chains helps in particular to parallelize the enumeration of the total model space: A model with K regressors has  $2^{K}$  potential covariate combinations: With K large (more than 25), this can be pretty time intensive. With the bms arguments start.value and iter, sampling can be done in steps: cf. example 'enumeration' below.

### See Also

bms for creating bma objects

Check http://bms.zeugner.eu for additional help.

# Examples

data(datafls)

```
model_all=c(model1,model2)
coef(model_all)
plot(model_all)
```

#standard case with 12 covariates (4096 differnt combinations): enum0=bms(datafls[,1:13],mcmc="enumerate")

```
# now split the task:
# enum1 does everything from model zero (the first model) to model 1999
enum1=bms(datafls[,1:13],mcmc="enumerate",start.value=0,iter=1999)
```

# enum2 does models from index 2000 to the index 3000 (in total 1001 models)
enum2=bms(datafls[,1:13],mcmc="enumerate",start.value=2000,iter=1000)

# enum3 does models from index 3001 to the end

# 12

# datafls

```
enum3=bms(datafls[,1:13],mcmc="enumerate",start.value=3001)
enum_combi=c(enum1,enum2,enum3)
coef(enum_combi)
coef(enum0)
#both enum_combi and enum0 have exactly the same results
#(one difference: enum_combi has more 'top models' (1500 instead of 500))
```

datafls

#### FLS (2001) growth data

# Description

The economic growth data set from Fernandez, Ley and Steel, Journal of Applied Econometrics 2001

# Usage

datafls

#### Format

A data frame with 53940 rows and 10 variables: A data frame with 72 observations on the following 42 variables.

y numeric: Economic growth 1960-1992 as from the Penn World Tables Rev 6.0

Abslat numeric: Absolute latitude

Spanish numeric: Spanish colony dummy

French numeric: French colony dummy

Brit numeric: British colony dummy

WarDummy numeric: War dummy

LatAmerica numeric: Latin America dummy

SubSahara numeric; Sub-Sahara dummy

OutwarOr numeric: Outward Orientation

Area numeric: Area surface

PrScEnroll numeric: Primary school enrolment

LifeExp numeric: Life expectancy

GDP60 numeric: Initial GDP in 1960

Mining numeric: Fraction of GDP in mining

EcoOrg numeric: Degree of capitalism

Yrs0pen numeric: Number of years having an open economy

Age numeric: Age

#### datafls

Buddha numeric: Fraction Buddhist Catholic numeric: Fraction Catholic Confucian numeric: Fraction Confucian EthnoL numeric: Ethnolinguistic fractionalization Hindu numeric: Fraction Hindu Jewish numeric: Fraction Jewish Muslim numeric: Fraction Muslim PrExports numeric: Primary exports 1970 Protestants numeric: Fraction Protestants RuleofLaw numeric: Rule of law Popg numeric: Population growth WorkPop numeric: workers per inhabitant LabForce numeric: Size of labor force HighEnroll numeric: Higher education enrolment PublEdupct numeric: Public education share RevnCoup numeric: Revolutions and coups PolRights numeric: Political rights CivlLib numeric: Civil liberties English numeric: Fraction speaking English Foreign numeric: Fraction speaking foreign language RFEXDist numeric: Exchange rate distortions EquipInv numeric: Equipment investment NequipInv numeric: Non-equipment investment stdBMP numeric: stand. dev. of black market premium BlMktPm numeric: black market premium

#### Source

Fernandez, C., Ley, E., and Steel, M. F. (2001b). Model Uncertainty in Cross-Country Growth Regressions. Journal of Applied Econometrics, 16:563-576. Data set from https://warwick.ac.uk/fac/sci/statistics/staff/academic-research/steel/steel\_homepage/software.

A working paper version of Fernandez, Ley and Steel (2001) is available via https://econpapers.repec.org/article/jaejapmet/v\_3a16\_3ay\_3a2001\_3ai\_3a5\_3ap\_3a563-576.htm.

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density.bma

# Description

Calculates the mixture marginal posterior densities for the coefficients from a BMA object and plots them

# Usage

```
## S3 method for class 'bma'
density(
    x,
    reg = NULL,
    addons = "lemsz",
    std.coefs = FALSE,
    n = 300,
    plot = TRUE,
    hnbsteps = 30,
    addons.lwd = 1.5,
    ...
)
```

# Arguments

х	A bma object (see bms) or a zlm object.
reg	A scalar integer or character detailing which covariate's coefficient should be plotted. If reg=NULL (default), then all regressors are plotted one after the other, waiting for user interaction.
addons	character. Specifies which additional information should be added to the plot via low-level commands (see 'Details' below).
std.coefs	logical. If TRUE then the posterior density is estimated for standardized coefficients (representing the case where all variables have mean zero and standard deviation 1) - default is FALSE.
n	numeric. the number of equally spaced points at which the density is to be estimated.
plot	logical. If TRUE (default), the density is plotted; if FALSE then density.bma only returns the estimated posterior densities without plotting.
hnbsteps	even integer, default 30. The number of numerical integration steps to be used in case of a hyper-g prior (cf. argument g in bms). Increase this number to increase accuracy.
addons.lwd	scalar, default 1.5. Line width to be used for the low-level plotting commands specified by addons. Cf. argument lwd in par
	Additional arguments for plot.default with sensible defaults

#### Details

The argument addons specifies what additional information should be added to the plot(s) via the low-level commands lines and legend:

"e" for the posterior expected value (EV) of coefficients conditional on inclusion (see argument exact=TRUE in coef.bma),

"s" for 2 times posterior standard deviation (SD) bounds,

"m" for the posterior median,

"b" for posterior expected values of the individual models whom the density is averaged over,

"E" for posterior EV under MCMC frequencies (see argument exact=FALSE in coef.bma),

"S" for the corresponding SD bounds (MCMC),

"p" for plotting the Posterior Inclusion Probability above the density plot,

"1" for including a legend, "z" for a zero line, "g" for adding a grid

Any combination of these letters will give the desired result. Use addons="" for not using any of these.

In case of density.zlm, only the letters e, s, l, z, and g will have an effect.

#### Value

The function returns a list containing objects of the class density detailing the marginal posterior densities for each coefficient provided in reg.

In case of density.zlm, simple marginal posterior coefficient densities are computed, while density.bma calculates there mixtures over models according to posterior model probabilities.

These densities contain only the density points apart from the origin. (see 'Note' below)

As long as plot=TRUE, the densities are plotted too. Note that (for density.bma) if the posterior inclusion probability of a covariate is zero, then it will not be plotted, and the returned density will be list(x=numeric(n), y=numeric(n)).

#### Note

The computed marginal posterior densities from density.bma are a Bayesian Model Averaging mixture of the marginal posterior densities of the individual models. The accuracy of the result therefore depends on the number of 'best' models contained in x (cf. argument nmodel in bms).

The marginal posterior density can be interpreted as 'conditional on inclusion': If the posterior inclusion probability of a variable is smaller than one, then some of its posterior density is Dirac at zero. Therefore the integral of the returned density vector adds up to the posterior inclusion probability, i.e. the probability that the coefficient is not zero.

Correspondingly, the posterior EV and SD specified by addons="es" are based on 'best' model likelihoods ('exact') and are conditional on inclusion. They correspond to the results from command coef.bma(x,exact=TRUE,condi.coef=TRUE,order.by.pip=FALSE) (cf. the example below).

The low-level commands enacted by the argument addons rely on colors of the palette: color 2 for "e" and "s", color 3 for "m", color 8 for "b", color 4 for "E" and "S". The default colors may be changed by a call to palette.

Up to BMS version 0.3.0, density.bma may only cope with built-in gpriors, not with any userdefined priors.

### estimates.bma

#### See Also

quantile.coef.density for extracting quantiles, coef.bma for similar concepts, bms for creating bma objects

Check http://bms.zeugner.eu for additional help.

# Examples

```
data(datafls)
mm=bms(datafls)
density(mm,reg="SubSahara")
density(mm, reg=7, addons="lbz")
density(mm,1:9)
density(mm,reg=2,addons="zgSE",addons.lwd=2,std.coefs=TRUE)
# plot the posterior density only for the very best model
density(mm[1], reg=1, addons="esz")
#using the calculated density for other purposes...
dd=density(mm,reg="SubSahara")
plot(dd)
dd_list=density(mm,reg=1:3,plot=FALSE,n=400)
plot(dd_list[[1]])
#Note that the shown density is only the part that is not zero
dd=density(mm,reg="Abslat",addons="esl")
pip_Abslat=sum(dd$y)*diff(dd$x)[1]
#this pip and the EV conform to what is done by the follwing command
coef(mm,exact=TRUE,condi.coef=TRUE)["Abslat",]
```

estimates.bma

Posterior Inclusion Probabilities and Coefficients from a 'bma' Object

# Description

Returns a matrix with aggregate covariate-specific Bayesian model Averaging: posterior inclusion probabilites (PIP), post. expected values and standard deviations of coefficients, as well as sign probabilites

# Usage

```
estimates.bma(
 bmao,
  exact = FALSE,
 order.by.pip = TRUE,
 include.constant = FALSE,
  incl.possign = TRUE,
  std.coefs = FALSE,
 condi.coef = FALSE
)
## S3 method for class 'bma'
coef(
 object,
  exact = FALSE,
 order.by.pip = TRUE,
  include.constant = FALSE,
  incl.possign = TRUE,
  std.coefs = FALSE,
  condi.coef = FALSE,
  . . .
)
```

# Arguments

exact	if exact=FALSE, then PIPs, coefficients, etc. will be based on aggregate in- formation from the sampling chain with posterior model distributions based on MCMC frequencies (except in case of enumeration - cf. 'Details'); if exact=TRUE, estimates will be based on the nmodel best models encountered by the sampling chain, with the posterior model distribution based on their <i>exact</i> marginal likelihoods - cf. 'Details' below.	
order.by.pip	order.by.pip=TRUE orders the resulting matrix according to posterior inclusion probabilites, order.by.pip=FALSE ranks them according to the original data (order of the covariates as in provided in X.data to bms), default TRUE	
include.constant		
	If include.constant=TRUE then the resulting matrix includes the expected value of the constant in its last row. Default FALSE	
incl.possign	If incl.possign=FALSE, then the sign probabilites column (cf. 'Values' below) is omitted from the result. Default TRUE	
std.coefs	If std.coefs=TRUE then the expected values and standard deviations are re- turned in standardized form, i.e. as if the original data all had mean zero and variance 1. If std.coefs=FALSE (default) then both expected values and stan- dard deviations are returned 'as is'.	
condi.coef	If condi.coef=FALSE (default) then coefficients $\beta_i$ and standard deviations are unconditional posterior expected values, as in standard model averaging; if condi.coef=FALSE then they are given as conditional on inclusion (equivalent to $\beta_i/PIP_i$ ).	
object, bmao	a 'bma' object (cf. bms)	

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. . .

further arguments for other coef methods

#### Details

More on the argument exact:

In case the argument exact=TRUE, the PIPs, coefficient statistics and conditional sign probabilities are computed on the basis of the (500) best models the sampling chain encountered (cf. argument nmodel in bms). Here, the weights for Bayesian model averaging (BMA) are the posterior marginal likelihoods of these best models.

In case exact=FALSE, then these statistics are based on all accepted models (except burn-ins): If mcmc="enumerate" then this are simply all models of the traversed model space, with their marginal likelihoods providing the weights for BMA.

If, however, the bma object bmao was based on an MCMC sampler (e.g. when bms argument mcmc="bd"), then BMA statistics are computed differently: In contrast to above, the weights for BMA are MCMC frequencies, i.e. how often the respective models were encountered by the MCMC sampler. (cf. a comparison of MCMC frequencies and marginal likelihoods for the best models via the function pmp.bma).

#### Value

A matrix with five columns (or four if incl.possign=FALSE)

Column 'PIP' Posterior inclusion probabilities  $\sum p(\gamma|i \in \gamma, Y)/sump(\gamma|Y)$ 

Column 'Post Mean'

posterior expected value of coefficients, unconditional  $E(\beta|Y) = \sum p(\gamma|Y)E(\beta|\gamma, Y)$ , where  $E(\beta_i|\gamma, i \notin \gamma, Y) = 0$  if condi . coef=FALSE, or conditional on inclusion  $(E(\beta|Y) / \sum p(\gamma|Y, i \in \gamma))$  if condi . coef=TRUE

Column 'Post SD'

posterior standard deviation of coefficients, unconditional or conditional on inclusion, depending on condi.coef

Column 'Cond.Pos.Sign'

The ratio of how often the coefficients' expected values were positive conditional on inclusion. (over all visited models in case exact=FALSE, over the best models in case exact=TRUE)

Column 'Idx' the original order of covariates as the were used for sampling. (if included, the constant has index 0)

#### See Also

bms for creating bma objects, pmp. bma for comparing MCMC frequencies and marginal likelihoods.

Check http://bms.zeugner.eu for additional help.

#### Examples

#sample, with keeping the best 200 models: data(datafls) mm=bms(datafls,burn=1000,iter=5000,nmodel=200)

#standard BMA PIPs and coefficients from the MCMC sampling chain, based on

# f21hyper

# ...how frequently the models were drawn
coef(mm)

#standardized coefficients, ordered by index coef(mm,std.coefs=TRUE,order.by.pip=FALSE)

#coefficients conditional on inclusion: coef(mm,condi.coef=TRUE)

#same as
ests=coef(mm,condi.coef=FALSE)
ests[,2]/ests[,1]

#PIPs, coefficients, and signs based on the best 200 models
estimates.bma(mm,exact=TRUE)

#... and based on the 50 best models
coef(mm[1:50],exact=TRUE)

f21hyper

Gaussian Hypergeometric Function F(a,b,c,z)

#### Description

Computes the value of a Gaussian hypergeometric function F(a,b,c,z) for  $-1 \leq z \leq 1$  and  $a,b,c \geq 0$ 

# Usage

f21hyper(a, b, c, z)

# Arguments

а	The parameter a of the Gaussian hypergeometric function, must be a positive scalar here
b	The parameter b of the Gaussian hypergeometric function, must be a positive scalar here
С	The parameter c of the Gaussian hypergeometric function, must be a positive scalar here
Z	The parameter z of the Gaussian hypergeometric function, must be between -1 and 1 here

# Details

The function f21hyper complements the analysis of the 'hyper-g prior' introduced by Liang et al. (2008).

For parameter values, compare cf. https://en.wikipedia.org/wiki/Hypergeometric\_function.

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# fullmodel.ssq

# Value

The value of the Gaussian hypergeometric function F(a, b, c, z)

# Note

This function is a simple wrapper function of sped-up code that is intended for sporadic application by the user; it is neither efficient nor general; for a more general version cf. the package 'hypergeo'

# References

Liang F., Paulo R., Molina G., Clyde M., Berger J.(2008): Mixtures of g-priors for Bayesian variable selection. J. Am. Statist. Assoc. 103, p. 410-423

https://en.wikipedia.org/wiki/Hypergeometric\_function

# See Also

package hypergeo for a more proficient implementation.

Check http://bms.zeugner.eu for additional help.

# Examples

f21hyper(30,1,20,.8) #returns about 165.8197

f21hyper(30,10,20,0) #returns one

f21hyper(10,15,20,-0.1) # returns about 0.4872972

fullmodel.ssq OLS Statistics for the Full Model Including All Potential Covariates

# Description

A utility function for reference: Returns a list with R2 and sum of squares for the OLS model encompassing all potential covariates that are included in a bma object.

### Usage

```
fullmodel.ssq(yX.data)
```

#### Arguments

yX.data a bma object (cf. bms) - alternatively a data.frame or matrix whose first column is the dependent variable

# gdensity

# Value

Returns a list with some basic OLS statistics

R2	The R-squared of the full model
ymy	The sum of squares of residuals of the full model
уру	The explained sum of squares of the full model
yty	The sum of squares of the (demeaned) dependent variable
Fstat	The F-statistic of the full model

# Note

This function is just for quick comparison; for proper OLS estimation consider 1m

# See Also

bms for creating bma objects, 1m for OLS estimation Check http://bms.zeugner.eu for additional help.

# Examples

data(datafls)
mm=bms(datafls)
fullmodel.ssq(mm)
#equivalent:
fullmodel.ssq(datafls)

gdensity

Posterior Density of the Shrinkage Factor

# Description

Calculates the mixture marginal posterior density for the shrinkage factor (g/(1+g)) from a BMA object under the hyper-g prior and plots it

# Usage

```
gdensity(x, n = 512, plot = TRUE, addons = "zles", addons.lwd = 1.5, ...)
```

#### gdensity

#### Arguments

x	A bma object (see bms).
n	The integer number of equally spaced points at which the density is to be esti- mated. see 'Details' below
plot	logical. If TRUE (default), the density is plotted; if FALSE then gdensity only returns the estimated posterior density without plotting.
addons	character, defaulting to "zles". Specifies which additional information should be added to the plot via low-level commands (see 'Details' below).
addons.lwd	scalar, default 1.5. Line width to be used for the low-level plotting commands specified by addons. Cf. argument 1wd in par
	Additional arguments for plot.default with sensible defaults

#### Details

The function gdensity estimates and plots the posterior density for the shrinkage factor g/(1+g)This is evidently only possible if the shrinkage factor if not fixed, i.e. if the bma object x was estimated with a hyper-g prior - cf. argument g in bms

The density is based only on the best models retained in the bma object x, cf. argument nmodel in bms

A note on argument n: The points at which the density is estimated start at max(0, E - 5 \* SD), where E and SD are the expected value and standard deviation of the shrinkage factor, respectively. For plotting the entire domain (0, 1) use xlim=c(0, 1) as an argument for gdensity.

The argument addons specifies what additional information should be added to the plot(s) via the low-level commands lines and legend:

"e" for the posterior expected value (EV) of the shrinkage factor,

"s" for 2 times posterior standard deviation (SD) bounds,

"m" for the posterior median,

"f" for posterior expected values of the individual models whom the density is averaged over,

"z" for a zero line, "1" for including a legend

The following two are only possible if the bma object collected statistics on shrinkage, cf. argument g.stats in bms "E" for posterior expected value under MCMC frequencies (see argument exact in coef.bma),

"S" for the corresponding 2 times standard deviation bounds (MCMC),

Any combination of these letters will give the desired result. Use addons="" for not using any of these.

#### Value

gdensity returns an object of the class density detailing the posterior mixture density of the shrinkage factor.

#### Note

The computed marginal posterior density is a Bayesian Model Averaging mixture of the marginal posterior densities of the shrinkage factor under individual models. The accuracy of the result therefore depends on the number of 'best' models contained in x (cf. argument nmodel in bms).

Correspondingly, the posterior EV and SD specified by addons="es" are based on 'best' model likelihoods ('exact') and are conditional on inclusion.

The low-level commands enacted by the argument addons rely on colors of the palette: color 2 for "e" and "s", color 3 for "m", color 8 for "f", color 4 for "E" and "S". The default colors may be changed by a call to palette.

#### See Also

density.bma for computing coefficient densities, bms for creating bma objects, density for the general method

Check http://bms.zeugner.eu for additional help.

#### Examples

```
data(datafls)
mm=bms(datafls,g="hyper=UIP")
gdensity(mm) # default plotting
# the grey bars represent expected shrinkage factors of the individual models
gdensity(mm,addons="lzfes")
# #plotting the median 'm' and the posterior mean and bounds based on MCMC results:
gdensity(mm,addons="zSEm",addons.lwd=2)
# plot the posterior shrinkage density only for the very best model
gdensity(mm[1],addons="esz")
#using the calculated density for other purposes...
dd=gdensity(mm,plot=FALSE)
plot(dd)
```

gprior-class Class "gprior"

#### Description

An object pertaining to a coefficient prior

#### **Objects from the Class**

A gprior object holds descriptions and subfunctions pertaining to coefficient priors. Functions such as bms or zlm rely on this class to 'convert' the output of OLS results into posterior expressions for a Bayesian Linear Model. Post-processing functions such as density.bma also resort to gprior objects.

# hex2bin

There are currently three coefficient prior structures built into the BMS package, generated by the following functions (cf. Feldkircher and Zeugner, 2009) : gprior.constg.init: creates a Zellner's g-prior object with constant g. gprior.eblocal.init: creates an Empricial Bayes Zellner's g-prior. gprior.hyperg.init: creates a hyper g-prior with a Beta-prior on the shrinkage parameter. The following describes the necessary slots

# Author(s)

Martin Feldkircher and Stefan Zeugner

### References

Feldkircher, M. and S. Zeugner (2009): Benchmark Priors Revisited: On Adaptive Shrinkage and the Supermodel Effect in Bayesian Model Averaging, IMF Working Paper 09/202.

# See Also

bms and zlm for creating bma or zlm objects. Check the appendix of vignette(BMS) for a more detailed description of built-in priors. Check http://bms.zeugner.eu/custompriors.php for examples.

#### Examples

```
data(datafls)
mm1=bms(datafls[,1:10], g="EBL")
gg=mm1$gprior.info # is the g-prior object, augmented with some posterior statistics
mm2=bms(datafls[,1:10], g=gg) #produces the same result
mm3=bms(datafls[,1:10], g=BMS:::.gprior.eblocal.init)
#this passes BMS's internal Empirical Bayes g-prior object as the coefficient prior
# - any other obejct might be used as well
```

hex2bin

Converting Binary Code to and from Hexadecimal Code

#### Description

A simple-to-use function for converting a logical ('binary') vector into hex code and reverse.

#### Usage

hex2bin(hexcode)

bin2hex(binvec)

#### Arguments

hexcode	a single-element character denoting an integer in hexcode (admissible character: 0 to 9, ato f)
binvec	a logical vector (alternatively a vector coercible into logical)

# Details

The argument is an integer in binary form (such as "101"), provided as a logical (c(T,F,T)) or numeric vector (c(1,0,1)).

bin2hex then returns a character denoting this number in hexcode (in this case "5").

The function hex2bin does the reverse operation, e.g. hex2bin("5") gives (c(1,0,1)).

# Value

bin2hex returns a single element character; hex2bin returns a numeric vector equivalent to a logical vector

# See Also

hex2bin for converting hexcode into binary vectors, format.hexmode for a related R function.

Check http://bms.zeugner.eu for additional help.

# Examples

```
bin2hex(c(TRUE,FALSE,TRUE,FALSE,TRUE,TRUE))
bin2hex(c(1,0,1,0,1,1))
hex2bin("b8a")
bin2hex(hex2bin("b8a"))
```

image.bma

Plot Signs of Best Models

# Description

Plots a grid with signs and inclusion of coefficients vs. posterior model probabilities for the best models in a 'bma' object:

### Usage

```
## S3 method for class 'bma'
image(
    x,
    yprop2pip = FALSE,
    order.by.pip = TRUE,
    do.par = TRUE,
    do.grid = TRUE,
```

# image.bma

```
do.axis = TRUE,
cex.axis = 1,
...
```

# Arguments

)

х	a list of class bma (cf. bms for further details)
yprop2pip	if yprop2pip=TRUE then the grid lines on the vertical axis are scaled according to the coefficients' inclusion probabilites. If yprop2pip=FALSE (default) then the grid lines on the vertical axis are equidis- tant.
order.by.pip	with order.by.pip=TRUE (default), coefficients are sorted according to their posterior inclusion probabilites along the vertical axis. If order.by.pip=FALSE they are ordered as they were provided to bms.
do.par	Defaults to do.par=TRUE, which adjusts par()\$mar for optimal positioning. Set do.par=FALSE for customizing par yourself.
do.grid	do.grid=TRUE (default) plots grid lines among the chart's boxes, akin to the low level command grid. do.grid=FALSE omits the grid lines.
do.axis	do.axis=TRUE (default) plots axis tick marks and labels (cf. axis). do.axis=FALSE omits them.
cex.axis	font size for the axes (cf. axis), defaults to 1
	Parameters to be passed on to image.default.

# Details

Under default settings, blue corresponds to positive sign, red to a negative sign, white to non-inclusion.

# See Also

coef.bma for the coefficients in matrix form, bms for creating 'bma' objects.

Check <a href="http://bms.zeugner.eu">http://bms.zeugner.eu</a> for additional help.

# Examples

```
data(datafls)
```

model=bms(datafls,nmodel=200)

```
#plot all models
image(model,order.by.pip=FALSE)
image(model,order.by.pip=TRUE,cex.axis=.8)
```

```
#plot best 7 models, with other colors
image(model[1:7],yprop2pip=TRUE,col=c("black","lightgrey"))
```

info.bma

# Description

Returns a vector with summary statistics for a 'bma' object

# Usage

```
info.bma(bmao)
```

```
## S3 method for class 'bma'
summary(object, ...)
```

# Arguments

bmao	same as object
object	a list/object of class 'bma' that typically results from the function bms (see bms for details)
	further arguments passed to or from other methods

# Details

info.bma is equivalent to summary.bma, its argument bmao conforms to the argument object

# Value

A character vector summarizing the results of a call to bms

Mean no. of Regre	essors	
	the posterior mean of model size	
Draws	the number of iterations (ex burn-ins)	
Burnins	the number of burn-in iterations	
Time	the time spent on iterating through the model space	
No. of models vis	sited	
	the number of times a model was accepted (including burn-ins)	
Modelspace	the total model space $2^K$	
<pre>list(list("2^K"))</pre>		
	the total model space $2^K$	
Percentage visit	ed	
	No. of models visited/Modelspace*100	
Percentage Topmo	odels	
	number of times the best models were drawn in percent of Draws	
Corr.PMP	the correlation between the MCMC frequencies of the best models (the number of times they were drawn) and their marginal likelihoods.	

# is.bma

No.Obs.	Number of observations	
Model Prior	a character conforming to the argument mprior of bms, and the expected prior model size	
g-prior	a character corresponding to argument g of function bms	
Shrinkage-Stats		
	Posterior expected value und standard deviation (if applicable) of the shrinkage factor. Only included if argument g.stats of function bms was set to TRUE	

# Note

All of the above statistics can also be directly extracted from the bma object (bmao). Therefore summary.bma only returns a character vector.

# See Also

bms and c.bma for functions creating bma objects, print.bma makes use of summary.bma.

Check <a href="http://bms.zeugner.eu">http://bms.zeugner.eu</a> for additional help.

# Examples

data(datafls)

```
m_fixed=bms(datafls,burn=1000,iter=3000,user.int=FALSE, )
summary(m_fixed)
```

```
m_ebl=bms(datafls,burn=1000,iter=3000,user.int=FALSE, g="EBL",g.stats=TRUE)
info.bma(m_ebl)
```

is.bma

Tests for a 'bma' Object

### Description

tests for objects of class "bma"

#### Usage

is.bma(bmao)

# Arguments

bmao a 'bma' object: see 'value'

# Value

Returns TRUE if bmao is of class 'bma', FALSE otherwise.

### See Also

'Output' in bms for the structure of a 'bma' object

Check http://bms.zeugner.eu for additional help.

# Examples

data(datafls)
mm=bms(datafls,burn=1000, iter=4000)
is.bma(mm)

lps.bma

Log Predictive Score

# Description

Computes the Log Predictive Score to evaluate a forecast based on a bma object

#### Usage

lps.bma(object, realized.y, newdata = NULL)

#### Arguments

object	an object of class pred.density, or class bma (cf. bms), or class zlm
realized.y	a vector with realized values of the dependent variables to be plotted in addition to the predictive density, must have its length conforming to newdata
newdata	Needs to be provided if object is not of class pred.density: a data.frame, matrix or vector containing variables with which to predict.

# Details

The log predictive score is an indicator for the likelihood of several forecasts. It is defined as minus the arithmethic mean of the logarithms of the point densities for realized.y

given newdata.

Note that in most cases is more efficient to first compute the predictive density object via a call to pred.density and only then pass the result on to lps.bma.

# Value

A scalar denoting the log predictive score

#### See Also

pred.density for constructing predictive densities, bms for creating bma objects, density.bma for
plotting coefficient densities

Check http://bms.zeugner.eu for additional help.

#### mprior-class

# Examples

```
data(datafls)
mm=bms(datafls,user.int=FALSE,nmodel=100)
#LPS for actual values under the used data (static forecast)
lps.bma(mm, realized.y=datafls[,1] , newdata=datafls[,-1])
#the same result via predicitve.density
pd=pred.density(mm, newdata=datafls[,-1])
lps.bma(pd,realized.y=datafls[,1])
# similarly for a linear model (not BMA)
zz = zlm(datafls)
lps.bma(zz, realized.y=datafls[,1] , newdata=datafls[,-1])
```

mprior-class Class "mprior"

#### Description

An object pertaining to a BMA model prior

#### **Objects from the Class**

An mprior object holds descriptions and subfunctions pertaining to model priors. The BMA functions bms and post-processing functions rely on this class.

There are currently five model prior structures built into the BMS package, generated by the following functions (cf. the appendix of vignette(BMS)):

mprior.uniform.init: creates a uniform model prior object.

mprior.fixedt.init: creates the popular binomial model prior object with common inclusion probabilities.

mprior.randomt.init: creates a beta-binomial model prior object.

mprior.pip.init: creates a binomial model prior object that allows for defining individual prior inclusion probabilities.

mprior.customk.init: creates a model prior object that allows for defining a custom prior for each model parameter size.

The following describes the necessary slots:

#### Author(s)

Martin Feldkircher and Stefan Zeugner

#### See Also

bms for creating bma objects.

Check the appendix of vignette(BMS) for a more detailed description of built-in priors. Check http://bms.zeugner.eu/custompriors.php for examples. plot.bma

# Description

Produces a combined plot: upper row shows prior and posterior model size distribution, lower row shows posterior model probabilities for the best models

#### Usage

## S3 method for class 'bma'
plot(x, ...)

#### Arguments

х	an object of class 'bma'
	additional arguments for matplot

#### Value

combines the plotting functions plotModelsize and plotConv

#### Note

The upper plot shows the prior and posterior distribution of model sizes (plotModelsize). The lower plot is an indicator of how well the bma object has converged (plotConv). and Paul

# See Also

plotModelsize and plotConv

Check http://bms.zeugner.eu for additional help.

#### Examples

```
data(datafls)
mm=bms(datafls,user.int=FALSE)
```

plot(mm)

plotComp

# Description

Plots a comparison of posterior inclusion probabilites, coefficients or their standard deviation between various bma objects

# Usage

```
plotComp(
   ...,
   varNr = NULL,
   comp = "PIP",
   exact = FALSE,
   include.legend = TRUE,
   add.grid = TRUE,
   do.par = TRUE,
   cex.xaxis = 0.8
)
```

# Arguments

	one or more objects of class 'bma' to be compared. plotComp passes on any other parameters in{} to matplot.
varNr	optionally, covariate indices to be included in the plot, can be either integer vector or character vector - see examples
comp	a character denoting what should be compared: comp="PIP" (default) for pos- terior inclusion probabilities, comp="Post Mean" for coefficients, comp="Post SD" for their standard deviations, comp="Std Mean" or standardized coefficients, or comp="Std SD" for standardized standard deviations
exact	if FALSE, the statistics to be compared are based on aggregate bma statistics, if TRUE, they are based solely on the best models retained in the bma objects
include.legend	whether to include a default legend in the plot (custom legends can be added with the command legend)
add.grid	whether to add a grid to the plot
do.par	whether to adjust par("mar") in order to fit in the tick labels on the x-axis
cex.xaxis	font size scaling parameter for the x-axis - cf. argument cex.axis in par

# See Also

coef.bma for the underlying function

Check http://bms.zeugner.eu for additional help.

# Examples

```
## sample two simple bma objects
data(datafls)
mm1=bms(datafls[,1:15])
mm2=bms(datafls[,1:15])
#compare PIPs
plotComp(mm1,mm2)
#compare standardized coefficeitns
plotComp(mm1,mm2,comp="Std Mean")
#...based on the lieklihoods of best models
plotComp(mm1,mm2,comp="Std Mean",exact=TRUE)
#plot only PIPs for first four covariates
plotComp(mm1,mm2,varNr=1:4, col=c("black","red"))
#plot only coefficients for covariates 'GDP60 ' and 'LifeExp'
plotComp(mm1,mm2,varNr=c("GDP60", "LifeExp"),comp="Post Mean")
```

plotConv

#### Plot Convergence of BMA Sampler

# Description

Plots the posterior model probabilites based on 1) marginal likelihoods and 2) MCMC frequencies for the best models in a 'bma' object and details the sampler's convergence by their correlation

# Usage

```
plotConv(bmao, include.legend = TRUE, add.grid = TRUE, ...)
```

# Arguments

bmao	an object of class 'bma' - see bms
include.legend	whether to include a legend in the plot
add.grid	whether to include a grid in the plot
	other parameters for matplot

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# plotModelsize

#### Details

A call to bms with a MCMC sampler (e.g. bms(datafls,mcmc="bd",nmodel=100) uses a Metropolis-Hastings algorithm to sample through the model space: the frequency of how often models are drawn converges to the distribution of their posterior marginal likelihoods.

While sampling, each 'bma' object stores the best models encountered by its sampling chain with their marginal likelihood and their MCMC frequencies.

plotConv compares the MCMC frequencies to marginal likelihoods, and thus visualizes how well the sampler has converged.

#### Note

```
plotConv is also used by plot.bma
```

#### See Also

pmp.bma for posterior model probabilites based on the two concepts, bms for creating objects of class 'bma'

Check http://bms.zeugner.eu for additional help.

# Examples

```
data(datafls)
mm=bms(datafls[,1:12],user.int=FALSE)
```

plotConv(mm)

```
#is similar to
matplot(pmp.bma(mm),type="1")
```

plotModelsize Plot Model Size Distribution

#### Description

Plots posterior and prior model size distribution

# Usage

```
plotModelsize(
    bmao,
    exact = FALSE,
    ksubset = NULL,
    include.legend = TRUE,
    do.grid = TRUE,
    ...
)
```

#### Arguments

bmao	a 'bma' object (cf. bms)
exact	if TRUE, then the posterior model distribution is based on the best models of bmao and their marginal likelihoods; if FALSE (default) then the distribution is based on all encountered models and their MCMC frequencies (cf. 'Details' in coef.bma)
ksubset	integer vector detailing for which model sizes the plot should be done
include.legend	if TRUE, a small legend is included via the low-level command legend
do.grid	if TRUE, a grid is added to the plot (with a simple grid()).
	parameters passed on to matplot with sensible defaults

# Value

As a default, plotModelsize plots the posterior model size distribution as a blue line, and the prior model distribution as a dashed red line.

In addition, it returns a list with the following elements:

mean	The posterior expected value of model size
var	The variance of the posterior model size distribution
dens	A vector detailing the posterior model size distribution from model size 0 (the first element) to $K$ (the last element)

# See Also

See also bms, image.bma, density.bma, plotConv Check http://bms.zeugner.eu for additional help.

# Examples

```
data(datafls)
mm=bms(datafls,burn=1500, iter=5000, nmodel=200,mprior="fixed",mprior.size=6)
#plot Nb.1 based on aggregate results
postdist= plotModelsize(mm)
#plot based only on 30 best models
plotModelsize(mm[1:30],exact=TRUE,include.legend=FALSE)
#plot based on all best models, but showing distribution only for model sizes 1 to 20
plotModelsize(mm,exact=TRUE,ksubset=1:20)
# create a plot similar to plot Nb. 1
plot(postdist$dens,type="1")
lines(mm$mprior.info$mp.Kdist)
```
pmp.bma

#### Description

Returns the posterior model probabilites for the best models encountered by a 'bma' object

# Usage

pmp.bma(bmao, oldstyle = FALSE)

#### Arguments

bmao	A bma object (see argument nmodel in bms), alternatively an object of class topmod
oldstyle	For normal use, leave this at FALSE. It is an argument for compatibility with older BMS versions - see section 'Notes'

#### Details

A call to bms with an MCMC sampler (e.g. bms(datafls,mcmc="bd",nmodel=100) uses a Metropolis-Hastings algorithm to sample through the model space - and the frequency of how often models are drawn converges to the distribution of their posterior marginal likelihoods. While sampling, each 'bma' object stores the best models encountered by its sampling chain with their marginal likelihood and their MCMC frequencies.

pmp.bma then allows for comparing the posterior model probabilities (PMPs) for the two different methods, similar to plotConv. It calculates the PMPs based on marginal likelihoods (first column) and the PMPs based on MCMC frequencies (second column) for the best x models stored in the bma object.

The correlation of the two columns is an indicator of how well the MCMC sampler has converged to the actual PMP distribution - it is therefore also given in the output of summary.bma.

The second column is slightly different in case the bms argument mcmc was set to mcmc="enumeration": In this case, the second column is also based on marginal likelihoods. The correlation between the two columns is therefore one.

# Value

the result is a matrix, its row names describe the model binaries There are two columns in the matrix:

PMP (Exact)	posterior model probabilities based on the posterior likelihoods of the best mod- els in bmao
PMP (MCMC)	posterior model probabilities of the best models in bmao based on their MCMC frequencies, relative to all models encountered by bmao - see 'Details'

The second column thus shows the PMPs of the best models relative to all models the call to bms has sampled through (therefore typically the second column adds up to less than one). The first column relates to the likelihoods of the best models, therefore it would add up to 1. In order estimate for their marginal likelihoods with respect to the other models (the ones not retained in the best models), these PMP aadding up to one are multiplied with the sum of PMP of the best models accroding to MCMC frequencies. Therefore, the two columns have the same column sum.

CAUTION: In package versions up to BMS 0.2.5, the first column was indeed set always equal to one. This behaviour can still be mimicked by setting oldstyle=TRUE.

#### See Also

plotConv for plotting pmp.bma, pmpmodel to obtain the PMP for any individual model, bms for sampling bma objects

Check http://bms.zeugner.eu for additional help.

# Examples

```
## sample BMA for growth dataset, MCMC sampler
data(datafls)
mm=bms(datafls[,1:10],nmodel=20, mcmc="bd")
```

## mmodel likelihoods and MCMC frequencies of best 20 models
print(mm\$topmod)

```
pmp.bma(mm)
#first column: posterior model prob based on model likelihoods,
# relative to best models in 'mm'
#second column: posterior model prob based MCMC frequencies,
# relative to all models encountered by 'mm'
```

```
#consequently, first column adds up to one
#second column shows how much of the sampled model space is
# contained in the best models
colSums(pmp.bma(mm))
```

```
#correlation betwwen the two shows how well the sampler converged
cor(pmp.bma(mm)[,1],pmp.bma(mm)[,2])
```

```
#is the same as given in summary.bma
summary(mm)["Corr PMP"]
```

#plot the two model probabilites
plotConv(mm)

```
#equivalent to the following chart
plot(pmp.bma(mm)[,2], type="s")
lines(pmp.bma(mm)[,1],col=2)
```

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# Note

# pmpmodel

```
#moreover, note how the first column is constructed
liks=exp(mm$top$lik())
liks/sum(liks)
pmp.bma(mm)[,1] #these two are equivalent
```

#the example above does not converge well, #too few iterations and best models # this is already better, but also not good mm=bms(datafls[,1:10],burn=2000,iter=5000,nmodel=200)

```
# in case the sampler has been 'enumeration' instead of MCMC,
# then both matrix columns are of course equivalent
mm=bms(datafls[,1:10],nmodel=512,mcmc="enumeration")
cor(pmp.bma(mm)[,1],pmp.bma(mm)[,2])
colSums(pmp.bma(mm))
```

pmpmodel

## Description

Returns the posterior model probability for any model based on bma results

#### Usage

pmpmodel(bmao, model = numeric(0), exact = TRUE)

# Arguments

bmao	A bma object as created by bms.
model	A model index - either variable names, or a logical with model binaries, or the model hexcode (cf. hex2bin, or a numeric with positions of the variables to be included.
exact	If TRUE, then the resulting PMP is based on analytical model likelihoods (works for any model). If FALSE, the the resulting PMP is derived from MCMC frequencies (works only for the null and fullmodel, as well as for models contained in bmao's topmod object. If bmao is based on enumeration (cf. argument mcmc in bms, then exact does not matter.

# Details

If the model as provided in model is the null or the full model, or is contained in bmao's topmod object (cf. argument nmodel in bms),

then the result is the same as in pmp.bma.

If not and exact=TRUE, then pmpmodel estimates the model based on comparing its marginal likelihood (times model prior) to the likelihoods in the topmod object and multiplying by their sum of PMP according to MCMC frequencies,

# Value

A scalar with (an estimate of) the posterior model probability for model

#### See Also

pmp.bma for similar functions

Check http://bms.zeugner.eu for additional help.

# Examples

```
## sample BMA for growth dataset, enumeration sampler
data(datafls)
mm=bms(datafls[,1:10],nmodel=5)
#show the best 5 models:
pmp.bma(mm)
#first column: posterior model prob based on model likelihoods,
#second column: posterior model prob based MCMC frequencies,
### Different ways to get the same result: #########
#PMP of 2nd-best model (hex-code representation)
pmpmodel(mm,"00c")
#PMP of 2nd-best model (binary representation)
incls=as.logical(beta.draws.bma(mm)[,2])
pmpmodel(mm,incls)
#PMP of 2nd-best model (via variable names)
#names of regressors in model "00c":
names(datafls[,2:10])[incls]
pmpmodel(mm,c("SubSahara", "LatAmerica"))
#PMP of 2nd-best model (via positions)
pmpmodel(mm,c(6,7))
####PMP of another model #########
pmpmodel(mm,1:5)
```

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post.var

# Description

Returns posterior residual variance, deviance, or pseudo R-squared, according to the chosen prior structure

# Usage

```
post.var(object, exact = FALSE, ...)
```

## Arguments

object	A bma object (as produced by bms) or a zlm object.
exact	When exact=FALSE, then deviance will be based on MCMC frequencies, if exact=TRUE then it will be based on analytical posterior model probabilities - cf. argument exact in coef.bma.
	further arguments passed to or from other methods

# Details

post.var: Posterior residual variance as according to the prior definitions contained in object post.pr2: A pseudo-R-squared corresponding to unity minus posterior variance over dependent variance.

deviance.bma: returns the deviance of a bma model as returned from bms. deviance.zlm: returns the deviance of a zlm model.

#### See Also

bms for creating bma objects and priors, zlm object.

Check http://bms.zeugner.eu for additional help.

# Examples

```
data(datafls)
```

```
mm=bms(datafls[,1:10])
deviance(mm)/nrow(datafls) # is equivalent to
post.var(mm)
```

```
post.pr2(mm) # is equivalent to
1 - post.var(mm) / ( var(datafls[,1])*(1-1/nrow(datafls)) )
```

pred.density

# Description

Predictive densities for conditional forecasts

# Usage

```
pred.density(object, newdata = NULL, n = 300, hnbsteps = 30, ...)
```

# Arguments

object	a bma object - see bms, alternativel a zlm object
newdata	A data frame, matrix or vector containing variables with which to predict.
n	The integer number of equally spaced points at which the density is to be esti- mated.
hnbsteps	The number of numerical integration steps to be used in case of a hyper-g prior (cf. argument g in bms). Increase this number to increase accuracy. Must be an even integer.
	arguments to be passed on to plot.density.

# Details

The predictive density is a mixture density based on the nmodels best models in a bma object (cf. nmodel in bms).

The number of 'best models' to retain is therefore vital and should be set quite high for accuracy.

## Value

pred.density returns a list of class pred.density with the following elements

<pre>densities()</pre>	a list whose elements each contain the estimated density for each forecasted observation
fit	a vector with the expected values of the predictions (the 'point forecasts')
std.err	a vector with the standard deviations of the predictions (the 'standard errors')
dyf(realized.y,predict_index=NULL)	
	Returns the densities of realized response variables provided in realized.y.
	If realized.y is a matrix, then each row corresponds to a forecast observation
	in newdata
	if not left empty, predict.index specifies to which observations in newdata the
	realized.y should apply
lps(realized.y,predict_index=NULL)	
	Computes the log predictive score for the response varaible provided in realized.y
	(cf. lps.bma) -
	Note that the LPS equals minus the mean of the logarithmized results from dyf)

# pred.density

<pre>plot((x, pred</pre>	<pre>ict_index = NULL, addons = "eslz", realized.y = NULL,</pre>	
addons.lwd = 1.5,)		
	the same as plot.pred.density	
n	The number of equally spaced points for which the density (under densities() was computed.	
nmodel	The number of best models predictive densities are based upon.	
call	the call that created this pred.density object	

# Note

In BMS version 0.3.0, pred.density may only cope with built-in gpriors, not with any userdefined priors.

#### See Also

predict.bma for simple point forecasts, plot.pred.density for plotting predictive densities, lps.bma for calculating the log predictive score independently, quantile.pred.density for extracting quantiles

Check http://bms.zeugner.eu for additional help.

# Examples

data(datafls)
mm=bms(datafls,user.int=FALSE)

#predictive densityfor two 'new' data points
pd=pred.density(mm,newdata=datafls[1:2,])

#fitted values based on best models, same as predict(mm, exact=TRUE)
pd\$fit

#plot the density for the first forecast observation
plot(pd,1)

# the same plot ' naked'
plot(pd\$densities()[[1]])

#predict density for the first forecast observation if the dep. variable is 0 pd\$dyf(0,1)

#predict densities for both forecasts for the realizations 0 and 0.5 pd\$dyf(rbind(c(0,.5),c(0,.5)))

# calc. Log Predictive Score if both forecasts are realized at 0: lps.bma(pd,c(0,0))

predict.bma

# Description

Expected value of prediction based on 'bma' object

#### Usage

```
## S3 method for class 'bma'
predict(object, newdata = NULL, exact = FALSE, topmodels = NULL, ...)
```

#### Arguments

object	a bma object - see bms
newdata	An optional data frame, matrix or vector containing variables with which to pre- dict. If omitted, then (the expected values of) the fitted values are returned.
exact	If FALSE (default), then prediction is based on all models (i.e. on their MCMC frequencies in case the bms parameter mcmc was set to an mcmc sampler. If TRUE, then prediction is based on analytical likelihoods of the best models retained in object - cf. bms parameter nmodel.
topmodels	index of the models with whom to predict: for instance, topmodels=1 predicts based solely on the best model, whereas topmodels=1:5 predicts based on a combination of the five best models. Note that setting topmodels triggers exact=TRUE. further arguments passed to or from other methods.

# Value

A vector with (expected values of) fitted values.

# See Also

coef.bma for obtaining coefficients, bms for creating bma objects, predict.lm for a comparable
function

Check <a href="http://bms.zeugner.eu">http://bms.zeugner.eu</a> for additional help.

# Examples

```
data(datafls)
mm=bms(datafls,user.int=FALSE)
predict(mm) #fitted values based on MCM frequencies
predict(mm, exact=TRUE) #fitted values based on best models
predict(mm, newdata=1:41) #prediction based on MCMC frequencies
```

# predict.zlm

```
predict(mm, newdata=datafls[1,], exact=TRUE) #prediction based on a data.frame
# the following two are equivalent:
predict(mm, topmodels=1:10)
predict(mm[1:10], exact=TRUE)
```

```
predict.zlm
```

Predict Method for zlm Linear Model

# Description

Expected value (And standard errors) of predictions based on 'zlm' linear Bayesian model under Zellner's g prior

# Usage

```
## S3 method for class 'zlm'
predict(object, newdata = NULL, se.fit = FALSE, ...)
```

# Arguments

object	a zlm linear model object - see zlm
newdata	An optional data.frame, matrix or vector containing variables with which to pre- dict. If omitted, then (the expected values of) the fitted values are returned.
se.fit	A switch indicating if the standard deviations for the predicted varaibles are required.
	further arguments passed to or from other methods.

# Value

A vector with (expected values of) fitted values.

If se.fit is TRUE, then the output is a list with the following elements:

fit	a vector with the expected values of fitted values
std.err	a vector with the standard deviations of fitted values
se.fit	a vector with the standard errors without the residual scale akin to se.fit in ${\tt predict.lm}$
residual.scale	The part from the standard deviations that involves the identity matrix. Note that sqrt(se.fit^2+residual.scale^2) yields std.err.

## See Also

bms for creating zlm objects, predict.lm for a comparable function, predict.bma for predicting with bma objects

Check <a href="http://bms.zeugner.eu">http://bms.zeugner.eu</a> for additional help.

# Examples

```
data(datafls)
mm=zlm(datafls,g="EBL")
predict(mm) #fitted values
predict(mm, newdata=1:41) #prediction based on a 'new data point'
#prediction based on a 'new data point', with 'standard errors'
predict(mm, newdata=datafls[1,], se.fit=TRUE)
```

# Description

Print method for objects of class 'topmod', typically the best models stored in a 'bma' object

# Usage

```
## S3 method for class 'topmod'
print(x, ...)
```

# Arguments

х	an object of class 'topmod' - see topmod
	additional arguments passed to link{print}

# Details

See pmp.bma for an explanation of likelihood vs. MCMC frequency concepts

#### Value

if x contains more than one model, then the function returns a 2-column matrix:

Row Names show the model binaries in hexcode Column 'Marg.Log.Lik' shows the marginal log-likelihoods of the models in x Column 'MCMC Freq' shows the MCMC frequencies of the models in x if x contains only one model, then more detailed information is shown for this model:

first line 'Model Index' provides the model binary in hexcode, 'Marg.Log.Lik' its marginal log likelhood, 'Sampled Freq.' how often it was accepted (function ncount() in topmod)

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# quantile.density

Estimates	first column: covariate indices included in the model, second column: posterior
	expected value of the coefficients, third column: their posterior standard devia-
	tions (excluded if no coefficients were stored in the topmod object - cf. argument
	bbeta in topmod)
Included Covari	ates

the model binary

Additional Statistics

any custom additional statistics saved with the model

# See Also

topmod for creating topmod objects, bms for their typical use, pmp.bma for comparing posterior model probabilities

Check http://bms.zeugner.eu for additional help.

# Examples

```
# do some small-scale BMA for demonstration
data(datafls)
mm=bms(datafls[,1:10],nmodel=20)
```

#print info on the best 20 models
print(mm\$topmod)
print(mm\$topmod,digits=10)

```
#equivalent:
cbind(mm$topmod$lik(),mm$topmod$ncount())
```

```
#now print info only for the second-best model:
print(mm$topmod[2])
```

```
#compare 'Included Covariates' to:
topmodels.bma(mm[2])
```

```
#and to
as.vector(mm$topmod[2]$bool_binary())
```

quantile.density Extract Quantiles from 'density' Objects

# Description

Quantiles for objects of class "density", "pred.density" or "coef.density"

```
## S3 method for class 'density'
quantile(x, probs = seq(0.25, 0.75, 0.25), names = TRUE, normalize = TRUE, ...)
## S3 method for class 'coef.density'
quantile(x, probs = seq(0.25, 0.75, 0.25), names = TRUE, ...)
## S3 method for class 'pred.density'
quantile(x, probs = seq(0.25, 0.75, 0.25), names = TRUE, ...)
```

#### Arguments

х	a object of class pred.density, coef.density, density, or a list of densities.
probs	numeric vector of probabilities with values in $[0,1]$ - elements very close to the boundaries return Inf or -Inf
names	logical; if TRUE, the result has a names attribute, resp. a rownames and colnames attributes. Set to FALSE for speedup with many probs.
normalize	logical; if TRUE then the values in x\$y are multiplied with a factor such that their integral is equal to one.
	further arguments passed to or from other methods.

#### Details

The methods quantile.coef.density and quantile.pred.density both apply quantile.density to densities nested with object of class coef.density or pred.density. The function quantile.density applies generically to the built-in class density (as least for versions where there is no such method in the pre-configured packages). Note that quantile.density relies on trapezoidal integration in order to compute the cumulative densities necessary for the calculation of quantiles.

#### Value

If x is of class density (or a list with exactly one element), a vector with quantiles. If x is a list of densities with more than one element (e.g. as resulting from pred.density or coef.density), then the output is a matrix of quantiles, with each matrix row corresponding to the respective density.

#### Author(s)

Stefan Zeugner

#### See Also

quantile.default for a comparable function, pred.density and density.bma for the BMA-specific objects.

Check http://bms.zeugner.eu for additional help.

#### summary.zlm

# Examples

```
data(datafls)
mm = bms(datafls[1:70,], user.int=FALSE)
#predict last two observations with preceding 70 obs:
pmm = pred.density(mm, newdata=datafls[71:72,], plot=FALSE)
#'standard error' quantiles
quantile(pmm, c(.05, .95))
#Posterior density for Coefficient of "GDP60"
cmm = density(mm, reg="GDP60", plot=FALSE)
quantile(cmm, probs=c(.05, .95))
#application to generic density:
dd1 = density(rnorm(1000))
quantile(dd1)
## Not run:
#application to list of densities:
quantile.density( list(density(rnorm(1000)), density(rnorm(1000))) )
## End(Not run)
```

summary.zlm Summarizing Linear Models under Zellner's g

# Description

summary method for class "zlm"

# Usage

```
## S3 method for class 'zlm'
summary(object, printout = TRUE, ...)
```

#### Arguments

object	an object of class zlm: see "Examples" below
printout	If TRUE (default, then information is printed to console in a neat form
	further arguments passed to or from other methods

# Details

summary.zlm prints out coefficients expected values and their standard deviations, as well as information on the gprior and the log marginal likelihood. However, it invisibly returns a list with elements as described below:

# Value

A list with the following elements

residuals	The expected value of residuals from the model
coefficients	The posterior expected values of coefficients (including the intercept)
coef.sd	Posterior standard deviations of the coefficients (the intercept SD is NA, since an improper prior was used)
gprior	The g prior as it has been submitted to object
E.shrinkage	the shrinkage factor $g/(1+g)$ , respectively its posterior expected value in case of a hyper-g prior
SD.shrinkage	(Optionally) the shrinkage factor's posterior standard deviation (in case of a hyper-g prior)
log.lik	The log marginal likelihood of the model

# Author(s)

Stefan Zeugner

# See Also

zlm for creating zlm objects, link{summary.lm} for a similar function on OLS models
See also http://bms.zeugner.eu for additional help.

# Examples

data(datafls)

```
#simple example
foo = zlm(datafls)
summary(foo)
```

sfoo = summary(foo,printout=FALSE)
print(sfoo\$E.shrinkage)

topmod

Topmodel Object

# Description

Create or use an updateable list keeping the best x models it encounters (for advanced users)

# topmod

# Usage

```
topmod(
  nbmodels,
  nmaxregressors = NA,
  bbeta = FALSE,
  lengthfixedvec = 0,
  liks = numeric(0),
  ncounts = numeric(0),
  modelbinaries = matrix(0, 0, 0),
  betas = matrix(0, 0, 0),
  betas2 = matrix(0, 0, 0),
  fixed_vector = matrix(0, 0, 0)
)
```

# Arguments

nbmodels	The maximum number of models to be retained by the topmod object
nmaxregressors	The maximum number of covariates the models in the topmod object are allowed to have
bbeta	if bbeta=TRUE, then first and second moments of model coefficients are stored in addition to basic model statistics (Note: if bbeta<0 then only the first moments are saved)
lengthfixedvec	The length of an optional fixed vector adhering to each model (for instance R-squared, etc). If lengthfixedvec=0 then no additonal fixed vector will be stored.
liks	optional vector of log-likelihoods to initialize topmod object with (length must be <=nbmodels) - see example below
ncounts	optional vector of MCMC frequencies to initialize topmod object with (same length as liks) - see example below
modelbinaries	optional matrix whose columns detail model binaries to initialize topmod object with (same nb columns as liks, nb rows as nmaxregressors) - see example below
betas	optional matrix whose columns are coefficients to initialize topmod object with (same dimensions as modelbinaries) - see example below
betas2	optional matrix whose columns are coefficients' second moments to initialize topmod object with (same dimensions as modelbinaries) - see example below
fixed_vector	optional matrix whose columns are a fixed vector initialize topmod object with (same ncol as modelbinaries) - see example below

# Details

A 'topmod' object (as created by topmod) holds three basic vectors: lik (for the (log) likelihood of models or similar), bool() for a hexcode presentation of the model binaries (cf. bin2hex) and ncount() for the times the models have been drawn.

All these vectors are sorted descendantly by lik, and are of the same length. The maximum length is limited by the argument nbmodels.

If tmo is a topmod object, then a call to tmo\$addmodel (e.g. tmo\$addmodel(mylik=4,vec01=c(T,F,F,T)) updates the object tmo by a model represented by vec01 (here the one including the first and fourth regressor) and the marginal (log) likelihood lik (here: 4).

If this model is already part of tmo, then its respective nount entry is incremented by one; else it is inserted into a position according to the ranking of lik.

In addition, there is the possibility to save (the first moments of) coefficients of a model (betas) and their second moments (betas2), as well as an arbitrary vector of statistics per model (fixed\_vector).

is.topmod returns TRUE if the argument is of class 'topmod'

# Value

a call to topmod returns a list of class "topmod" with the following elements:

addmodel(mylik, fixedvec=numeri		<pre>vbeta=numeric(0),</pre>	<pre>vbeta2=numeric(0),</pre>
	function that a mylik is the ba binary (logical vbeta is a vec coefficients (or of second mor	sic selection criterion (usu or numeric) indicating wi tor of length equal to sum nly accounted for if bbet	in the 'topmod' object (see Details). ally log likelihood), vec01 is the model nich regressors are included. (vec01), contianing only the non-zero a!=FALSE). vbeta2 is a similar vector d for if bbeta=TRUE); fixedvec is an ec (see above)
lik()	A numeric vec	tor of the best models (log	) likelihoods, in decreasing order
bool()	A character vec sorted by lik(		ns for the model binaries (cf. bin2hex),
ncount()		tor of MCMC frequencies lel was introduced by add	for the best models (i.e. how often the model)
nbmodels	Returns the arg	gument nbmodel	
nregs	Returns the arg	gument nmaxregressors	
bool_binary()	Returns a mathematic binary form	rix whose columns preser	nt the models conforming to lik() in
betas()	(Note that the		cients conforming to bool_binary() ts due to non-inclusion of covariates); pty matrix
betas2()	similar to beta this returns an		nts of coefficients Note: if bbeta<=0,
fixed_vector()			`ixed_vector statistics conforming to edvec=0 this returns an empty matrix

# Note

topmod is rather intended as a building block for programming; it has no direct application for a user of the BMS package.

#### topmod-class

#### See Also

the object resulting from bms includes an element of class 'topmod'

Check http://bms.zeugner.eu for additional help.

#### Examples

```
#standard use
 tm= topmod(2,4,TRUE,0) #should keep a maximum two models
 tm$addmodel(-2.3,c(1,1,1,1),1:4,5:8) #update with some model
 tm$addmodel(-2.2,c(0,1,1,1),1:3,5:7) #add another model
 tm$addmodel(-2.2,c(0,1,1,1),1:3,5:7) #add it again -> adjust ncount
 tm$addmodel(-2.5,c(1,0,0,1),1:2,5:6) #add another model
 #read out
 tm$lik()
 tm$ncount()
 tm$bool_binary()
 tm$betas()
 is.topmod(tm)
 #extract a topmod oobject only containing the second best model
 tm2=tm[2]
 #advanced: should return the same result as
 #initialize
 tm2= topmod(2,4,TRUE,0, liks = c(-2.2,-2.3), ncounts = c(2,1),
          modelbinaries = cbind(c(0,1,1,1),c(1,1,1,1)), betas = cbind(0:3,1:4),
          betas2 = cbind(c(0,5:7),5:8))
 #update
 tm$addmodel(-2.5,c(1,0,0,1),1:2,5:6) #add another model
 #read out
 tm$lik()
 tm$ncount()
 tm$bool_binary()
 tm$betas()
```

topmod-class Class "topmod"

#### Description

An updateable list keeping the best x models it encounters in any kind of model iteration

# **Objects from the Class**

Objects can be created by calls to topmod, or indirectly by calls to bms.

A 'topmod' object (as created by topmod) holds three basic vectors: lik (for the (log) likelihood of models or similar), bool() for a hexcode presentation of the model binaries (cf. bin2hex) and ncount() for the times the models have been drawn.

All these vectors are sorted descendantly by lik, and are of the same length. The maximum length is limited by the argument nbmodels.

If two is a topmod object, then a call to two\$addmodel (e.g. two\$addmodel(mylik=4,vec01=c(T,F,F,T)) updates the object two by a model represented by vec01 (here the one including the first and fourth regressor) and the marginal (log) likelihood lik (here: 4).

If this model is already part of tmo, then its respective nount entry is incremented by one; else it is inserted into a position according to the ranking of lik.

In addition, there is the possibility to save (the first moments of) coefficients of a model (betas) and their second moments (betas2), as well as an arbitrary vector of statistics per model (fixed\_vector).

# Author(s)

Martin Feldkircher and Stefan Zeugner

# References

http://bms.zeugner.eu

# See Also

topmod to create topmod objects and a more detailed description, is.topmod to test for this class

#### Examples

```
tm= topmod(2,4,TRUE,0) #should keep a maximum two models
tm$addmodel(-2.3,c(1,1,1,1),1:4,5:8) #update with some model
tm$addmodel(-2.2,c(0,1,1,1),1:3,5:7) #add another model
tm$addmodel(-2.2,c(0,1,1,1),1:3,5:7) #add it again -> adjust ncount
tm$addmodel(-2.5,c(1,0,0,1),1:2,5:6) #add another model
```

#read out
tm\$lik()
tm\$ncount()
tm\$bool\_binary()
tm\$betas()

topmodels.bma

#### Description

Returns a matrix whose columns show which covariates were included in the best models in a 'bma' object. The last two columns detail posterior model probabilities.

## Usage

topmodels.bma(bmao)

#### Arguments

bmao

an object of class 'bma' - see bma-class

# Details

Each bma class (the result of bms) contains 'top models', the x models with the best analytical likelihood that bms had encountered while sampling

See pmp.bma for an explanation of likelihood vs. MCMC frequency concepts

# Value

Each column in the resulting matrix corresponds to one of the 'best' models in bmao: the first column for the best model, the second for the second-best model, etc. The model binaries have elements 1 if the regressor given by the row name was included in the respective models, and 0 otherwise. The second-last row shows the model's posterior model probability based on marginal likelihoods (i.e. its marginal likelihood over the sum of likelihoods of all best models) The last row shows the model's posterior model probability based on MCMC frequencies (i.e. how often the model was accepted vs sum of acceptance of all models) Note that the column names are hexcode representations of the model binaries (e.g. "03" for c(0,0,0,1,0,0))

## See Also

topmod for creating topmod objects, bms for their typical use, pmp.bma for comparing posterior model probabilities

Check http://bms.zeugner.eu for additional help.

## Examples

```
data(datafls)
#sample with a limited data set for demonstration
mm=bms(datafls[,1:12],nmodel=20)
```

#show binaries for all
topmodels.bma(mm)

```
#show binaries for 2nd and 3rd best model, without the model probs
topmodels.bma(mm[2:3])[1:11,]
#access model binaries directly
```

```
mm$topmod$bool_binary()
```

variable.names.bma Variable names and design matrix

# Description

Simple utilities retrieving variable names and design matrix from a bma object

# Usage

```
## S3 method for class 'bma'
variable.names(object, ...)
```

# Arguments

object	A bma object (as produced by bms)
	further arguments passed to or from other methods

# Details

All functions are bma-functions for the generic methods variable.names, deviance, and model.frame.

# See Also

bms for creating bma objects

Check http://bms.zeugner.eu for additional help.

# Examples

```
data(datafls)
bma_enum=bms(datafls[1:20,1:10])
```

model.frame(bma\_enum) # similar to
bma\_enum\$arguments\$X.data

```
variable.names(bma_enum)[-1] # is equivalent to
bma_enum$reg.names
```

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# Description

Simple utilities retrieving variable names and design matrix from a bma object

# Usage

```
## S3 method for class 'zlm'
variable.names(object, ...)
```

#### Arguments

object	A bma object (as produced by bms)
	further arguments passed to or from other methods

#### Details

variable.names.zlm: method variable.names for a zlm model. vcov.zlm: the posterior variance-covariance matrix of the coefficients of a zlm model - cf. vcov logLik.zlm: a zlm model's log-likelihood p(y|M) according to the implementation of the respective coefficient prior

# See Also

zlm for creating zlm objects

Check http://bms.zeugner.eu for additional help.

# Examples

```
data(datafls)
```

```
zz=zlm(datafls)
variable.names(zz)
vcov(zz)
logLik(zz)
```

# Description

Used to fit the Bayesian normal-conjugate linear model with Zellner's g prior and mean zero coefficient priors. Provides an object similar to the lm class.

#### Usage

zlm(formula, data = NULL, subset = NULL, g = "UIP")

#### Arguments

formula	an object of class "formula" (or one that can be coerced to that class), such as a data.frame - cf. $lm$
data	an optional data.frame (or one that can be coerced to that class): cf. 1m
subset	an optional vector specifying a subset of observations to be used in the fitting process.
g	specifies the hyperparameter on Zellner's g-prior for the regression coefficients. g="UIP" corresponds to $g = N$ , the number of observations (default); g="BRIC" corresponds to the benchmark prior suggested by Fernandez, Ley and Steel (2001), i.e $g = max(N, K^2)$ , where K is the total number of covariates; g="EBL" estimates a local empirical Bayes g-parameter (as in Liang et al. (2008)); g="hyper" takes the 'hyper-g' prior distribution (as in Liang et al., 2008) with the default hyper-parameter $a = 3$ ; This hyperparameter can be adjusted (between $2 < a <= 4$ ) by setting g="hyper=2.9", for instance. Alternatively, g="hyper=UIP" sets the prior expected value of the shrinkage factor equal to that of UIP (above), g="hyper=BRIC" sets it according to BRIC

#### Details

zlm estimates the coefficients of the following model  $y = \alpha + X\beta + \epsilon$  where  $\epsilon \sim N(0, \sigma^2)$  and X is the design matrix

The priors on the intercept  $\alpha$  and the variance  $\sigma$  are improper:  $alpha \propto 1, sigma \propto \sigma^{-1}$ 

Zellner's g affects the prior on coefficients:  $beta \sim N(0, \sigma^2 g(X'X)^{-1})$ .

Note that the prior mean of coefficients is set to zero by default and cannot be adjusted. Note moreover that zlm always includes an intercept.

#### Value

Returns a list of class zlm that contains at least the following elements (cf. lm):

coefficients	a named vector of posterior coefficient expected values
residuals	the residuals, that is response minus fitted values
fitted.values	the fitted mean values

# zlm

rank	the numeric rank of the fitted linear model
df.residual	the residual degrees of freedom
call	the matched call
terms	the terms object used
model	the model frame used
coef2moments	a named vector of coefficient posterior second moments
marg.lik	the log marginal likelihood of the model
gprior.info	a list detailing information on the g-prior, cf. output value gprior.info in bms

# Author(s)

Stefan Zeugner

#### References

The representation follows Fernandez, C. E. Ley and M. Steel (2001): Benchmark priors for Bayesian model averaging. Journal of Econometrics 100(2), 381–427

See also <a href="http://bms.zeugner.eu">http://bms.zeugner.eu</a> for additional help.

# See Also

The methods summary.zlm and predict.lm provide additional insights into zlm output. The function as.zlm extracts a single out model of a bma object (as e.g. created throughbms). Moreover, lm for the standard OLS object, bms for the application of zlm in Bayesian model averaging.

Check http://bms.zeugner.eu for additional help.

## Examples

data(datafls)

```
#simple example
foo = zlm(datafls)
summary(foo)
```

```
#example with formula and subset
foo2 = zlm(y~GDP60+LifeExp, data=datafls, subset=2:70) #basic model, omitting three countries
summary(foo2)
```

zlm-class

# Description

A list holding output from the Bayesian Linar Model under Zellner's g prior akin to class 'lm'

#### **Objects from the Class**

Objects can be created via calls to zlm, but indirectly also via as.zlm. zlm estimates a Bayesian Linear Model under Zellner's g prior - its output is very similar to objects of class lm (cf. section 'Value')

# Author(s)

Martin Feldkircher and Stefan Zeugner

# References

http://bms.zeugner.eu

# See Also

zlm and as.zlm for creating zlm objects, density.zlm, predict.zlm and summary.zlm for other posterior results

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