Package 'lsirm12pl'

October 22, 2025

```
Type Package
Title Latent Space Item Response Model
Version 1.3.9
Date 2025-10-22
Maintainer Gwanghee Kim <musagh08@yonsei.ac.kr>
Description Analysis of dichotomous and continuous response data using latent fac-
     tor by both 1PL LSIRM and 2PL LSIRM as described in Jeon et al. (2021) <doi:10.1007/s11336-
     021-09762-5>. It includes original 1PL LSIRM and 2PL LSIRM provided for binary re-
     sponse data and its extension for continuous response data. Bayesian model selection with spike-
     and-slab prior and method for dealing data with missing value under missing at random, miss-
     ing completely at random are also supported. Various diagnostic plots are available to in-
     spect the latent space and summary of estimated parameters.
License GPL-3
Imports Rcpp (>= 1.0.5), MCMCpack, ggplot2, GPArotation, dplyr (>=
     1.1.4), grDevices, rlang, pROC, coda, spatstat, spatstat.geom,
     spatstat.random, plotly, gridExtra, grid, tidyr, fpc, kernlab,
     plyr, purrr
LinkingTo Rcpp, RcppArmadillo
Encoding UTF-8
RoxygenNote 7.3.2
Suggests knitr, testthat
Depends R (>= 3.1.0)
LazyData true
NeedsCompilation yes
Author Dongyoung Go [aut],
     Gwanghee Kim [aut, cre],
     Jina Park [aut],
     Ickhoon Jin [ctb],
     Minjeong Jeon [ctb]
```

Repository CRAN

Date/Publication 2025-10-22 07:00:02 UTC

2 Contents

Contents

| BFPT |
|----------------------------------|
| diagnostic |
| gof |
| lsirm |
| lsirm.formula |
| lsirm12pl |
| lsirm1pl |
| lsirm1pl_fixed_gamma |
| lsirm1pl_fixed_gamma_mar |
| lsirm1pl_fixed_gamma_mcar |
| lsirm1pl_mar |
| lsirm1pl_mar_ss |
| lsirm1pl_mcar |
| lsirm1pl_mcar_ss |
| lsirm1pl_normal_fixed_gamma |
| lsirm1pl_normal_fixed_gamma_mar |
| lsirm1pl_normal_fixed_gamma_mcar |
| lsirm1pl_normal_mar |
| lsirm1pl_normal_mar_ss |
| lsirm1pl_normal_mcar |
| lsirm1pl_normal_mcar_ss |
| lsirm1pl_normal_o |
| lsirm1pl_normal_ss |
| lsirm1pl_o |
| lsirm1pl_ss |
| lsirm2pl |
| lsirm2pl_fixed_gamma |
| lsirm2pl_fixed_gamma_mar |
| lsirm2pl_fixed_gamma_mcar |
| lsirm2pl_mar |
| lsirm2pl_mar_ss |
| lsirm2pl_mcar |
| lsirm2pl_mcar_ss |
| lsirm2pl_normal_fixed_gamma |
| lsirm2pl_normal_fixed_gamma_mar |
| lsirm2pl_normal_fixed_gamma_mcar |
| lsirm2pl_normal_mar |
| lsirm2pl_normal_mar_ss |
| lsirm2pl_normal_mcar |
| lsirm2pl_normal_mcar_ss |
| lsirm2pl_normal_o |
| lsirm2pl_normal_ss |
| lsirm2pl_o |
| lsirm2pl_ss |
| onepl |
| plot |
| |

BFPT 3

| Index | | | | | | | | | | | | | | | | | | | | | 1 | 144 |
|-------|-------------------|--|---|------|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|-----|-----|
| | TDRI twopl | | | | | | | | | | | | | | | | | | | | . 1 | 141 |
| | print.su summa | | • | | | | | | | | | | | | | | | | | | | |

BFPT

Big Five Personality Test

Description

A dataset containing the result of personality test for 50 questions from 1,000 random sampled people.

Usage

```
data(BFPT)
```

Format

A matrix with 1,015,341 rows and 50 columns.

Details

A dataset collected in 2016-2018 through an interactive on-line personality test, containing the result of personality test for 50 questions. 1,000 people are random sampled from the original dataset containing 1,015,341 people. The scale is labeled as 1=Disagree, 3=Neutral and 5=Agree.

Source

```
https://www.kaggle.com/tunguz/big-five-personality-test
```

diagnostic

Diagnostic the result of LSIRM.

Description

diagnostic checks the convergence of MCMC for LSIRM parameters using various diagnostic tools, such as trace plots, posterior density distributions, autocorrelation functions (ACF), and Gelman-Rubin-Brooks plots.

```
diagnostic(
  object,
  draw.item = list(beta = c(1), theta = c(1)),
  gelman.diag = FALSE
)
```

4 gof

Arguments

object Object of class lsirm.

draw.item List; Each key in the list corresponds to a specific parameters such as "beta",

"theta", "gamma", "alpha", "sigma", "theta_sd", "z", "w", and "zw.dist". The values of the list indicate the indices of these parameters. For the key "zw.dist", the value is a matrix with two columns: the first column represents the indices of respondents, and the second column represents the indices of items. For the keys "z" and "w", the value is a matrix with two columns: the first column represents the indices of respondents/items, and the second column represents

the dimension indices.

gelman.diag Logical; If TRUE, the Gelman-Rubin convergence diagnostic will be printed.

Default is FALSE.

Value

diagnostic returns plots for checking MCMC convergence for selected parameters.

Examples

gof

Goodness-of-fit LSIRM

Description

gof is goodness-of-fit the latent space of fitted LSIRM.

```
gof(object, chain.idx = 1)
```

lsirm 5

Arguments

object Object of class 1sirm.

chain.idx Numeric; Index of MCMC chain. Default is 1.

Value

gof returns the boxplot or AUC plot

Examples

```
# generate example item response matrix
data <- matrix(rbinom(500, size = 1, prob = 0.5),ncol=10,nrow=50)
lsirm_result <- lsirm(data ~ lsirm1pl())
gof(lsirm_result)</pre>
```

lsirm

Fit a LSIRM (Latent Space Item Response Model)

Description

lsirm is used to fit 1PL LSIRM and 2PL LSIRM using Bayesian method as described in Jeon et al. (2021).

Usage

```
lsirm(formula, ...)
```

Arguments

formula

The form of formula is lsirm(A ~ <term 1>(<term 2>, <term 3>...)), where A is binary or continuous item response matrix to be analyzed, <term1> is the model you want to fit and has one of the following values: "lsirm1pl" and "lsirm2pl"., and <term 2>, <term 3>, etc. are each option for the model.

... Additional arguments for the corresponding function.

Details

The descriptions of options for each model, such as <term 2> and <term 3>, are included in lsirm1pl for 1PL LSIRM and lsirm2pl for 2PL LSIRM.

Value

lsirm returns an object of class list.

See corresponding functions such as lsirm1pl for 1PL LSIRM and lsirm2pl for 2PL LSIRM.

6 Isirm12pl

See Also

```
lsirm1pl for 1PL LSIRM.
lsirm2pl for 2PL LSIRM.
```

Examples

```
# generate example item response matrix
data <- matrix(rbinom(500, size = 1, prob = 0.5),ncol=10,nrow=50)

lsirm_result <- lsirm(data~lsirm1pl())
lsirm_result <- lsirm(data~lsirm2pl())</pre>
```

lsirm.formula

Formula function for LSIRM

Description

lsirm.formula is formula object.

Usage

```
## S3 method for class 'formula'
lsirm(formula, ...)
```

Arguments

formula

The form of formula is lsirm(A ~ <term 1> (<term 2>, <term 3> . . .)), where A is binary or continuous item response matrix to be analyzed, <term1> is the model you want to fit and has one of the following values: "lsirm1pl" and "lsirm2pl"., and <term 2>, <term 3>, etc., are each option for the model.

. . . Additional arguments for the corresponding function.

lsirm12pl

lsirm12pl-package

Description

Analysis of dichotomous and continuous response data using latent factor by both 1PL LSIRM and 2PL LSIRM as described in Jeon et al. (2021) <doi:10.1007/s11336-021-09762-5>. It includes original 1PL LSIRM and 2PL LSIRM provided for binary response data and its extension for continuous response data. Bayesian model selection with spike-and-slab prior and method for dealing data with missing value under missing at random, missing completely at random are also supported. Various diagnostic plots are available to inspect the latent space and summary of estimated parameters.

lsirm1pl 7

lsirm1pl

Fit a 1PL LSIRM for binary and continuous item response data

Description

lsirm1pl integrates all functions related to 1PL LSIRM. Various 1PL LSIRM function can be used by setting the spikenslab, fixed_gamma, and missing_data arguments.

This function can be used regardless of the data type, providing a unified approach to model fitting.

Usage

```
lsirm1pl(
  data,
  spikenslab = FALSE,
  fixed_gamma = FALSE,
  missing_data = NA,
  chains = 1,
  multicore = 1,
  seed = NA,
  ndim = 2,
  niter = 15000,
  nburn = 2500,
  nthin = 5,
  nprint = 500,
  jump\_beta = 0.4,
  jump\_theta = 1,
  jump_gamma = 0.025,
  jump_z = 0.5,
  jump_w = 0.5,
  pr_mean_beta = 0,
  pr_sd_beta = 1,
  pr_mean_theta = 0,
  pr_sd_theta = 1,
  pr_mean_gamma = 0.5,
  pr_sd_gamma = 1,
  pr_a_theta = 0.001,
  pr_b_t = 0.001,
  verbose = FALSE,
  fix_theta_sd = FALSE,
)
```

Arguments

data

Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item.

lsirm1pl

spikenslab Logical; specifies whether to use a model selection approach. Default is FALSE.

fixed_gamma Logical; indicates whether to fix gamma at 1. Default is FALSE.

missing_data Character; the type of missing data assumed. Options are NA, "mar", or "mcar".

Default is NA.

chains Integer; the number of MCMC chains to run. Default is 1.

multicore Integer; the number of cores to use for parallel execution. Default is 1.

seed Integer; the seed number for MCMC fitting. Default is NA.

ndim Integer; the dimension of the latent space. Default is 2.

niter Integer; the total number of MCMC iterations to run. Default is 15000.

nburn Integer; the number of initial MCMC iterations to discard as burn-in. Default is

2500.

nthin Integer; the number of MCMC iterations to thin. Default is 5.

nprint Integer; the interval at which MCMC samples are displayed during execution.

Default is 500.

jump_beta Numeric; the jumping rule for the beta proposal density. Default is 0.4.

Numeric; the jumping rule for the theta proposal density. Default is 1.0.

jump_gamma Numeric; the jumping rule for the gamma proposal density. Default is 0.025.

jump_z Numeric; the jumping rule for the z proposal density. Default is 0.5.

Numeric; the jumping rule for the w proposal density. Default is 0.5.

pr_mean_beta Numeric; the mean of the normal prior for beta. Default is 0.

pr_sd_beta Numeric; the standard deviation of the normal prior for beta. Default is 1.0.

pr_mean_theta Numeric; the mean of the normal prior for theta. Default is 0.

pr_sd_theta Numeric; the standard deviation of the normal prior for theta. Default is 1.0.

pr_mean_gamma Numeric; mean of log normal prior for gamma. Default is 0.5.

pr_sd_gamma Numeric; standard deviation of log normal prior for gamma. Default is 1.0.

pr_a_theta Numeric; the shape parameter of the inverse gamma prior for the variance of

theta. Default is 0.001.

theta. Default is 0.001.

verbose Logical; If TRUE, MCMC samples are printed for each nprint. Default is

FALSE.

fix_theta_sd Logical; If TRUE, the standard deviation of the theta parameter is fixed. Default

is FALSE.

... Additional arguments for the for various settings. Refer to the functions in the

Details.

lsirm1pl 9

Details

Additional arguments and return values for each function are documented in the respective function's description.

- * For LSIRM with data included missing value are detailed in lsirm1pl_mar and lsirm1pl_mcar.
- * For LSIRM using the spike-and-slab model selection approach are detailed in lsirm1pl_ss.
- * For continuous version of LSIRM are detailed in lsirm1pl normal o.

For 1PL LSIRM with binary item response data, the probability of correct response by respondent j to item i with item effect β_i , respondent effect θ_j and the distance between latent position w_i of item i and latent position z_j of respondent j in the shared metric space, with γ represents the weight of the distance term:

$$logit(P(Y_{j,i} = 1 | \theta_j, \beta_i, \gamma, z_j, w_i)) = \theta_j + \beta_i - \gamma ||z_j - w_i||$$

For 1PL LSIRM with continuous item response data, the continuous value of response by respondent j to item i with item effect β_i , respondent effect θ_j and the distance between latent position w_i of item i and latent position z_j of respondent j in the shared metric space, with γ represents the weight of the distance term:

$$Y_{i,i} = \theta_i + \beta_i - \gamma ||z_i - w_i|| + e_{i,i}$$

where the error $e_{j,i} \sim N(0, \sigma^2)$.

Value

lsirm1pl returns an object of list. The basic return list containing the following components:

data A data frame or matrix containing the variables used in the model.

bic A numeric value representing the Bayesian Information Criterion (BIC).

mcmc_inf Details about the number of MCMC iterations, burn-in periods, and thinning

intervals.

map_inf The log maximum a posteriori (MAP) value and the iteration number at which

this MAP value occurs.

beta_estimate Posterior estimates of the beta parameter.

theta_estimate Posterior estimates of the theta parameter.

sigma_theta_estimate

Posterior estimates of the standard deviation of theta.

z_estimate Posterior estimates of the z parameter.
 w_estimate Posterior estimates of the w parameter.
 beta Posterior samples of the beta parameter.
 theta Posterior samples of the theta parameter.

theta_sd Posterior samples of the standard deviation of theta.

z Posterior samples of the z parameter, represented as a 3-dimensional matrix

where the last axis denotes the dimension of the latent space.

| W | Posterior samples of the w parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space. |
|--------------|--------------------------------------------------------------------------------------------------------------------------------------------|
| accept_beta | Acceptance ratio for the beta parameter. |
| accept_theta | Acceptance ratio for the theta parameter. |
| accept_z | Acceptance ratio for the z parameter. |
| accept_w | Acceptance ratio for the w parameter. |
| | Additional return values for various settings. Refer to the functions in the Details. |

Note

If both spikenslab and fixed_gamma are set TRUE, it returns error because both are related to gamma.

See Also

The LSIRM for 1PL LSIRM for binary item response data as following:

```
lsirm1pl_o, lsirm1pl_fixed_gamma, lsirm1pl_mar, lsirm1pl_mcar, lsirm1pl_fixed_gamma_mar,
lsirm1pl_fixed_gamma_mcar, lsirm1pl_ss, lsirm1pl_mar_ss, and lsirm1pl_mcar_ss
```

The LSIRM for 1PL LSIRM for continuous item response data as following:

```
lsirm1pl_normal_o, lsirm1pl_normal_fixed_gamma, lsirm1pl_normal_mar, lsirm1pl_normal_mcar,lsirm1pl_norm
lsirm1pl_normal_fixed_gamma_mcar, lsirm1pl_normal_ss, lsirm1pl_normal_mar_ss, lsirm1pl_normal_mcar_ss
```

Examples

```
# generate example item response matrix
data <- matrix(rbinom(500, size = 1, prob = 0.5),ncol=10,nrow=50)
lsirm_result <- lsirm1pl(data)

# The code following can achieve the same result.
lsirm_result <- lsirm(data~lsirm1pl())</pre>
```

```
{\tt lsirm1pl\_fixed\_gamma} \quad \textit{1PL LSIRM fixing gamma to 1}.
```

Description

lsirm1pl_fixed_gamma is used to fit 1PL LSIRM with gamma fixed to 1. lsirm1pl_fixed_gamma factorizes item response matrix into column-wise item effect, row-wise respondent effect and further embeds interaction effect in a latent space. The resulting latent space provides an interaction map that represents interactions between respondents and items.

Usage

```
lsirm1pl_fixed_gamma(
 data,
 ndim = 2,
 niter = 15000,
 nburn = 2500,
 nthin = 5,
 nprint = 500,
  jump\_beta = 0.4,
  jump\_theta = 1,
  jump_z = 0.5,
  jump_w = 0.5,
 pr_mean_beta = 0,
 pr_sd_beta = 1,
 pr_mean_theta = 0,
 pr_sd_theta = 1,
 pr_a_theta = 0.001,
 pr_b_t = 0.001,
 verbose = FALSE,
  fix_theta_sd = FALSE
)
```

Arguments

| data | Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item. |
|---------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| ndim | Integer; the dimension of the latent space. Default is 2. |
| niter | Integer; the total number of MCMC iterations to run. Default is 15000. |
| nburn | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500. |
| nthin | Integer; the number of MCMC iterations to thin. Default is 5. |
| nprint | Integer; the interval at which MCMC samples are displayed during execution. Default is 500. |
| jump_beta | Numeric; the jumping rule for the beta proposal density. Default is 0.4. |
| jump_theta | Numeric; the jumping rule for the theta proposal density. Default is 1.0. |
| jump_z | Numeric; the jumping rule for the z proposal density. Default is 0.5. |
| jump_w | Numeric; the jumping rule for the w proposal density. Default is 0.5. |
| pr_mean_beta | Numeric; the mean of the normal prior for beta. Default is 0. |
| pr_sd_beta | Numeric; the standard deviation of the normal prior for beta. Default is 1.0. |
| pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0. |
| pr_sd_theta | Numeric; the standard deviation of the normal prior for theta. Default is 1.0. |
| pr_a_theta | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001. |

theta. Default is 0.001.

verbose Logical; If TRUE, MCMC samples are printed for each nprint. default value

is FALSE

fix_theta_sd Logical; If TRUE, the standard deviation of the theta parameter is fixed. Default

is FALSE.

Details

lsirm1pl_fixed_gamma models the probability of correct response by respondent j to item i with item effect β_i , respondent effect θ_j and the distance between latent position w_i of item i and latent position z_j of respondent j in the shared metric space:

$$logit(P(Y_{i,i} = 1 | \theta_i, \beta_i, z_i, w_i)) = \theta_i + \beta_i - ||z_i - w_i||$$

Value

lsirm1pl_fixed_gamma returns an object of list containing the following components:

data Data frame or matrix containing the variables in the model.

bic Numeric value with the corresponding BIC.

mcmc_inf Details about the number of MCMC iterations, burn-in periods, and thinning

intervals.

map_inf The log maximum a posteriori (MAP) value and the iteration number at which

this MAP value occurs.

beta_estimate Posterior estimates of the beta parameter.
theta_estimate Posterior estimates of the theta parameter.

sigma_theta_estimate

Posterior estimates of the standard deviation of theta.

z_estimate
 w_estimate
 Posterior estimates of the z parameter.
 w_estimate
 Posterior estimates of the w parameter.
 beta
 Posterior samples of the beta parameter.
 theta
 Posterior samples of the theta parameter.

theta_sd Posterior samples of the standard deviation of theta.

z Posterior samples of the z parameter, represented as a 3-dimensional matrix

where the last axis denotes the dimension of the latent space.

w Posterior samples of the w parameter, represented as a 3-dimensional matrix

where the last axis denotes the dimension of the latent space.

z_raw Posterior samples of the z parameter without procrustes matching.w_raw Posterior samples of the w parameter without procrustes matching.

accept_beta Acceptance ratio for the beta parameter.
accept_theta Acceptance ratio for the theta parameter.
accept_z Acceptance ratio for the z parameter.
accept_w Acceptance ratio for the w parameter.

Examples

```
# generate example item response matrix
data <- matrix(rbinom(500, size = 1, prob = 0.5),ncol=10,nrow=50)

lsirm_result <- lsirm1pl_fixed_gamma(data)

# The code following can achieve the same result.
lsirm_result <- lsirm(data ~ lsirm1pl(spikenslab = FALSE, fixed_gamma = TRUE))</pre>
```

lsirm1pl_fixed_gamma_mar

1PL LSIRM fixing gamma to 1 for missing at random data.

Description

lsirm1pl_fixed_gamma_mar is used to fit LSIRM with gamma fixed to 1 in incomplete data assumed to be missing at random. lsirm1pl_fixed_gamma_mar factorizes item response matrix into columnwise item effect, row-wise respondent effect and further embeds interaction effect in a latent space, while considering the missing element under the assumption of missing at random. The resulting latent space provides an interaction map that represents interactions between respondents and items.

```
lsirm1pl_fixed_gamma_mar(
  data,
  ndim = 2,
 niter = 15000,
  nburn = 2500,
  nthin = 5,
  nprint = 500,
  jump\_beta = 0.4,
  jump\_theta = 1,
  jump_z = 0.5,
  jump_w = 0.5,
  pr_mean_beta = 0,
  pr_sd_beta = 1,
 pr_mean_theta = 0,
 pr_sd_theta = 1,
  pr_a_theta = 0.001,
 pr_b_teta = 0.001,
 missing.val = 99,
 verbose = FALSE,
  fix_{theta_sd} = FALSE
)
```

Arguments

| data | Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item. |
|---------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| ndim | Integer; the dimension of the latent space. Default is 2. |
| niter | Integer; the total number of MCMC iterations to run. Default is 15000. |
| nburn | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500. |
| nthin | Integer; the number of MCMC iterations to thin. Default is 5. |
| nprint | Integer; the interval at which MCMC samples are displayed during execution. Default is 500. |
| jump_beta | Numeric; the jumping rule for the beta proposal density. Default is 0.4. |
| jump_theta | Numeric; the jumping rule for the theta proposal density. Default is 1.0. |
| jump_z | Numeric; the jumping rule for the z proposal density. Default is 0.5. |
| jump_w | Numeric; the jumping rule for the w proposal density. Default is 0.5. |
| pr_mean_beta | Numeric; the mean of the normal prior for beta. Default is 0. |
| pr_sd_beta | Numeric; the standard deviation of the normal prior for beta. Default is 1.0. |
| pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0. |
| pr_sd_theta | Numeric; the standard deviation of the normal prior for theta. Default is 1.0. |
| pr_a_theta | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001 . |
| pr_b_theta | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001 . |
| missing.val | Numeric; a number to replace missing values. Default is 99. |
| verbose | Logical; If TRUE, MCMC samples are printed for each nprint. default value is FALSE. |
| fix_theta_sd | Logical; If TRUE, the standard deviation of the theta parameter is fixed. Default is FALSE. |

Details

lsirm1pl_fixed_gamma_mar models the probability of correct response by respondent j to item i with item effect β_i , respondent effect θ_j and the distance between latent position w_i of item i and latent position z_j of respondent j in the shared metric space:

$$logit(P(Y_{j,i} = 1 | \theta_j, \beta_i, z_j, w_i)) = \theta_j + \beta_i - ||z_j - w_i||$$

Under the assumption of missing at random, the model takes the missing element into consideration in the sampling procedure. For the details of missing at random assumption and data augmentation, see References.

Value

lsirm1pl_fixed_gamma_mar returns an object of list containing the following components:

data Data frame or matrix containing the variables in the model.

missing.val A number to replace missing values.

bic Numeric value with the corresponding BIC.

mcmc_inf Details about the number of MCMC iterations, burn-in periods, and thinning

intervals.

map_inf The log maximum a posteriori (MAP) value and the iteration number at which

this MAP value occurs.

beta_estimate Posterior estimates of the beta parameter.

theta_estimate Posterior estimates of the theta parameter.

sigma_theta_estimate

Posterior estimates of the standard deviation of theta.

z_estimate Posterior estimates of the z parameter.w_estimate Posterior estimates of the w parameter.

imp_estimate Probability of imputating a missing value with 1.

beta Posterior samples of the beta parameter.
theta Posterior samples of the theta parameter.

theta_sd Posterior samples of the standard deviation of theta.

z Posterior samples of the z parameter, represented as a 3-dimensional matrix

where the last axis denotes the dimension of the latent space.

w Posterior samples of the w parameter, represented as a 3-dimensional matrix

where the last axis denotes the dimension of the latent space.

z_rawPosterior samples of the z parameter without procrustes matching.w_rawPosterior samples of the w parameter without procrustes matching.

imp Imputation for missing Values using posterior samples.

accept_beta Acceptance ratio for the beta parameter.

accept_theta Acceptance ratio for the theta parameter.

accept_z Acceptance ratio for the z parameter.

accept_w Acceptance ratio for the w parameter.

References

Little, R. J., & Rubin, D. B. (2019). Statistical analysis with missing data (Vol. 793). John Wiley & Sons.

Examples

```
# generate example item response matrix
data <- matrix(rbinom(500, size = 1, prob = 0.5),ncol=10,nrow=50)

# generate example missing indicator matrix
missing_mat <- matrix(rbinom(500, size = 1, prob = 0.2),ncol=10,nrow=50)

# make missing value with missing indicator matrix
data[missing_mat==1] <- 99

lsirm_result <- lsirm1pl_fixed_gamma_mar(data)

# The code following can achieve the same result.
lsirm_result <- lsirm(data ~ lsirm1pl(spikenslab = FALSE, fixed_gamma = TRUE, missing_data = "mar", missing.val = 99))</pre>
```

lsirm1pl_fixed_gamma_mcar

1PL LSIRM fixing gamma to 1 for missing completely at random data.

Description

lsirm1pl_fixed_gamma_mcar is used to fit LSIRM with gamma fixed to 1 in incomplete data assumed to be missing completely at random. lsirm1pl_fixed_gamma_mcar factorizes item response matrix into column-wise item effect, row-wise respondent effect and further embeds interaction effect in a latent space, while ignoring the missing element under the assumption of missing completely at random. The resulting latent space provides an interaction map that represents interactions between respondents and items.

```
lsirm1pl_fixed_gamma_mcar(
  data,
  ndim = 2,
  niter = 15000,
  nburn = 2500,
  nthin = 5,
  nprint = 500,
  jump\_beta = 0.4,
  jump\_theta = 1,
  jump_z = 0.5,
  jump_w = 0.5,
  pr_mean_beta = 0,
  pr_sd_beta = 1,
  pr_mean_theta = 0,
  pr_sd_theta = 1,
  pr_a_theta = 0.001,
```

```
pr_b_theta = 0.001,
missing.val = 99,
verbose = FALSE,
fix_theta_sd = FALSE)
```

Arguments

| data | Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item. |
|---------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| ndim | Integer; the dimension of the latent space. Default is 2. |
| niter | Integer; the total number of MCMC iterations to run. Default is 15000. |
| nburn | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500. |
| nthin | Integer; the number of MCMC iterations to thin. Default is 5. |
| nprint | Integer; the interval at which MCMC samples are displayed during execution. Default is 500. |
| jump_beta | Numeric; the jumping rule for the beta proposal density. Default is 0.4. |
| jump_theta | Numeric; the jumping rule for the theta proposal density. Default is 1.0. |
| jump_z | Numeric; the jumping rule for the z proposal density. Default is 0.5. |
| jump_w | Numeric; the jumping rule for the w proposal density. Default is 0.5. |
| pr_mean_beta | Numeric; the mean of the normal prior for beta. Default is 0. |
| pr_sd_beta | Numeric; the standard deviation of the normal prior for beta. Default is 1.0. |
| pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0. |
| pr_sd_theta | Numeric; the standard deviation of the normal prior for theta. Default is 1.0. |
| pr_a_theta | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001. |
| pr_b_theta | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001. |
| missing.val | Numeric; a number to replace missing values. Default is 99. |
| verbose | Logical; If TRUE, MCMC samples are printed for each nprint. default value is \ensuremath{FALSE} |
| fix_theta_sd | Logical; If TRUE, the standard deviation of the theta parameter is fixed. Default is FALSE. |

Details

lsirm1pl_fixed_gamma_mcar models the probability of correct response by respondent j to item i with item effect β_i , respondent effect θ_j and the distance between latent position w_i of item i and latent position z_j of respondent j in the shared metric space:

$$logit(P(Y_{j,i} = 1 | \theta_j, \beta_i, z_j, w_i)) = \theta_j + \beta_i - ||z_j - w_i||$$

Under the assumption of missing completely at random, the model ignores the missing element in doing inference. For the details of missing completely at random assumption and data augmentation, see References.

Value

lsirm1pl_fixed_gamma_mcar returns an object of list containing the following components:

data Data frame or matrix containing the variables in the model.

missing.val A number to replace missing values.

bic Numeric value with the corresponding BIC.

mcmc_inf Details about the number of MCMC iterations, burn-in periods, and thinning

intervals

map_inf The log maximum a posteriori (MAP) value and the iteration number at which

this MAP value occurs.

beta_estimate Posterior estimates of the beta parameter.
theta_estimate Posterior estimates of the theta parameter.

sigma_theta_estimate

Posterior estimates of the standard deviation of theta.

z_estimate Posterior estimates of the z parameter.
 w_estimate Posterior estimates of the w parameter.
 beta Posterior samples of the beta parameter.
 theta Posterior samples of the theta parameter.

theta_sd Posterior samples of the standard deviation of theta.

z Posterior samples of the z parameter, represented as a 3-dimensional matrix

where the last axis denotes the dimension of the latent space.

w Posterior samples of the w parameter, represented as a 3-dimensional matrix

where the last axis denotes the dimension of the latent space.

z_raw Posterior samples of the z parameter without procrustes matching.w_raw Posterior samples of the w parameter without procrustes matching.

accept_beta Acceptance ratio for the beta parameter.
accept_theta Acceptance ratio for the theta parameter.
accept_z Acceptance ratio for the z parameter.
accept_w Acceptance ratio for the w parameter.

References

Little, R. J., & Rubin, D. B. (2019). Statistical analysis with missing data (Vol. 793). John Wiley & Sons.

Examples

```
# generate example item response matrix
data <- matrix(rbinom(500, size = 1, prob = 0.5),ncol=10,nrow=50)
# generate example missing indicator matrix
missing_mat <- matrix(rbinom(500, size = 1, prob = 0.2),ncol=10,nrow=50)</pre>
```

lsirm1pl_mar 19

```
# make missing value with missing indicator matrix
data[missing_mat==1] <- 99

lsirm_result <- lsirm1pl_fixed_gamma_mcar(data)

# The code following can achieve the same result.
lsirm_result <- lsirm(data ~ lsirm1pl(spikenslab = FALSE, fixed_gamma = TRUE, missing_data = "mcar", missing.val = 99))</pre>
```

lsirm1pl_mar

1PL LSIRM for missing at random data.

Description

lsirm1pl_mar is used to fit 1PL LSIRM in incomplete data assumed to be missing at random. lsirm1pl_mar factorizes item response matrix into column-wise item effect, row-wise respondent effect and further embeds interaction effect in a latent space, while considering the missing element under the assumption of missing at random. The resulting latent space provides an interaction map that represents interactions between respondents and items.

```
lsirm1pl_mar(
  data,
  ndim = 2,
  niter = 15000.
  nburn = 2500,
  nthin = 5,
  nprint = 500,
  jump_beta = 0.4,
  jump\_theta = 1,
  jump_gamma = 0.025,
  jump_z = 0.5,
  jump_w = 0.5,
  pr_mean_beta = 0,
 pr_sd_beta = 1,
  pr_mean_theta = 0,
  pr_sd_theta = 1,
  pr_mean_gamma = 0.5,
  pr_sd_gamma = 1,
  pr_a_theta = 0.001,
  pr_b_t = 0.001,
 missing.val = 99,
 verbose = FALSE,
  fix_{theta_sd} = FALSE
)
```

20 lsirm1pl_mar

Arguments

| 1.4. | Marin Diagram of the control of Parkers |
|---------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| data | Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item. |
| | |
| ndim | Integer; the dimension of the latent space. Default is 2. |
| niter | Integer; the total number of MCMC iterations to run. Default is 15000. |
| nburn | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500. |
| nthin | Integer; the number of MCMC iterations to thin. Default is 5. |
| nprint | Integer; the interval at which MCMC samples are displayed during execution. Default is 500. |
| jump_beta | Numeric; the jumping rule for the beta proposal density. Default is 0.4. |
| jump_theta | Numeric; the jumping rule for the theta proposal density. Default is 1.0. |
| jump_gamma | Numeric; the jumping rule for the gamma proposal density. Default is 0.025 |
| jump_z | Numeric; the jumping rule for the z proposal density. Default is 0.5. |
| jump_w | Numeric; the jumping rule for the w proposal density. Default is 0.5. |
| pr_mean_beta | Numeric; the mean of the normal prior for beta. Default is 0. |
| pr_sd_beta | Numeric; the standard deviation of the normal prior for beta. Default is 1.0. |
| pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0. |
| pr_sd_theta | Numeric; the standard deviation of the normal prior for theta. Default is 1.0. |
| pr_mean_gamma | Numeric; mean of log normal prior for gamma. Default is 0.5. |
| pr_sd_gamma | Numeric; standard deviation of log normal prior for gamma. Default is 1.0. |
| pr_a_theta | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001. |
| pr_b_theta | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001. |
| missing.val | Numeric; a number to replace missing values. Default is 99. |
| verbose | Logical; If TRUE, MCMC samples are printed for each nprint. default value is FALSE. |
| fix_theta_sd | Logical; If TRUE, the standard deviation of the theta parameter is fixed. Default is FALSE. |

Details

lsirm1pl_mar models the probability of correct response by respondent j to item i with item effect β_i , respondent effect θ_j and the distance between latent position w_i of item i and latent position z_j of respondent j in the shared metric space, with γ represents the weight of the distance term:

$$logit(P(Y_{j,i} = 1 | \theta_j, \beta_i, \gamma, z_j, w_i)) = \theta_j + \beta_i - \gamma ||z_j - w_i||$$

Under the assumption of missing at random, the model takes the missing element into consideration in the sampling procedure. For the details of missing at random assumption and data augmentation, see References.

Isirm1pl_mar 21

Value

lsirm1pl_mar returns an object of list containing the following components:

data Data frame or matrix containing the variables in the model.

missing.val A number to replace missing values.

bic Numeric value with the corresponding BIC.

mcmc_inf Details about the number of MCMC iterations, burn-in periods, and thinning

intervals.

map_inf The log maximum a posteriori (MAP) value and the iteration number at which

this MAP value occurs.

beta_estimate Posterior estimates of the beta parameter.
theta_estimate Posterior estimates of the theta parameter.

sigma_theta_estimate

Posterior estimates of the standard deviation of theta.

gamma_estimate posterior estimates of gamma parameter.

z_estimate Posterior estimates of the z parameter.

w_estimate Posterior estimates of the w parameter.

imp_estimate Probability of imputating a missing value with 1.

beta Posterior samples of the beta parameter.
theta Posterior samples of the theta parameter.
gamma Posterior samples of the gamma parameter.

theta_sd Posterior samples of the standard deviation of theta.

z Posterior samples of the z parameter, represented as a 3-dimensional matrix

where the last axis denotes the dimension of the latent space.

w Posterior samples of the w parameter, represented as a 3-dimensional matrix

where the last axis denotes the dimension of the latent space.

z_raw Posterior samples of the z parameter without procrustes matching.w_raw Posterior samples of the w parameter without procrustes matching.

imp Imputation for missing Values using posterior samples.

accept_beta Acceptance ratio for the beta parameter.
accept_theta Acceptance ratio for the theta parameter.
accept_z Acceptance ratio for the z parameter.
accept_w Acceptance ratio for the w parameter.
accept_gamma Acceptance ratio for the gamma parameter.

References

Little, R. J., & Rubin, D. B. (2019). Statistical analysis with missing data (Vol. 793). John Wiley & Sons.

Examples

```
# generate example item response matrix
data     <- matrix(rbinom(500, size = 1, prob = 0.5),ncol=10,nrow=50)

# generate example missing indicator matrix
missing_mat     <- matrix(rbinom(500, size = 1, prob = 0.2),ncol=10,nrow=50)

# make missing value with missing indicator matrix
data[missing_mat==1] <- 99

lsirm_result <- lsirm1pl_mar(data)

# The code following can achieve the same result.
lsirm_result <- lsirm(data ~ lsirm1pl(spikenslab = FALSE, fixed_gamma = FALSE, missing_data = 'mar', missing.val = 99))</pre>
```

lsirm1pl_mar_ss

1PL LSIRM with model selection approach for missing at random data.

Description

Isirm1pl_mar_ss is used to fit 1PL LSIRM with model selection approach based on spike-and-slab priors in incomplete data assumed to be missing at random. Isirm1pl_mar_ss factorizes item response matrix into column-wise item effect, row-wise respondent effect and further embeds interaction effect in a latent space, while considering the missing element under the assumption of missing at random. The resulting latent space provides an interaction map that represents interactions between respondents and items.

```
lsirm1pl_mar_ss(
  data,
  ndim = 2,
  niter = 15000,
  nburn = 2500,
  nthin = 5,
  nprint = 500,
  jump\_beta = 0.4,
  jump\_theta = 1,
  jump\_gamma = 1,
  jump_z = 0.5,
  jump_w = 0.5,
  pr_mean_beta = 0,
  pr_sd_beta = 1,
  pr_mean_theta = 0,
  pr_sd_theta = 1,
```

```
pr_spike_mean = -3,
pr_spike_sd = 1,
pr_slab_mean = 0.5,
pr_slab_sd = 1,
pr_a_theta = 0.001,
pr_b_theta = 0.001,
pr_xi_a = 1,
pr_xi_b = 1,
missing.val = 99,
verbose = FALSE,
fix_theta_sd = FALSE
```

Arguments

| data | Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item. |
|---------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| ndim | Integer; the dimension of the latent space. Default is 2. |
| niter | Integer; the total number of MCMC iterations to run. Default is 15000. |
| nburn | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500. |
| nthin | Integer; the number of MCMC iterations to thin. Default is 5. |
| nprint | Integer; the interval at which MCMC samples are displayed during execution. Default is 500. |
| jump_beta | Numeric; the jumping rule for the beta proposal density. Default is 0.4. |
| jump_theta | Numeric; the jumping rule for the theta proposal density. Default is 1.0. |
| jump_gamma | Numeric; the jumping rule for the theta proposal density. Default is 1.0. |
| jump_z | Numeric; the jumping rule for the z proposal density. Default is 0.5. |
| jump_w | Numeric; the jumping rule for the w proposal density. Default is 0.5. |
| pr_mean_beta | Numeric; the mean of the normal prior for beta. Default is 0. |
| pr_sd_beta | Numeric; the standard deviation of the normal prior for beta. Default is 1.0. |
| pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0. |
| pr_sd_theta | Numeric; the standard deviation of the normal prior for theta. Default is 1.0. |
| pr_spike_mean | Numeric; the mean of spike prior for log gamma. Default is -3. |
| pr_spike_sd | Numeric; the standard deviation of spike prior for log gamma. Default is 1. |
| pr_slab_mean | Numeric; the mean of spike prior for log gamma. Default is 0.5. |
| pr_slab_sd | Numeric; the standard deviation of spike prior for log gamma. Default is is 1. |
| pr_a_theta | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001. |
| pr_b_theta | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001 . |
| | |

pr_xi_a

Numeric; the first shape parameter of beta prior for latent variable xi. Default is 1.

pr_xi_b

Numeric; the second shape parameter of beta prior for latent variable xi. Default is 1.

missing.val

Numeric; a number to replace missing values. Default is 99.

verbose

Logical; If TRUE, MCMC samples are printed for each nprint. Default is FALSE.

fix_theta_sd Logical; If TRUE, the standard deviation of the theta parameter is fixed. Default

is FALSE.

Details

lsirm1pl_mar_ss models the probability of correct response by respondent j to item i with item effect β_i , respondent effect θ_j and the distance between latent position w_i of item i and latent position z_j of respondent j in the shared metric space, with γ represents the weight of the distance term:

$$logit(P(Y_{j,i} = 1 | \theta_j, \beta_i, \gamma, z_j, w_i)) = \theta_j + \beta_i - \gamma ||z_j - w_i||$$

Under the assumption of missing at random, the model takes the missing element into consideration in the sampling procedure. For the details of missing at random assumption and data augmentation, see References. lsirm1pl_mar_ss model include model selection approach based on spike-and-slab priors for log gamma. For detail of spike-and-slab priors, see References.

Value

lsirm1pl_mar_ss returns an object of list containing the following components:

data Data frame or matrix containing the variables in the model.

missing.val A number to replace missing values.

bic Numeric value with the corresponding BIC.

mcmc_inf Details about the number of MCMC iterations, burn-in periods, and thinning

intervals.

map_inf The log maximum a posteriori (MAP) value and the iteration number at which

this MAP value occurs.

beta_estimate Posterior estimates of the beta parameter.
theta_estimate Posterior estimates of the theta parameter.

sigma_theta_estimate

Posterior estimates of the standard deviation of theta.

gamma_estimate posterior estimates of gamma parameter.

z_estimate Posterior estimates of the z parameter.

w_estimate Posterior estimates of the w parameter.

beta Posterior samples of the beta parameter.

theta Posterior samples of the theta parameter.

gamma Posterior samples of the gamma parameter.

| theta_sd | Posterior samples of the standard deviation of theta. |
|--------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| Z | Posterior samples of the z parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space. |
| W | Posterior samples of the w parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space. |
| z_raw | Posterior samples of the z parameter without procrustes matching. |
| w_raw | Posterior samples of the w parameter without procrustes matching. |
| pi | Posterior samples of phi which is indicator of spike and slab prior. If phi is 1, log gamma follows the slab prior, otherwise follows the spike prior. |
| imp | Imputation for missing Values using posterior samples. |
| accept_beta | Acceptance ratio for the beta parameter. |
| accept_theta | Acceptance ratio for the theta parameter. |
| accept_z | Acceptance ratio for the z parameter. |
| accept_w | Acceptance ratio for the w parameter. |
| accept_gamma | Acceptance ratio for the gamma parameter. |
| pi_estimate | Posterior estimation of phi. inclusion probability of gamma. if estimation of phi is less than 0.5 , choose Rasch model with gamma = 0 , otherwise latent space model with gamma > 0 . |
| imp_estimate | Probability of imputating a missing value with 1. |

References

Little, R. J., & Rubin, D. B. (2019). Statistical analysis with missing data (Vol. 793). John Wiley & Sons. Ishwaran, H., & Rao, J. S. (2005). Spike and slab variable selection: frequentist and Bayesian strategies. The Annals of Statistics, 33(2), 730-773.

Examples

26 lsirm1pl_mcar

lsirm1pl_mcar

1PL LSIRM for missing completely at random data.

Description

lsirm1pl_mcar is used to fit 1PL LSIRM in incomplete data assumed to be missing completely at random. lsirm1pl_mcar factorizes item response matrix into column-wise item effect, row-wise respondent effect and further embeds interaction effect in a latent space, while ignoring the missing element under the assumption of missing completely at random. The resulting latent space provides an interaction map that represents interactions between respondents and items.

Usage

```
lsirm1pl_mcar(
  data,
  ndim = 2,
  niter = 15000,
  nburn = 2500,
  nthin = 5,
  nprint = 500,
  jump\_beta = 0.4,
  jump\_theta = 1,
  jump_gamma = 0.025,
  jump_z = 0.5,
  jump_w = 0.5,
  pr_mean_beta = 0,
  pr_sd_beta = 1,
  pr_mean_theta = 0,
  pr_sd_theta = 1,
  pr_mean_gamma = 0.5,
  pr_sd_gamma = 1,
 pr_a_theta = 0.001,
  pr_b_t = 0.001,
 missing.val = 99,
  verbose = FALSE,
  fix_{theta_sd} = FALSE
)
```

Arguments

| data | Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item. |
|-------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| ndim | Integer; the dimension of the latent space. Default is 2. |
| niter | Integer; the total number of MCMC iterations to run. Default is 15000. |

lsirm1pl_mcar 27

| nburn | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500. |
|---------------|---------------------------------------------------------------------------------------------------------|
| nthin | Integer; the number of MCMC iterations to thin. Default is 5. |
| nprint | Integer; the interval at which MCMC samples are displayed during execution. Default is 500. |
| jump_beta | Numeric; the jumping rule for the beta proposal density. Default is 0.4. |
| jump_theta | Numeric; the jumping rule for the theta proposal density. Default is 1.0. |
| jump_gamma | Numeric; the jumping rule for the gamma proposal density. Default is 0.025. |
| jump_z | Numeric; the jumping rule for the z proposal density. Default is 0.5. |
| jump_w | Numeric; the jumping rule for the w proposal density. Default is 0.5. |
| pr_mean_beta | Numeric; the mean of the normal prior for beta. Default is 0. |
| pr_sd_beta | Numeric; the standard deviation of the normal prior for beta. Default is 1.0. |
| pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0. |
| pr_sd_theta | Numeric; the standard deviation of the normal prior for theta. Default is 1.0. |
| pr_mean_gamma | Numeric; mean of log normal prior for gamma. Default is 0.5. |
| pr_sd_gamma | Numeric; standard deviation of log normal prior for gamma. Default is 1.0. |
| pr_a_theta | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001 . |
| pr_b_theta | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001 . |
| missing.val | Numeric; A number to replace missing values. Default is 99. |
| verbose | Logical; If TRUE, MCMC samples are printed for each nprint. Default is FALSE. |
| fix_theta_sd | Logical; If TRUE, the standard deviation of the theta parameter is fixed. Default is FALSE. |

Details

lsirm1pl_mcar models the probability of correct response by respondent j to item i with item effect β_i , respondent effect θ_j and the distance between latent position w_i of item i and latent position z_j of respondent j in the shared metric space, with γ represents the weight of the distance term:

$$logit(P(Y_{j,i} = 1 | \theta_j, \beta_i, \gamma, z_j, w_i)) = \theta_j + \beta_i - \gamma ||z_j - w_i||$$

Under the assumption of missing completely at random, the model ignores the missing element in doing inference. For the details of missing completely at random assumption and data augmentation, see References.

Value

lsirm1pl_mcar returns an object of list containing the following components:

data A data frame or matrix containing the variables used in the model.

missing.val A number to replace missing values.

28 Isirm1pl_mcar

Numeric value with the corresponding BIC. bic mcmc_inf Details about the number of MCMC iterations, burn-in periods, and thinning intervals. map_inf The log maximum a posteriori (MAP) value and the iteration number at which this MAP value occurs. beta_estimate Posterior estimates of the beta parameter. theta_estimate Posterior estimates of the theta parameter. sigma_theta_estimate Posterior estimates of the standard deviation of theta. gamma_estimate Posterior estimates of gamma parameter. Posterior estimates of the z parameter. z_estimate Posterior estimates of the w parameter. w_estimate Posterior samples of the beta parameter. beta theta Posterior samples of the theta parameter. Posterior samples of the standard deviation of theta. theta_sd Posterior samples of the gamma parameter. gamma Posterior samples of the z parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space. Posterior samples of the w parameter, represented as a 3-dimensional matrix W where the last axis denotes the dimension of the latent space. Posterior samples of the z parameter without procrustes matching. z_raw w_raw Posterior samples of the w parameter without procrustes matching. accept_beta Acceptance ratio for the beta parameter. accept_theta Acceptance ratio for the theta parameter.

accept_theta Acceptance ratio for the theta parameter.
accept_z Acceptance ratio for the z parameter.
accept_w Acceptance ratio for the w parameter.
accept_gamma Acceptance ratio for the gamma parameter.

References

Little, R. J., & Rubin, D. B. (2019). Statistical analysis with missing data (Vol. 793). John Wiley & Sons.

Examples

```
# generate example item response matrix
data <- matrix(rbinom(500, size = 1, prob = 0.5),ncol=10,nrow=50)
# generate example missing indicator matrix
missing_mat <- matrix(rbinom(500, size = 1, prob = 0.2),ncol=10,nrow=50)
# make missing value with missing indicator matrix
data[missing_mat==1] <- 99</pre>
```

```
lsirm_result <- lsirm1pl_mcar(data)

# The code following can achieve the same result.
lsirm_result <- lsirm(data ~ lsirm1pl(spikenslab = FALSE, fixed_gamma = FALSE, missing_data = 'mcar', missing.val = 99))</pre>
```

lsirm1pl_mcar_ss

1PL LSIRM with model selection approach for missing completely at random data.

Description

lsirm1pl_mcar_ss is used to fit 1PL LSIRM with model selection approach based on spike-and-slab priors in incomplete data assumed to be missing completely at random. lsirm1pl_mcar_ss factorizes item response matrix into column-wise item effect, row-wise respondent effect and further embeds interaction effect in a latent space, while ignoring the missing element under the assumption of missing completely at random. The resulting latent space provides an interaction map that represents interactions between respondents and items.

```
lsirm1pl_mcar_ss(
  data,
  ndim = 2,
  niter = 15000,
  nburn = 2500,
  nthin = 5,
  nprint = 500,
  jump_beta = 0.4,
  jump\_theta = 1,
  jump_gamma = 1,
  jump_z = 0.5,
  jump_w = 0.5,
  pr_mean_beta = 0,
  pr_sd_beta = 1,
 pr_mean_theta = 0,
  pr_sd_theta = 1,
  pr_spike_mean = -3,
  pr_spike_sd = 1,
 pr_slab_mean = 0.5,
  pr_slab_sd = 1,
  pr_a_theta = 0.001,
  pr_b_t = 0.001,
 pr_xi_a = 1,
  pr_xi_b = 1,
 missing.val = 99,
```

```
verbose = FALSE,
fix_theta_sd = FALSE
)
```

Arguments

| data | Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item. |
|---------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| ndim | Integer; the dimension of the latent space. Default is 2. |
| niter | Integer; the total number of MCMC iterations to run. Default is 15000. |
| nburn | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500. |
| nthin | Integer; the number of MCMC iterations to thin. Default is 5. |
| nprint | Integer; the interval at which MCMC samples are displayed during execution. Default is 500. |
| jump_beta | Numeric; the jumping rule for the beta proposal density. Default is 0.4. |
| jump_theta | Numeric; the jumping rule for the theta proposal density. Default is 1.0. |
| jump_gamma | Numeric; the jumping rule for the theta proposal density. Default is 1.0. |
| jump_z | Numeric; the jumping rule for the z proposal density. Default is 0.5. |
| jump_w | Numeric; the jumping rule for the w proposal density. Default is 0.5. |
| pr_mean_beta | Numeric; the mean of the normal prior for beta. Default is 0. |
| pr_sd_beta | Numeric; the standard deviation of the normal prior for beta. Default is 1.0. |
| pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0. |
| pr_sd_theta | Numeric; the standard deviation of the normal prior for theta. Default is 1.0. |
| pr_spike_mean | Numeric; the mean of spike prior for log gamma. Default is -3. |
| pr_spike_sd | Numeric; the standard deviation of spike prior for log gamma. Default is 1. |
| pr_slab_mean | Numeric; the mean of spike prior for log gamma. Default is 0.5. |
| pr_slab_sd | Numeric; the standard deviation of spike prior for log gamma. Default is 1. |
| pr_a_theta | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001 . |
| pr_b_theta | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001 . |
| pr_xi_a | Numeric; the first shape parameter of beta prior for latent variable xi. Default is 1. |
| pr_xi_b | Numeric; the second shape parameter of beta prior for latent variable xi. Default is 1. |
| missing.val | Numeric; a number to replace missing values. Default is 99. |
| verbose | Logical; If TRUE, MCMC samples are printed for each nprint. Default is FALSE. |
| fix_theta_sd | Logical; If TRUE, the standard deviation of the theta parameter is fixed. Default is FALSE. |
| | |

Details

lsirm1p1_mcar_ss models the probability of correct response by respondent j to item i with item effect β_i , respondent effect θ_j and the distance between latent position w_i of item i and latent position z_j of respondent j in the shared metric space, with γ represents the weight of the distance term:

$$logit(P(Y_{i,i} = 1 | \theta_i, \beta_i, \gamma, z_i, w_i)) = \theta_i + \beta_i - \gamma ||z_i - w_i||$$

Under the assumption of missing completely at random, the model ignores the missing element in doing inference. For the details of missing completely at random assumption and data augmentation, see References. lsirm1pl_mcar_ss model include model selection approach based on spike-and-slab priors for log gamma. For detail of spike-and-slab priors, see References.

Value

lsirm1pl_mcar_ss returns an object of list containing the following components:

data Data frame or matrix containing the variables in the model.

missing.val A number to replace missing values.

bic Numeric value with the corresponding BIC.

mcmc_inf Details about the number of MCMC iterations, burn-in periods, and thinning

intervals.

map_inf The log maximum a posteriori (MAP) value and the iteration number at which

this MAP value occurs.

beta_estimate Posterior estimates of the beta parameter.

theta_estimate Posterior estimates of the theta parameter.

sigma_theta_estimate

Posterior estimates of the standard deviation of theta.

 ${\tt gamma_estimate} \ \ posterior \ estimates \ of \ gamma \ parameter.$

z_estimate Posterior estimates of the z parameter.
w_estimate Posterior estimates of the w parameter.
beta Posterior samples of the beta parameter.
theta Posterior samples of the theta parameter.
Posterior samples of the gamma parameter.

theta_sd Posterior samples of the standard deviation of theta.

z Posterior samples of the z parameter, represented as a 3-dimensional matrix

where the last axis denotes the dimension of the latent space.

w Posterior samples of the w parameter, represented as a 3-dimensional matrix

where the last axis denotes the dimension of the latent space.

z_raw Posterior samples of the z parameter without procrustes matching.
w_raw Posterior samples of the w parameter without procrustes matching.

pi Posterior samples of phi which is indicator of spike and slab prior. If phi is 1,

log gamma follows the slab prior, otherwise follows the spike prior.

accept_theta Acceptance ratio for the theta parameter.

accept_z Acceptance ratio for the z parameter.

accept_w Acceptance ratio for the w parameter.

accept_gamma Acceptance ratio for the gamma parameter.

References

Little, R. J., & Rubin, D. B. (2019). Statistical analysis with missing data (Vol. 793). John Wiley & Sons. Ishwaran, H., & Rao, J. S. (2005). Spike and slab variable selection: frequentist and Bayesian strategies. The Annals of Statistics, 33(2), 730-773.

Examples

```
# generate example item response matrix
data <- matrix(rbinom(500, size = 1, prob = 0.5),ncol=10,nrow=50)

# generate example missing indicator matrix
missing_mat <- matrix(rbinom(500, size = 1, prob = 0.2),ncol=10,nrow=50)

# make missing value with missing indicator matrix
data[missing_mat==1] <- 99

lsirm_result <- lsirm1pl_mcar_ss(data)

# The code following can achieve the same result.
lsirm_result <- lsirm(data ~ lsirm1pl(spikenslab = TRUE, fixed_gamma = FALSE, missing_data = 'mcar', missing.val = 99))</pre>
```

```
lsirm1pl_normal_fixed_gamma
```

1PL LSIRM fixing gamma to 1 with normal likelihood

Description

lsirm1pl_normal_fixed_gamma is used to fit 1PL LSIRM for continuous variable with gamma fixed to 1. lsirm1pl_normal_fixed_gamma factorizes continuous item response matrix into column-wise item effect, row-wise respondent effect and further embeds interaction effect in a latent space, while ignoring the missing element under the assumption of missing at random. The resulting latent space provides an interaction map that represents interactions between respondents and items.

```
lsirm1pl_normal_fixed_gamma(
  data,
  ndim = 2,
  niter = 15000,
  nburn = 2500,
```

```
nthin = 5,
 nprint = 500,
  jump\_beta = 0.4,
  jump\_theta = 1,
  jump_z = 0.5,
  jump_w = 0.5,
 pr_mean_beta = 0,
 pr_sd_beta = 1,
 pr_mean_theta = 0,
 pr_sd_theta = 1,
 pr_a_theta = 0.001,
 pr_b_teta = 0.001,
 pr_a_{eps} = 0.001,
 pr_b_{eps} = 0.001,
 verbose = FALSE,
 fix_{theta_sd} = FALSE
)
```

Arguments

data

| data | resents a respondent, and each column contains responses to the corresponding item. |
|---------------|--------------------------------------------------------------------------------------------------------|
| ndim | Integer; the dimension of the latent space. Default is 2. |
| niter | Integer; the total number of MCMC iterations to run. Default is 15000. |
| nburn | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500. |
| nthin | Integer; the number of MCMC iterations to thin. Default is 5. |
| nprint | Integer; the interval at which MCMC samples are displayed during execution. Default is 500. |
| jump_beta | Numeric; the jumping rule for the beta proposal density. Default is 0.4. |
| jump_theta | Numeric; the jumping rule for the theta proposal density. Default is 1.0. |
| jump_z | Numeric; the jumping rule for the z proposal density. Default is 0.5. |
| jump_w | Numeric; the jumping rule for the w proposal density. Default is 0.5. |
| pr_mean_beta | Numeric; the mean of the normal prior for beta. Default is 0. |
| pr_sd_beta | Numeric; the standard deviation of the normal prior for beta. Default is 1.0. |
| pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0. |
| pr_sd_theta | Numeric; the standard deviation of the normal prior for theta. Default is 1.0. |
| pr_a_theta | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001. |
| pr_b_theta | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001. |
| pr_a_eps | Numeric; the shape parameter of inverse gamma prior for variance of data likelihood. Default is 0.001. |
| | |

Matrix; a binary or continuous item response matrix for analysis. Each row rep-

pr_b_eps Numeric; the scale parameter of inverse gamma prior for variance of data likeli-

hood Default is 0.001.

verbose Logical; If TRUE, MCMC samples are printed for each nprint. default value

is FALSE.

fix_theta_sd Logical; If TRUE, the standard deviation of the theta parameter is fixed. Default

is FALSE.

Details

lsirm1pl_normal_fixed_gamma models the continuous value of response by respondent j to item i with item effect β_i , respondent effect θ_j and the distance between latent position w_i of item i and latent position z_j of respondent j in the shared metric space:

$$Y_{i,i} = \theta_i + \beta_i - ||z_i - w_i|| + e_{i,i}$$

where the error $e_{i,i} \sim N(0, \sigma^2)$.

Value

lsirm1pl_normal_fixed_gamma returns an object of list containing the following components:

data A data frame or matrix containing the variables used in the model.

bic A numeric value representing the Bayesian Information Criterion (BIC).

mcmc_inf Details about the number of MCMC iterations, burn-in periods, and thinning

intervals.

map_inf The log maximum a posteriori (MAP) value and the iteration number at which

this MAP value occurs.

beta_estimate Posterior estimates of the beta parameter.

theta_estimate Posterior estimates of the theta parameter.

sigma_theta_estimate

Posterior estimates of the standard deviation of theta.

z_estimate Posterior estimates of the z parameter.
 w_estimate Posterior estimates of the w parameter.
 beta Posterior samples of the beta parameter.
 theta Posterior samples of the theta parameter.

theta_sd Posterior samples of the standard deviation of theta.

z Posterior samples of the z parameter, represented as a 3-dimensional matrix

where the last axis denotes the dimension of the latent space.

w Posterior samples of the w parameter, represented as a 3-dimensional matrix

where the last axis denotes the dimension of the latent space.

z_raw Posterior samples of the z parameter without procrustes matching.w_raw Posterior samples of the w parameter without procrustes matching.

accept_beta Acceptance ratio for the beta parameter.

accept_theta Acceptance ratio for the theta parameter.

```
accept_z Acceptance ratio for the z parameter.

accept_w Acceptance ratio for the w parameter.

sigma_estimate Posterior estimates of the standard deviation.

sigma Posterior samples of the standard deviation.
```

Examples

```
lsirm1pl_normal_fixed_gamma_mar
```

1PL LSIRM fixing gamma to 1 with normal likelihood for missing at random data.

Description

lsirm1pl_normal_fixed_gamma_mar is used to fit 1PL LSIRM for continuous variable with gamma fixed to 1 in incomplete data assumed to be missing at random.

lsirm1pl_normal_fixed_gamma_mar factorizes continuous item response matrix into column-wise item effect, row-wise respondent effect and further embeds interaction effect in a latent space, while considering the missing element under the assumption of missing at random. The resulting latent space provides an interaction map that represents interactions between respondents and items.

```
lsirm1pl_normal_fixed_gamma_mar(
  data,
  ndim = 2,
  niter = 15000,
  nburn = 2500,
  nthin = 5,
  nprint = 500,
  jump_beta = 0.4,
  jump_theta = 1,
```

```
jump_z = 0.5,
jump_w = 0.5,
pr_mean_beta = 0,
pr_sd_beta = 1,
pr_mean_theta = 0,
pr_sd_theta = 1,
pr_a_theta = 0.001,
pr_b_theta = 0.001,
pr_b_eps = 0.001,
missing.val = 99,
verbose = FALSE,
fix_theta_sd = FALSE
```

Arguments

| data | Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item. |
|---------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| ndim | Integer; the dimension of the latent space. Default is 2. |
| niter | Integer; the total number of MCMC iterations to run. Default is 15000. |
| nburn | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500. |
| nthin | Integer; the number of MCMC iterations to thin. Default is 5. |
| nprint | Integer; the interval at which MCMC samples are displayed during execution. Default is 500. |
| jump_beta | Numeric; the jumping rule for the beta proposal density. Default is 0.4. |
| jump_theta | Numeric; the jumping rule for the theta proposal density. Default is 1.0. |
| jump_z | Numeric; the jumping rule for the z proposal density. Default is 0.5. |
| jump_w | Numeric; the jumping rule for the w proposal density. Default is 0.5. |
| pr_mean_beta | Numeric; the mean of the normal prior for beta. Default is 0. |
| pr_sd_beta | Numeric; the standard deviation of the normal prior for beta. Default is 1.0. |
| pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0. |
| pr_sd_theta | Numeric; the standard deviation of the normal prior for theta. Default is 1.0. |
| pr_a_theta | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001 . |
| pr_b_theta | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001 . |
| pr_a_eps | Numeric; the shape parameter of inverse gamma prior for variance of data likelihood. Default is 0.001. |
| pr_b_eps | Numeric; the scale parameter of inverse gamma prior for variance of data likelihood Default is 0.001. |

missing.val Numeric; a number to replace missing values. Default is 99.

verbose Logical; If TRUE, MCMC samples are printed for each nprint. Default is

FALSE.

fix_theta_sd Logical; If TRUE, the standard deviation of the theta parameter is fixed. Default

is FALSE.

Details

lsirm1pl_normal_fixed_gamma_mar models the continuous value of response by respondent j to item i with item effect β_i , respondent effect θ_j and the distance between latent position w_i of item i and latent position z_j of respondent j in the shared metric space:

$$Y_i, i = \theta_i + \beta_i - ||z_i - w_i|| + e_{ii}$$

where the error $e_j i \ N(0, \sigma^2)$ Under the assumption of missing at random, the model takes the missing element into consideration in the sampling procedure. For the details of missing at random assumption and data augmentation, see References.

Value

lsirm1pl_normal_fixed_gamma_mar returns an object of list containing the following components:

data Data frame or matrix containing the variables in the model.

missing.val A number to replace missing values.

bic Numeric value with the corresponding BIC.

mcmc_inf Details about the number of MCMC iterations, burn-in periods, and thinning

intervals.

map_inf The log maximum a posteriori (MAP) value and the iteration number at which

this MAP value occurs.

beta_estimate Posterior estimates of the beta parameter.

theta_estimate Posterior estimates of the theta parameter.

sigma_theta_estimate

Posterior estimates of the standard deviation of theta.

z_estimate Posterior estimates of the z parameter. w_estimate Posterior estimates of the w parameter.

imp_estimate Probability of imputating a missing value with 1.

beta Posterior samples of the beta parameter.
theta Posterior samples of the theta parameter.

theta_sd Posterior samples of the standard deviation of theta.

z Posterior samples of the z parameter, represented as a 3-dimensional matrix

where the last axis denotes the dimension of the latent space.

w Posterior samples of the w parameter, represented as a 3-dimensional matrix

where the last axis denotes the dimension of the latent space.

Posterior samples of the z parameter without procrustes matching. z_raw Posterior samples of the w parameter without procrustes matching. w_raw imp Imputation for missing Values using posterior samples. accept_beta Acceptance ratio for the beta parameter. Acceptance ratio for the theta parameter. accept_theta Acceptance ratio for the z parameter. accept_z Acceptance ratio for the w parameter. accept_w sigma_estimate Posterior estimates of the standard deviation. Posterior samples of the standard deviation. sigma

Examples

```
lsirm1pl_normal_fixed_gamma_mcar
```

1PL LSIRM fixing gamma to 1 with normal likelihood for missing completely at random data.

Description

lsirm1pl_normal_fixed_gamma_mcar is used to fit 1PL LSIRM for continuous variable with gamma fixed to 1 in incomplete data assumed to be missing completely at random.

lsirm1pl_normal_fixed_gamma_mcar factorizes continuous item response matrix into column-wise item effect, row-wise respondent effect and further embeds interaction effect in a latent space, while ignoring the missing element under the assumption of missing completely at random. The resulting latent space provides an interaction map that represents interactions between respondents and items.

Usage

```
lsirm1pl_normal_fixed_gamma_mcar(
  data,
  ndim = 2,
  niter = 15000,
  nburn = 2500,
  nthin = 5,
  nprint = 500,
  jump\_beta = 0.4,
  jump\_theta = 1,
  jump_z = 0.5,
  jump_w = 0.5,
  pr_mean_beta = 0,
 pr_sd_beta = 1,
  pr_mean_theta = 0,
 pr_sd_theta = 1,
 pr_a_theta = 0.001,
 pr_b_t = 0.001,
  pr_a_{eps} = 0.001,
 pr_b_{eps} = 0.001,
 missing.val = 99,
 verbose = FALSE,
  fix_{theta_sd} = FALSE
)
```

| data | Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item. |
|---------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| ndim | Integer; the dimension of the latent space. Default is 2. |
| niter | Integer; the total number of MCMC iterations to run. Default is 15000. |
| nburn | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500. |
| nthin | Integer; the number of MCMC iterations to thin. Default is 5. |
| nprint | Integer; the interval at which MCMC samples are displayed during execution. Default is 500. |
| jump_beta | Numeric; the jumping rule for the beta proposal density. Default is 0.4. |
| jump_theta | Numeric; the jumping rule for the theta proposal density. Default is 1.0. |
| jump_z | Numeric; the jumping rule for the z proposal density. Default is 0.5. |
| jump_w | Numeric; the jumping rule for the w proposal density. Default is 0.5. |
| pr_mean_beta | Numeric; the mean of the normal prior for beta. Default is 0. |
| pr_sd_beta | Numeric; the standard deviation of the normal prior for beta. Default is 1.0. |
| pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0. |

| pr_sd_theta | Numeric; the standard deviation of the normal prior for theta. Default is 1.0. |
|--------------|--------------------------------------------------------------------------------------------------------|
| pr_a_theta | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001. |
| pr_b_theta | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001. |
| pr_a_eps | Numeric; the shape parameter of inverse gamma prior for variance of data likelihood. Default is 0.001. |
| pr_b_eps | Numeric; the scale parameter of inverse gamma prior for variance of data likelihood. Default is 0.001. |
| missing.val | Numeric; a number to replace missing values. Default is 99. |
| verbose | Logical; If TRUE, MCMC samples are printed for each nprint. Default is FALSE. |
| fix_theta_sd | Logical; If TRUE, the standard deviation of the theta parameter is fixed. Default is FALSE. |

Details

lsirm1pl_normal_fixed_gamma_mcar models the continuous value of response by respondent j to item i with item effect β_i , respondent effect θ_j and the distance between latent position w_i of item i and latent position z_j of respondent j in the shared metric space:

$$Y_{j,i} = \theta_j + \beta_i - ||z_j - w_i|| + e_{j,i}$$

where the error $e_{j,i} \sim N(0, \sigma^2)$ Under the assumption of missing completely at random, the model ignores the missing element in doing inference. For the details of missing completely at random assumption and data augmentation, see References.

Value

lsirm1pl_normal_fixed_gamma_mcar returns an object of list containing the following components:

data Data frame or matrix containing the variables in the model.

missing.val A number to replace missing values.

bic Numeric value with the corresponding BIC.

mcmc_inf Details about the number of MCMC iterations, burn-in periods, and thinning

intervals.

map_inf The log maximum a posteriori (MAP) value and the iteration number at which

this MAP value occurs.

beta_estimate Posterior estimates of the beta parameter.

theta_estimate Posterior estimates of the theta parameter.

 $sigma_theta_estimate$

Posterior estimates of the standard deviation of theta.

z_estimate Posterior estimates of the z parameter.w_estimate Posterior estimates of the w parameter.

Isirm1pl_normal_mar 41

| beta | Posterior samples of the beta parameter. |
|----------------|--------------------------------------------------------------------------------------------------------------------------------------------|
| theta | Posterior samples of the theta parameter. |
| theta_sd | Posterior samples of the standard deviation of theta. |
| Z | Posterior samples of the z parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space. |
| W | Posterior samples of the w parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space. |
| z_raw | Posterior samples of the z parameter without procrustes matching. |
| w_raw | Posterior samples of the w parameter without procrustes matching. |
| accept_beta | Acceptance ratio for the beta parameter. |
| accept_theta | Acceptance ratio for the theta parameter. |
| accept_z | Acceptance ratio for the z parameter. |
| accept_w | Acceptance ratio for the w parameter. |
| sigma_estimate | Posterior estimates of the standard deviation. |
| sigma | Posterior samples of the standard deviation. |

Examples

lsirm1pl_normal_mar

1PL LSIRM with normal likelihood for missing at random data.

Description

lsirm1pl_normal_mar is used to fit LSIRM for continuous variable with 1pl in incomplete data assumed to be missing at random. lsirm1pl_normal_mar factorizes continuous item response matrix into column-wise item effect, row-wise respondent effect and further embeds interaction effect in a latent space, while considering the missing element under the assumption of missing at random. The resulting latent space provides an interaction map that represents interactions between respondents and items.

Usage

```
lsirm1pl_normal_mar(
  data,
  ndim = 2,
  niter = 15000,
  nburn = 2500,
  nthin = 5,
  nprint = 500,
  jump\_beta = 0.4,
  jump\_theta = 1,
  jump_gamma = 1,
  jump_z = 0.5,
  jump_w = 0.5,
  pr_mean_beta = 0,
  pr_sd_beta = 1,
  pr_mean_theta = 0,
  pr_sd_theta = 1,
  pr_mean_gamma = 0.5,
  pr_sd_gamma = 1,
  pr_a_theta = 0.001,
 pr_b_teta = 0.001,
 pr_a_{eps} = 0.001,
  pr_b_{eps} = 0.001,
 missing.val = 99,
 verbose = FALSE,
  fix_{theta_sd} = FALSE
)
```

| data | Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item. |
|------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| ndim | Integer; the dimension of the latent space. Default is 2. |
| niter | Integer; the total number of MCMC iterations to run. Default is 15000. |
| nburn | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500. |
| nthin | Integer; the number of MCMC iterations to thin. Default is 5. |
| nprint | Integer; the interval at which MCMC samples are displayed during execution. Default is 500. |
| jump_beta | Numeric; the jumping rule for the beta proposal density. Default is 0.4. |
| jump_theta | Numeric; the jumping rule for the theta proposal density. Default is 1.0. |
| jump_gamma | Numeric; the jumping rule for the gamma proposal density. Default is 0.025 |
| jump_z | Numeric; the jumping rule for the z proposal density. Default is 0.5. |
| jump_w | Numeric; the jumping rule for the w proposal density. Default is 0.5. |

| pr_mean_beta | Numeric; the mean of the normal prior for beta. Default is 0. |
|---------------|-----------------------------------------------------------------------------------------------------------|
| pr_sd_beta | Numeric; the standard deviation of the normal prior for beta. Default is 1.0. |
| pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0. |
| pr_sd_theta | Numeric; the standard deviation of the normal prior for theta. Default is 1.0. |
| pr_mean_gamma | Numeric; mean of log normal prior for gamma. Default is 0.5. |
| pr_sd_gamma | Numeric; standard deviation of log normal prior for gamma. Default is 1.0. |
| pr_a_theta | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001 . |
| pr_b_theta | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001 . |
| pr_a_eps | Numeric; the shape parameter of inverse gamma prior for variance of data likelihood. Default is $0.001.$ |
| pr_b_eps | Numeric; the scale parameter of inverse gamma prior for variance of data likelihood. Default is 0.001 . |
| missing.val | Numeric; a number to replace missing values. Default is 99. |
| verbose | Logical; If TRUE, MCMC samples are printed for each nprint. Default is FALSE. |
| fix_theta_sd | Logical; If TRUE, the standard deviation of the theta parameter is fixed. Default is FALSE. |
| | |

Details

lsirm1pl_normal_mar models the continuous value of response by respondent j to item i with item effect β_i , respondent effect θ_j and the distance between latent position w_i of item i and latent position z_j of respondent j in the shared metric space, with γ represents the weight of the distance term:

$$Y_j, i = \theta_j + \beta_i - \gamma ||z_j - w_i|| + e_{ji}$$

where the error $e_{ji} \sim N(0, \sigma^2)$ Under the assumption of missing at random, the model takes the missing element into consideration in the sampling procedure. For the details of missing at random assumption and data augmentation, see References.

Value

lsirm1pl_normal_mar returns an object of list containing the following components:

data Data frame or matrix containing the variables in the model.

missing.val A number to replace missing values.

bic Numeric value with the corresponding BIC.

mcmc_inf Details about the number of MCMC iterations, burn-in periods, and thinning

intervals.

map_inf The log maximum a posteriori (MAP) value and the iteration number at which

this MAP value occurs.

beta_estimate Posterior estimates of the beta parameter.

 $\label{theta_estimate} \mbox{ Posterior estimates of the theta parameter.}$

sigma_theta_estimate

Posterior estimates of the standard deviation of theta.

gamma_estimate posterior estimates of gamma parameter.

z_estimate Posterior estimates of the z parameter.

w_estimate Posterior estimates of the w parameter.

imp_estimate Probability of imputating a missing value with 1.

beta Posterior samples of the beta parameter.
theta Posterior samples of the theta parameter.
gamma Posterior samples of the gamma parameter.

theta_sd Posterior samples of the standard deviation of theta.

z Posterior samples of the z parameter, represented as a 3-dimensional matrix

where the last axis denotes the dimension of the latent space.

w Posterior samples of the w parameter, represented as a 3-dimensional matrix

where the last axis denotes the dimension of the latent space.

z_rawPosterior samples of the z parameter without procrustes matching.w_rawPosterior samples of the w parameter without procrustes matching.

imp Imputation for missing Values using posterior samples.

accept_beta Acceptance ratio for the beta parameter.
accept_theta Acceptance ratio for the theta parameter.
accept_z Acceptance ratio for the z parameter.
accept_w Acceptance ratio for the w parameter.
accept_gamma Acceptance ratio for the gamma parameter.
sigma_estimate Posterior estimates of the standard deviation.
Posterior samples of the standard deviation.

References

Little, R. J., & Rubin, D. B. (2019). Statistical analysis with missing data (Vol. 793). John Wiley & Sons.

Examples

```
# generate example (continuous) item response matrix
data <- matrix(rnorm(500, mean = 0, sd = 1),ncol=10,nrow=50)

# generate example missing indicator matrix
missing_mat <- matrix(rbinom(500, size = 1, prob = 0.2),ncol=10,nrow=50)

# make missing value with missing indicator matrix
data[missing_mat==1] <- 99

lsirm_result <- lsirm1pl_normal_mar(data)</pre>
```

```
# The code following can achieve the same result.
lsirm_result <- lsirm(data ~ lsirm1pl(spikenslab = FALSE, fixed_gamma = FALSE,
missing_data ='mar', missing.val = 99))</pre>
```

lsirm1pl_normal_mar_ss

1PL LSIRM with normal likelihood and model selection approach for missing at random data.

Description

lsirm1pl_normal_mar_ss is used to fit 1PL LSIRM with model selection approach based on spike-and-slab priors for continuous variable with 1pl in incomplete data assumed to be missing at random. lsirm1pl_normal_mar_ss factorizes continuous item response matrix into column-wise item effect, row-wise respondent effect and further embeds interaction effect in a latent space, while considering the missing element under the assumption of missing at random. The resulting latent space provides an interaction map that represents interactions between respondents and items.

Usage

```
lsirm1pl_normal_mar_ss(
  data,
  ndim = 2,
  niter = 15000,
  nburn = 2500,
  nthin = 5,
  nprint = 500,
  jump\_beta = 0.4,
  jump\_theta = 1,
  jump_gamma = 1,
  jump_z = 0.5,
  jump_w = 0.5,
  pr_mean_beta = 0,
  pr_sd_beta = 1,
 pr_mean_theta = 0,
  pr_sd_theta = 1,
  pr_spike_mean = -3,
  pr_spike_sd = 1,
  pr_slab_mean = 0.5,
  pr_slab_sd = 1,
  pr_a_theta = 0.001,
  pr_b_t = 0.001,
  pr_a_{eps} = 0.001,
  pr_b_eps = 0.001,
  pr_xi_a = 0.001,
```

```
pr_xi_b = 0.001,
missing.val = 99,
verbose = FALSE,
fix_theta_sd = FALSE)
```

| data | Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item. |
|---------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| ndim | Integer; the dimension of the latent space. Default is 2. |
| niter | Integer; the total number of MCMC iterations to run. Default is 15000. |
| nburn | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500. |
| nthin | Integer; the number of MCMC iterations to thin. Default is 5. |
| nprint | Integer; the interval at which MCMC samples are displayed during execution. Default is 500. |
| jump_beta | Numeric; the jumping rule for the beta proposal density. Default is 0.4. |
| jump_theta | Numeric; the jumping rule for the theta proposal density. Default is 1.0. |
| jump_gamma | Numeric; the jumping rule for the theta proposal density. Default is 1.0. |
| jump_z | Numeric; the jumping rule for the z proposal density. Default is 0.5. |
| jump_w | Numeric; the jumping rule for the w proposal density. Default is 0.5. |
| pr_mean_beta | Numeric; the mean of the normal prior for beta. Default is 0. |
| pr_sd_beta | Numeric; the standard deviation of the normal prior for beta. Default is 1.0. |
| pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0. |
| pr_sd_theta | Numeric; the standard deviation of the normal prior for theta. Default is 1.0. |
| pr_spike_mean | Numeric; the mean of spike prior for log gamma. Default is -3. |
| pr_spike_sd | Numeric; the standard deviation of spike prior for log gamma. Default is 1. |
| pr_slab_mean | Numeric; the mean of spike prior for log gamma. Default is 0.5. |
| pr_slab_sd | Numeric; the standard deviation of spike prior for log gamma. Default is is 1. |
| pr_a_theta | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001 . |
| pr_b_theta | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001. |
| pr_a_eps | Numeric; the shape parameter of inverse gamma prior for variance of data likelihood. Default is 0.001. |
| pr_b_eps | Numeric; the scale parameter of inverse gamma prior for variance of data likelihood Default is 0.001. |
| pr_xi_a | Numeric; the first shape parameter of beta prior for latent variable xi. Default is 1. |

pr_xi_b Numeric; the second shape parameter of beta prior for latent variable xi. Default

is 1.

missing.val Numeric; a number to replace missing values. Default is 99.

verbose Logical; If TRUE, MCMC samples are printed for each nprint. Default is

FALSE.

fix_theta_sd Logical; If TRUE, the standard deviation of the theta parameter is fixed. Default

is FALSE.

Details

lsirm1pl_normal_mar_ss models the continuous value of response by respondent j to item i with item effect β_i , respondent effect θ_j and the distance between latent position w_i of item i and latent position z_j of respondent j in the shared metric space, with γ represents the weight of the distance term:

$$Y_{j,i} = \theta_j + \beta_i - \gamma ||z_j - w_i|| + e_{j,i}$$

where the error $e_{j,i} \sim N(0,\sigma^2)$ Under the assumption of missing at random, the model takes the missing element into consideration in the sampling procedure. For the details of missing at random assumption and data augmentation, see References. lsirm1pl_normal_mar_ss model include model selection approach based on spike-and-slab priors for log gamma. For detail of spike-and-slab priors, see References.

Value

lsirm1pl_normal_mar_ss returns an object of list containing the following components:

data Data frame or matrix containing the variables in the model.

missing.val A number to replace missing values.

bic Numeric value with the corresponding BIC.

mcmc_inf Details about the number of MCMC iterations, burn-in periods, and thinning

intervals.

map_inf The log maximum a posteriori (MAP) value and the iteration number at which

this MAP value occurs.

beta_estimate Posterior estimates of the beta parameter.

theta_estimate Posterior estimates of the theta parameter.

sigma_theta_estimate

Posterior estimates of the standard deviation of theta.

gamma_estimate posterior estimates of gamma parameter.

z_estimate Posterior estimates of the z parameter.

w_estimate Posterior estimates of the w parameter.

beta Posterior samples of the beta parameter.

theta Posterior samples of the theta parameter.

gamma Posterior samples of the gamma parameter.

theta_sd Posterior samples of the standard deviation of theta.

| Z | Posterior samples of the z parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space. |
|-------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| W | Posterior samples of the w parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space. |
| z_raw | Posterior samples of the z parameter without procrustes matching. |
| w_raw | Posterior samples of the w parameter without procrustes matching. |
| pi | Posterior samples of phi which is indicator of spike and slab prior. If phi is 1, log gamma follows the slab prior, otherwise follows the spike prior. |
| imp | Imputation for missing Values using posterior samples. |
| accept_beta | Acceptance ratio for the beta parameter. |
| accept_theta | Acceptance ratio for the theta parameter. |
| accept_z | Acceptance ratio for the z parameter. |
| accept_w | Acceptance ratio for the w parameter. |
| accept_gamma | Acceptance ratio for the gamma parameter. |
| pi_estimate | Posterior estimation of phi. inclusion probability of gamma. if estimation of phi is less than 0.5 , choose Rasch model with gamma = 0 , otherwise latent space model with gamma > 0 . |
| <pre>imp_estimate</pre> | Probability of imputating a missing value with 1. |
| sigma_estimate | Posterior estimates of the standard deviation. |
| sigma | Posterior samples of the standard deviation. |
| | |

References

Little, R. J., & Rubin, D. B. (2019). Statistical analysis with missing data (Vol. 793). John Wiley & Sons. Ishwaran, H., & Rao, J. S. (2005). Spike and slab variable selection: frequentist and Bayesian strategies. The Annals of Statistics, 33(2), 730-773.

Examples

lsirm1pl_normal_mcar *IPL*

1PL LSIRM with normal likelihood for missing completely at random data.

Description

lsirm1pl_normal_mcar is used to fit LSIRM with 1pl in incomplete data assumed to be missing completely at random. lsirm1pl_normal_mcar factorizes continuous item response matrix into columnwise item effect, row-wise respondent effect and further embeds interaction effect in a latent space, while ignoring the missing element under the assumption of missing completely at random. The resulting latent space provides an interaction map that represents interactions between respondents and items.

Usage

```
lsirm1pl_normal_mcar(
  data,
  ndim = 2,
  niter = 15000,
  nburn = 2500,
  nthin = 5,
  nprint = 500,
  jump\_beta = 0.4,
  jump\_theta = 1,
  jump_gamma = 1,
  jump_z = 0.5,
  jump_w = 0.5,
  pr_mean_beta = 0,
  pr_sd_beta = 1,
  pr_mean_theta = 0,
  pr_sd_theta = 1,
  pr_mean_gamma = 0.5,
  pr_sd_gamma = 1,
  pr_a_theta = 0.001,
  pr_b_t = 0.001,
  pr_a_{eps} = 0.001,
  pr_b_{eps} = 0.001,
 missing.val = 99,
  verbose = FALSE,
  fix_{theta_sd} = FALSE
```

Arguments

data

Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item.

| ndim | Integer; the dimension of the latent space. Default is 2. |
|---------------|---------------------------------------------------------------------------------------------------------|
| niter | Integer; the total number of MCMC iterations to run. Default is 15000. |
| nburn | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500. |
| nthin | Integer; the number of MCMC iterations to thin. Default is 5. |
| nprint | Integer; the interval at which MCMC samples are displayed during execution. Default is 500. |
| jump_beta | Numeric; the jumping rule for the beta proposal density. Default is 0.4. |
| jump_theta | Numeric; the jumping rule for the theta proposal density. Default is 1.0. |
| jump_gamma | Numeric; the jumping rule for the gamma proposal density. Default is 0.025 |
| jump_z | Numeric; the jumping rule for the z proposal density. Default is 0.5. |
| jump_w | Numeric; the jumping rule for the w proposal density. Default is 0.5. |
| pr_mean_beta | Numeric; the mean of the normal prior for beta. Default is 0. |
| pr_sd_beta | Numeric; the standard deviation of the normal prior for beta. Default is 1.0. |
| pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0. |
| pr_sd_theta | Numeric; the standard deviation of the normal prior for theta. Default is 1.0. |
| pr_mean_gamma | Numeric; mean of log normal prior for gamma. Default is 0.5. |
| pr_sd_gamma | Numeric; standard deviation of log normal prior for gamma. Default is 1.0. |
| pr_a_theta | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001 . |
| pr_b_theta | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001. |
| pr_a_eps | Numeric; the shape parameter of inverse gamma prior for variance of data likelihood. Default is 0.001. |
| pr_b_eps | Numeric; the scale parameter of inverse gamma prior for variance of data likelihood. Default is 0.001. |
| missing.val | Numeric; a number to replace missing values. Default is 99. |
| verbose | Logical; If TRUE, MCMC samples are printed for each nprint. Default is FALSE. |
| fix_theta_sd | Logical; If TRUE, the standard deviation of the theta parameter is fixed. Default is FALSE. |

Details

lsirm1pl_normal_mcar models the continuous value of response by respondent j to item i with item effect β_i , respondent effect θ_j and the distance between latent position w_i of item i and latent position z_j of respondent j in the shared metric space, with γ represents the weight of the distance term:

$$Y_{j,i} = \theta_j + \beta_i - \gamma ||z_j - w_i|| + e_{j,i}$$

where the error $e_{j,i} \sim N(0,\sigma^2)$ Under the assumption of missing completely at random, the model ignores the missing element in doing inference. For the details of missing at random assumption and data augmentation, see References.

Value

lsirm1pl_normal_mcar returns an object of list containing the following components:

data A data frame or matrix containing the variables used in the model.

missing.val A number to replace missing values.

bic Numeric value with the corresponding BIC.

mcmc_inf Details about the number of MCMC iterations, burn-in periods, and thinning

intervals.

map_inf The log maximum a posteriori (MAP) value and the iteration number at which

this MAP value occurs.

beta_estimate Posterior estimates of the beta parameter.
theta_estimate Posterior estimates of the theta parameter.

sigma_theta_estimate

Posterior estimates of the standard deviation of theta.

gamma_estimate Posterior estimates of gamma parameter.

z_estimate Posterior estimates of the z parameter.

w_estimate Posterior estimates of the w parameter.

beta Posterior samples of the beta parameter.

theta Posterior samples of the theta parameter.

theta_sd Posterior samples of the standard deviation of theta.

gamma Posterior samples of the gamma parameter.

z Posterior samples of the z parameter, represented as a 3-dimensional matrix

where the last axis denotes the dimension of the latent space.

w Posterior samples of the w parameter, represented as a 3-dimensional matrix

where the last axis denotes the dimension of the latent space.

z_raw Posterior samples of the z parameter without procrustes matching.w_raw Posterior samples of the w parameter without procrustes matching.

Acceptance ratio for the beta parameter.

accept_theta Acceptance ratio for the theta parameter.
accept_z Acceptance ratio for the z parameter.
accept_w Acceptance ratio for the w parameter.
accept_gamma Acceptance ratio for the gamma parameter.
sigma_estimate Posterior estimates of the standard deviation.
Posterior samples of the standard deviation.

References

accept_beta

Little, R. J., & Rubin, D. B. (2019). Statistical analysis with missing data (Vol. 793). John Wiley & Sons.

Examples

lsirm1pl_normal_mcar_ss

1PL LSIRM with normal likelihood and model selection approach for missing completely at random data.

Description

lsirm1pl_normal_mcar_ss is used to fit LSIRM with model selection approach based on spike-and-slab priors for continuous variable with 1pl in incomplete data assumed to be missing completely at random. lsirm1pl_normal_mcar_ss factorizes continuous item response matrix into column-wise item effect, row-wise respondent effect and further embeds interaction effect in a latent space, while ignoring the missing element under the assumption of missing completely at random. The resulting latent space provides an interaction map that represents interactions between respondents and items.

Usage

```
lsirm1pl_normal_mcar_ss(
    data,
    ndim = 2,
    niter = 15000,
    nburn = 2500,
    nthin = 5,
    nprint = 500,
    jump_beta = 0.4,
    jump_theta = 1,
    jump_gamma = 1,
    jump_z = 0.5,
    jump_w = 0.5,
    pr_mean_beta = 0,
    pr_sd_beta = 1,
    pr_mean_theta = 0,
```

```
pr_sd_theta = 1,
pr_spike_mean = -3,
pr_spike_sd = 1,
pr_slab_mean = 0.5,
pr_slab_sd = 1,
pr_a_theta = 0.001,
pr_b_theta = 0.001,
pr_a_eps = 0.001,
pr_xi_a = 0.001,
pr_xi_b = 0.001,
missing.val = 99,
verbose = FALSE,
fix_theta_sd = FALSE)
```

| data | Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item. |
|---------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| ndim | Integer; the dimension of the latent space. Default is 2. |
| niter | Integer; the total number of MCMC iterations to run. Default is 15000. |
| nburn | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500. |
| nthin | Integer; the number of MCMC iterations to thin. Default is 5. |
| nprint | Integer; the interval at which MCMC samples are displayed during execution. Default is 500. |
| jump_beta | Numeric; the jumping rule for the beta proposal density. Default is 0.4. |
| jump_theta | Numeric; the jumping rule for the theta proposal density. Default is 1.0. |
| jump_gamma | Numeric; the jumping rule for the theta proposal density. Default is 1.0. |
| jump_z | Numeric; the jumping rule for the z proposal density. Default is 0.5. |
| jump_w | Numeric; the jumping rule for the w proposal density. Default is 0.5. |
| pr_mean_beta | Numeric; the mean of the normal prior for beta. Default is 0. |
| pr_sd_beta | Numeric; the standard deviation of the normal prior for beta. Default is 1.0. |
| pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0. |
| pr_sd_theta | Numeric; the standard deviation of the normal prior for theta. Default is 1.0. |
| pr_spike_mean | Numeric; the mean of spike prior for log gamma. Default is -3. |
| pr_spike_sd | Numeric; the standard deviation of spike prior for log gamma. Default is 1. |
| pr_slab_mean | Numeric; the mean of spike prior for log gamma. Default is 0.5. |
| pr_slab_sd | Numeric; the standard deviation of spike prior for log gamma. Default is is 1. |
| pr_a_theta | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001 . |
| | |

| pr_b_theta | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001. |
|--------------|--------------------------------------------------------------------------------------------------------|
| pr_a_eps | Numeric; the shape parameter of inverse gamma prior for variance of data likelihood. Default is 0.001. |
| pr_b_eps | Numeric; the scale parameter of inverse gamma prior for variance of data likelihood. Default is 0.001. |
| pr_xi_a | Numeric; the first shape parameter of beta prior for latent variable xi. Default is 1. |
| pr_xi_b | Numeric; the second shape parameter of beta prior for latent variable xi. Default is 1. |
| missing.val | Numeric; a number to replace missing values. Default is 99. |
| verbose | Logical; If TRUE, MCMC samples are printed for each nprint. Default is FALSE. |
| fix_theta_sd | Logical; If TRUE, the standard deviation of the theta parameter is fixed. Default is FALSE. |

Details

lsirm1pl_normal_mcar_ss models the continuous value of response by respondent j to item i with item effect β_i , respondent effect θ_j and the distance between latent position w_i of item i and latent position z_j of respondent j in the shared metric space, with γ represents the weight of the distance term:

$$Y_{j,i} = \theta_j + \beta_i - \gamma ||z_j - w_i|| + e_{j,i}$$

where the error $e_{j,i} \sim N(0,\sigma^2)$. Under the assumption of missing completely at random, the model ignores the missing element in doing inference. For the details of missing at random assumption and data augmentation, see References. lsirm1pl_normal_mcar_ss model include model selection approach based on spike-and-slab priors for log gamma. For detail of spike-and-slab priors, see References.

Value

lsirm1pl_normal_mcar_ss returns an object of list containing the following components:

Data frame or matrix containing the variables in the model.

missing.val A number to replace missing values.

bic Numeric value with the corresponding BIC.

mcmc_inf Details about the number of MCMC iterations, burn-in periods, and thinning intervals.

map_inf The log maximum a posteriori (MAP) value and the iteration number at which this MAP value occurs.

beta_estimate Posterior estimates of the beta parameter.

theta_estimate Posterior estimates of the theta parameter.

sigma_theta_estimate

Posterior estimates of the standard deviation of theta.

| <pre>gamma_estimate</pre> | posterior estimates of gamma parameter. |
|---------------------------|--------------------------------------------------------------------------------------------------------------------------------------------------------|
| z_estimate | Posterior estimates of the z parameter. |
| w_estimate | Posterior estimates of the w parameter. |
| beta | Posterior samples of the beta parameter. |
| theta | Posterior samples of the theta parameter. |
| gamma | Posterior samples of the gamma parameter. |
| theta_sd | Posterior samples of the standard deviation of theta. |
| Z | Posterior samples of the z parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space. |
| W | Posterior samples of the w parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space. |
| z_raw | Posterior samples of the z parameter without procrustes matching. |
| w_raw | Posterior samples of the w parameter without procrustes matching. |
| pi | Posterior samples of phi which is indicator of spike and slab prior. If phi is 1, log gamma follows the slab prior, otherwise follows the spike prior. |
| accept_beta | Acceptance ratio for the beta parameter. |
| accept_theta | Acceptance ratio for the theta parameter. |
| accept_z | Acceptance ratio for the z parameter. |
| accept_w | Acceptance ratio for the w parameter. |
| accept_gamma | Acceptance ratio for the gamma parameter. |
| sigma_estimate | Posterior estimates of the standard deviation. |
| sigma | Posterior samples of the standard deviation. |
| | |

References

Little, R. J., & Rubin, D. B. (2019). Statistical analysis with missing data (Vol. 793). John Wiley & Sons. Ishwaran, H., & Rao, J. S. (2005). Spike and slab variable selection: frequentist and Bayesian strategies. The Annals of Statistics, 33(2), 730-773.

Examples

56 lsirm1pl_normal_o

lsirm1pl_normal_o

1PL LSIRM with normal likelihood.

Description

lsirm1pl_normal_o is used to fit LSIRM for continuous variable with 1pl. lsirm1pl_normal_o factorizes continuous item response matrix into column-wise item effect, row-wise respondent effect and further embeds interaction effect in a latent space. The resulting latent space provides an interaction map that represents interactions between respondents and items.

Usage

```
lsirm1pl_normal_o(
  data,
  ndim = 2,
  niter = 15000,
  nburn = 2500,
 nthin = 5,
  nprint = 500,
  jump\_beta = 0.4,
  jump\_theta = 1,
  jump_gamma = 1,
  jump_z = 0.5,
  jump_w = 0.5,
  pr_mean_beta = 0,
  pr_sd_beta = 1,
  pr_mean_theta = 0,
  pr_sd_theta = 1,
  pr_mean_gamma = 0.5,
  pr_sd_gamma = 1,
  pr_a_theta = 0.001,
 pr_b_t = 0.001,
 pr_a_{eps} = 0.001,
 pr_b_{eps} = 0.001,
  verbose = FALSE,
  fix_{theta_sd} = FALSE
)
```

| data | Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item. |
|-------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| ndim | Integer; the dimension of the latent space. Default is 2. |
| niter | Integer; the total number of MCMC iterations to run. Default is 15000. |

lsirm1pl_normal_o 57

| nburn | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500. |
|---------------|-----------------------------------------------------------------------------------------------------------|
| nthin | Integer; the number of MCMC iterations to thin. Default is 5. |
| nprint | Integer; the interval at which MCMC samples are displayed during execution. Default is 500. |
| jump_beta | Numeric; the jumping rule for the beta proposal density. Default is 0.4. |
| jump_theta | Numeric; the jumping rule for the theta proposal density. Default is 1.0. |
| jump_gamma | Numeric; the jumping rule for the gamma proposal density. Default is 0.025 |
| jump_z | Numeric; the jumping rule for the z proposal density. Default is 0.5. |
| jump_w | Numeric; the jumping rule for the w proposal density. Default is 0.5. |
| pr_mean_beta | Numeric; the mean of the normal prior for beta. Default is 0. |
| pr_sd_beta | Numeric; the standard deviation of the normal prior for beta. Default is 1.0. |
| pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0. |
| pr_sd_theta | Numeric; the standard deviation of the normal prior for theta. Default is 1.0. |
| pr_mean_gamma | Numeric; mean of log normal prior for gamma. Default is 0.5. |
| pr_sd_gamma | Numeric; standard deviation of log normal prior for gamma. Default is 1.0. |
| pr_a_theta | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001. |
| pr_b_theta | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001. |
| pr_a_eps | Numeric; the shape parameter of inverse gamma prior for variance of data likelihood. Default is 0.001. |
| pr_b_eps | Numeric; the scale parameter of inverse gamma prior for variance of data likelihood. Default is 0.001 . |
| verbose | Logical; If TRUE, MCMC samples are printed for each nprint. Default is FALSE. |
| fix_theta_sd | Logical; If TRUE, the standard deviation of the theta parameter is fixed. Default is FALSE. |

Details

lsirm1pl_normal_o models the continuous value of response by respondent j to item i with item effect β_i , respondent effect θ_j and the distance between latent position w_i of item i and latent position z_j of respondent j in the shared metric space, with γ represents the weight of the distance term:

$$Y_{j,i} = \theta_j + \beta_i - \gamma ||z_j - w_i|| + e_{j,i}$$

where the error $e_{j,i} \sim N(0, \sigma^2)$.

58 lsirm1pl_normal_o

Value

lsirm1pl_normal_o returns an object of list containing the following components:

data Data frame or matrix containing the variables used in the model.

bic A numeric value representing the Bayesian Information Criterion (BIC).

mcmc_inf Details about the number of MCMC iterations, burn-in periods, and thinning

intervals.

map_inf The log maximum a posteriori (MAP) value and the iteration number at which

this MAP value occurs.

beta_estimate Posterior estimates of the beta parameter. theta_estimate Posterior estimates of the theta parameter.

sigma_theta_estimate

Posterior estimates of the standard deviation of theta.

gamma_estimate Posterior estimates of gamma parameter.

z_estimate Posterior estimates of the z parameter.

w_estimate Posterior estimates of the w parameter.

beta Posterior samples of the beta parameter.

theta Posterior samples of the theta parameter.

theta_sd Posterior samples of the standard deviation of theta.

gamma Posterior samples of the gamma parameter.

z Posterior samples of the z parameter, represented as a 3-dimensional matrix

where the last axis denotes the dimension of the latent space.

w Posterior samples of the w parameter, represented as a 3-dimensional matrix

where the last axis denotes the dimension of the latent space.

z_raw Posterior samples of the z parameter without procrustes matching. w_raw Posterior samples of the w parameter without procrustes matching.

accept_beta Acceptance ratio for the beta parameter.
accept_theta Acceptance ratio for the theta parameter.
accept_z Acceptance ratio for the z parameter.
accept_w Acceptance ratio for the w parameter.
accept_gamma Acceptance ratio for the gamma parameter.
sigma_estimate Posterior estimates of the standard deviation.
Posterior samples of the standard deviation.

Examples

```
# generate example (continuous) item response matrix
data <- matrix(rnorm(500, mean = 0, sd = 1),ncol=10,nrow=50)

lsirm_result <- lsirm1pl_normal_o(data)

# The code following can achieve the same result.
lsirm_result <- lsirm(data ~ lsirm1pl(spikenslab = FALSE, fixed_gamma = FALSE))</pre>
```

lsirm1pl_normal_ss 59

lsirm1pl_normal_ss

1PL LSIRM with normal likelihood and model selection approach.

Description

lsirm1pl_normal_ss is used to fit LSIRM with model selection approach based on spike-and-slab priors for continuous variable with 1pl. LSIRM factorizes continuous item response matrix into column-wise item effect, row-wise respondent effect and further embeds interaction effect in a latent space. The resulting latent space provides an interaction map that represents interactions between respondents and items.

Usage

```
lsirm1pl_normal_ss(
  data,
  ndim = 2,
  niter = 15000,
  nburn = 2500,
  nthin = 5,
  nprint = 500,
  jump\_beta = 0.4,
  jump\_theta = 1,
  jump_gamma = 1,
  jump_z = 0.5,
  jump_w = 0.5,
  pr_mean_beta = 0,
  pr_sd_beta = 1,
 pr_mean_theta = 0,
  pr_sd_theta = 1,
 pr_spike_mean = -3,
  pr_spike_sd = 1,
  pr_slab_mean = 0.5,
  pr_slab_sd = 1,
  pr_a_theta = 0.001,
  pr_b_t = 0.001,
  pr_a_{eps} = 0.001,
  pr_b_{eps} = 0.001,
 pr_xi_a = 0.001,
 pr_xi_b = 0.001,
 verbose = FALSE,
  fix_theta_sd = FALSE
)
```

Arguments

data

Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item.

60 lsirm1pl_normal_ss

| ndim | Integer; the dimension of the latent space. Default is 2. |
|---------------|---------------------------------------------------------------------------------------------------------|
| niter | Integer; the total number of MCMC iterations to run. Default is 15000. |
| nburn | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500. |
| nthin | Integer; the number of MCMC iterations to thin. Default is 5. |
| nprint | Integer; the interval at which MCMC samples are displayed during execution. Default is 500. |
| jump_beta | Numeric; the jumping rule for the beta proposal density. Default is 0.4. |
| jump_theta | Numeric; the jumping rule for the theta proposal density. Default is 1.0. |
| jump_gamma | Numeric; the jumping rule for the theta proposal density. Default is 1.0. |
| jump_z | Numeric; the jumping rule for the z proposal density. Default is 0.5. |
| jump_w | Numeric; the jumping rule for the w proposal density. Default is 0.5. |
| pr_mean_beta | Numeric; the mean of the normal prior for beta. Default is 0. |
| pr_sd_beta | Numeric; the standard deviation of the normal prior for beta. Default is 1.0. |
| pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0. |
| pr_sd_theta | Numeric; the standard deviation of the normal prior for theta. Default is 1.0. |
| pr_spike_mean | Numeric; mean of spike prior for log gamma default value is -3. |
| pr_spike_sd | Numeric; standard deviation of spike prior for log gamma default value is 1. |
| pr_slab_mean | Numeric; mean of spike prior for log gamma default value is 0.5. |
| pr_slab_sd | Numeric; standard deviation of spike prior for log gamma default value is 1. |
| pr_a_theta | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001. |
| pr_b_theta | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001 . |
| pr_a_eps | Numeric; shape parameter of inverse gamma prior for variance of data likelihood. Default is 0.001. |
| pr_b_eps | Numeric; scale parameter of inverse gamma prior for variance of data likelihood. Default is 0.001. |
| pr_xi_a | Numeric; first shape parameter of beta prior for latent variable xi. Default is 1. |
| pr_xi_b | Numeric; second shape parameter of beta prior for latent variable xi. Default is 1. |
| verbose | Logical; If TRUE, MCMC samples are printed for each nprint. Default is FALSE. |
| fix_theta_sd | Logical; If TRUE, the standard deviation of the theta parameter is fixed. Default is FALSE. |

Isirm1pl_normal_ss 61

Details

lsirm1pl_normal_ss models the continuous value of response by respondent j to item i with item effect β_i , respondent effect θ_j and the distance between latent position w_i of item i and latent position z_j of respondent j in the shared metric space, with γ represents the weight of the distance term:

$$Y_{j,i} = \theta_j + \beta_i - \gamma ||z_j - w_i|| + e_{j,i}$$

where the error $e_{j,i} \sim N(0, \sigma^2)$. lsrm1pl_noraml_ss model include model selection approach based on spike-and-slab priors for log gamma. For detail of spike-and-slab priors, see References.

Value

lsirm1pl_normal_ss returns an object of list containing the following components:

data Data frame or matrix containing the variables in the model.

bic Numeric value with the corresponding BIC.

mcmc_inf number of mcmc iteration, burn-in periods, and thinning intervals.

map_inf value of log maximum a posterior and iteration number which have log maxi-

mum a posterior.

beta_estimate posterior estimation of beta.
theta_estimate posterior estimation of theta.

sigma_theta_estimate

posterior estimation of standard deviation of theta.

sigma_estimate posterior estimation of standard deviation.

gamma_estimate posterior estimation of gamma.

 z_{estimate} posterior estimation of z. w_{estimate} posterior estimation of w.

pi_estimate posterior estimation of phi. inclusion probability of gamma. if estimation of phi

is less than 0.5, choose Rasch model with gamma = 0, otherwise latent space

model with gamma > 0.

beta posterior samples of beta. theta posterior samples of theta.

theta_sd posterior samples of standard deviation of theta.

sigma posterior samples of standard deviation.

gamma posterior samples of gamma.

z posterior samples of z. The output is 3-dimensional matrix with last axis repre-

sent the dimension of latent space.

w posterior samples of w. The output is 3-dimensional matrix with last axis repre-

sent the dimension of latent space.

z_raw posterior samples of z without procrustes matching.w_raw posterior samples of w without procrustes matching.

pi posterior samples of phi which is indicator of spike and slab prior. If phi is 1,

log gamma follows the slab prior, otherwise follows the spike prior.

lsirm1pl_o

```
accept_beta accept ratio of beta.

accept_theta accept ratio of theta.

accept_w accept ratio of w.

accept_z accept ratio of z.

accept_gamma accept ratio of gamma.
```

References

Ishwaran, H., & Rao, J. S. (2005). Spike and slab variable selection: Frequentist and Bayesian strategies (Vol. 33). The Annals of Statistics

Examples

```
# generate example (continuous) item response matrix
data <- matrix(rnorm(500, mean = 0, sd = 1),ncol=10,nrow=50)

lsirm_result <- lsirm1pl_normal_ss(data)

# The code following can achieve the same result.
lsirm_result <- lsirm(data ~ lsirm1pl(spikenslab = TRUE, fixed_gamma = FALSE))</pre>
```

lsirm1pl_o

1PL LSIRM.

Description

lsirm1pl_o is used to fit 1PL LSIRM. lsirm1pl_o factorizes item response matrix into column-wise item effect, row-wise respondent effect and further embeds interaction effect in a latent space. The resulting latent space provides an interaction map that represents interactions between respondents and items.

Usage

```
lsirm1pl_o(
   data,
   ndim = 2,
   niter = 15000,
   nburn = 2500,
   nthin = 5,
   nprint = 500,
   jump_beta = 0.4,
   jump_theta = 1,
   jump_gamma = 0.025,
   jump_z = 0.5,
   jump_w = 0.5,
   pr_mean_beta = 0,
```

lsirm1pl_o 63

```
pr_sd_beta = 1,
pr_mean_theta = 0,
pr_sd_theta = 1,
pr_mean_gamma = 0.5,
pr_sd_gamma = 1,
pr_a_theta = 0.001,
pr_b_theta = 0.001,
verbose = FALSE,
fix_theta_sd = FALSE)
```

| data | Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item. |
|---------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| ndim | Integer; the dimension of the latent space. Default is 2. |
| niter | Integer; the total number of MCMC iterations to run. Default is 15000. |
| nburn | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500. |
| nthin | Integer; the number of MCMC iterations to thin. Default is 5. |
| nprint | Integer; the interval at which MCMC samples are displayed during execution. Default is 500. |
| jump_beta | Numeric; the jumping rule for the beta proposal density. Default is 0.4. |
| jump_theta | Numeric; the jumping rule for the theta proposal density. Default is 1.0. |
| jump_gamma | Numeric; the jumping rule for the gamma proposal density. Default is 0.025. |
| jump_z | Numeric; the jumping rule for the z proposal density. Default is 0.5. |
| jump_w | Numeric; the jumping rule for the w proposal density. Default is 0.5. |
| pr_mean_beta | Numeric; the mean of the normal prior for beta. Default is 0. |
| pr_sd_beta | Numeric; the standard deviation of the normal prior for beta. Default is 1.0. |
| pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0. |
| pr_sd_theta | Numeric; the standard deviation of the normal prior for theta. Default is 1.0. |
| pr_mean_gamma | Numeric; mean of log normal prior for gamma. Default is 0.5. |
| pr_sd_gamma | Numeric; standard deviation of log normal prior for gamma. Default is 1.0. |
| pr_a_theta | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001. |
| pr_b_theta | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001. |
| verbose | Logical; If TRUE, MCMC samples are printed for each nprint. Default is FALSE. |
| fix_theta_sd | Logical; If TRUE, the standard deviation of the theta parameter is fixed. Default is FALSE. |

64 Isirm1pl_o

Details

lsirm1pl_o models the probability of correct response by respondent j to item i with item effect β_i , respondent effect θ_j and the distance between latent position w_i of item i and latent position z_j of respondent j in the shared metric space, with γ represents the weight of the distance term:

$$logit(P(Y_{j,i} = 1 | \theta_j, \beta_i, \gamma, z_j, w_i)) = \theta_j + \beta_i - \gamma ||z_j - w_i||$$

Value

lsirm1pl_o returns an object of list containing the following components:

data Data frame or matrix containing the variables used in the model.

bic A numeric value representing the Bayesian Information Criterion (BIC).

mcmc_inf Details about the number of MCMC iterations, burn-in periods, and thinning

intervals.

map_inf The log maximum a posteriori (MAP) value and the iteration number at which

this MAP value occurs.

beta_estimate Posterior estimates of the beta parameter.

theta_estimate Posterior estimates of the theta parameter.

sigma_theta_estimate

Posterior estimates of the standard deviation of theta.

gamma_estimate Posterior estimates of gamma parameter.

z_estimate Posterior estimates of the z parameter.
 w_estimate Posterior estimates of the w parameter.
 beta Posterior samples of the beta parameter.
 theta Posterior samples of the theta parameter.

theta_sd Posterior samples of the standard deviation of theta.

gamma Posterior samples of the gamma parameter.

z Posterior samples of the z parameter, represented as a 3-dimensional matrix

where the last axis denotes the dimension of the latent space.

w Posterior samples of the w parameter, represented as a 3-dimensional matrix

where the last axis denotes the dimension of the latent space.

z_raw Posterior samples of the z parameter without procrustes matching.
w_raw Posterior samples of the w parameter without procrustes matching.

accept_beta Acceptance ratio for the beta parameter.
accept_theta Acceptance ratio for the theta parameter.
accept_z Acceptance ratio for the z parameter.
accept_w Acceptance ratio for the w parameter.
accept_gamma Acceptance ratio for the gamma parameter.

lsirm1pl_ss 65

Examples

```
# generate example item response matrix
data <- matrix(rbinom(500, size = 1, prob = 0.5),ncol=10,nrow=50)

lsirm_result <- lsirm1pl_o(data)

# The code following can achieve the same result.
lsirm_result <- lsirm(data ~ lsirm1pl(spikenslab = FALSE, fixed_gamma = FALSE))</pre>
```

lsirm1pl_ss

1PL LSIRM with model selection approach.

Description

lsirm1pl_ss is used to fit 1PL LSIRM with model selection approach based on spike-and-slab priors. LSIRM factorizes item response matrix into column-wise item effect, row-wise respondent effect and further embeds interaction effect in a latent space. The resulting latent space provides an interaction map that represents interactions between respondents and items.

Usage

```
lsirm1pl_ss(
  data,
  ndim = 2,
  niter = 15000,
  nburn = 2500,
  nthin = 5,
  nprint = 500,
  jump\_beta = 0.4,
  jump\_theta = 1,
  jump_gamma = 1,
  jump_z = 0.5,
  jump_w = 0.5,
  pr_mean_beta = 0,
  pr_sd_beta = 1,
 pr_mean_theta = 0,
  pr_sd_theta = 1,
  pr_spike_mean = -3,
  pr_spike_sd = 1,
  pr_slab_mean = 0.5,
  pr_slab_sd = 1,
  pr_a_theta = 0.001,
  pr_b_t = 0.001,
 pr_xi_a = 1,
  pr_xi_b = 1,
  verbose = FALSE,
```

lsirm1pl_ss

```
fix_theta_sd = FALSE
)
```

| data | Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item. |
|---------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| ndim | Integer; the dimension of the latent space. Default is 2. |
| niter | Integer; the total number of MCMC iterations to run. Default is 15000. |
| nburn | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500. |
| nthin | Integer; the number of MCMC iterations to thin. Default is 5. |
| nprint | Integer; the interval at which MCMC samples are displayed during execution. Default is 500. |
| jump_beta | Numeric; the jumping rule for the beta proposal density. Default is 0.4. |
| jump_theta | Numeric; the jumping rule for the theta proposal density. Default is 1.0. |
| jump_gamma | Numeric; the jumping rule for the theta proposal density. Default is 1.0. |
| jump_z | Numeric; the jumping rule for the z proposal density. Default is 0.5. |
| jump_w | Numeric; the jumping rule for the w proposal density. Default is 0.5. |
| pr_mean_beta | Numeric; the mean of the normal prior for beta. Default is 0. |
| pr_sd_beta | Numeric; the standard deviation of the normal prior for beta. Default is 1.0. |
| pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0. |
| pr_sd_theta | Numeric; the standard deviation of the normal prior for theta. Default is 1.0. |
| pr_spike_mean | Numeric; the mean of spike prior for log gamma. Default is -3. |
| pr_spike_sd | Numeric; the standard deviation of spike prior for log gamma. Default is 1. |
| pr_slab_mean | Numeric; the mean of spike prior for log gamma. Default is 0.5. |
| pr_slab_sd | Numeric; the standard deviation of spike prior for log gamma. Default is is 1. |
| pr_a_theta | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001 . |
| pr_b_theta | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001. |
| pr_xi_a | Numeric; the first shape parameter of beta prior for latent variable xi. Default is 1. |
| pr_xi_b | Numeric; the second shape parameter of beta prior for latent variable xi. Default is 1. |
| verbose | Logical; If TRUE, MCMC samples are printed for each nprint. Default is FALSE. |
| fix_theta_sd | Logical; If TRUE, the standard deviation of the theta parameter is fixed. Default is FALSE. |

lsirm1pl_ss 67

Details

lsirm1pl_ss models the probability of correct response by respondent j to item i with item effect β_i , respondent effect θ_j and the distance between latent position w_i of item i and latent position z_j of respondent j in the shared metric space, with γ represents the weight of the distance term:

$$logit(P(Y_{j,i} = 1 | \theta_j, \beta_i, \gamma, z_j, w_i)) = \theta_j + \beta_i - \gamma ||z_j - w_i||$$

lsirm1pl_ss model include model selection approach based on spike-and-slab priors for log gamma. For detail of spike-and-slab priors, see References.

Value

lsirm1pl_ss returns an object of list containing the following components:

data Data frame or matrix containing the variables used in the model.

bic A numeric value representing the Bayesian Information Criterion (BIC).

mcmc_inf Details about the number of MCMC iterations, burn-in periods, and thinning

intervals.

map_inf The log maximum a posteriori (MAP) value and the iteration number at which

this MAP value occurs.

beta_estimate Posterior estimates of the beta parameter.
theta_estimate Posterior estimates of the theta parameter.

sigma_theta_estimate

Posterior estimates of the standard deviation of theta.

gamma_estimate Posterior estimates of gamma parameter.

z_estimate Posterior estimates of the z parameter.

w_estimate Posterior estimates of the w parameter.

beta Posterior samples of the beta parameter.

theta Posterior samples of the theta parameter.

theta_sd Posterior samples of the standard deviation of theta.

gamma Posterior samples of the gamma parameter.

z Posterior samples of the z parameter, represented as a 3-dimensional matrix

where the last axis denotes the dimension of the latent space.

w Posterior samples of the w parameter, represented as a 3-dimensional matrix

where the last axis denotes the dimension of the latent space.

z_raw Posterior samples of the z parameter without procrustes matching.w_raw Posterior samples of the w parameter without procrustes matching.

accept_beta Acceptance ratio for the beta parameter.
accept_theta Acceptance ratio for the theta parameter.
accept_z Acceptance ratio for the z parameter.
accept_w Acceptance ratio for the w parameter.
accept_gamma Acceptance ratio for the gamma parameter.

68 lsirm2pl

| pi_estimate | Posterior estimation of phi. inclusion probability of gamma. if estimation of phi is less than 0.5 , choose Rasch model with gamma = 0 , otherwise latent space model with gamma > 0 . |
|-------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| pi | Posterior samples of phi which is indicator of spike and slab prior. If phi is 1, log gamma follows the slab prior, otherwise follows the spike prior. |

References

Ishwaran, H., & Rao, J. S. (2005). Spike and slab variable selection: Frequentist and Bayesian strategies (Vol. 33). The Annals of Statistics

Examples

```
# generate example item response matrix
data <- matrix(rbinom(500, size = 1, prob = 0.5),ncol=10,nrow=50)
lsirm_result <- lsirm1pl_ss(data)
# The code following can achieve the same result.
lsirm_result <- lsirm(data ~ lsirm1pl(spikenslab = TRUE, fixed_gamma = FALSE))</pre>
```

lsirm2pl

Fit a 2pl LSIRM for binary and continuous item resopnse data

Description

lsirm2pl integrates all functions related to 2PL LSIRM. Various 2PL LSIRM function can be used by setting the spikenslab, fixed_gamma, and missing_data arguments.

This function can be used regardless of the data type, providing a unified approach to model fitting.

Usage

```
lsirm2pl(
  data,
  spikenslab = FALSE,
  fixed_gamma = FALSE,
  missing_data = NA,
  chains = 1,
  multicore = 1,
  seed = NA,
  ndim = 2,
  niter = 15000,
  nburn = 2500,
  nthin = 5,
  nprint = 500,
  jump_beta = 0.4,
```

lsirm2pl 69

```
jump\_theta = 1,
  jump_alpha = 1,
  jump_gamma = 0.025,
  jump_z = 0.5,
  jump_w = 0.5,
 pr_mean_beta = 0,
 pr_sd_beta = 1,
 pr_mean_theta = 0,
 pr_sd_theta = 1,
 pr_mean_gamma = 0.5,
 pr_sd_gamma = 1,
 pr_a_theta = 0.001,
 pr_b_t = 0.001,
 pr_mean_alpha = 0.5,
 pr_sd_alpha = 1,
 fix_{theta_sd} = FALSE,
 fix_alpha_1 = TRUE,
)
```

| data | Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item. |
|--------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| spikenslab | Logical; specifies whether to use a model selection approach. Default is FALSE. |
| fixed_gamma | Logical; indicates whether to fix gamma at 1. Default is FALSE. |
| missing_data | Character; the type of missing data assumed. Options are NA, "mar", or "mcar". Default is NA. |
| chains | Integer; the number of MCMC chains to run. Default is 1. |
| multicore | Integer; the number of cores to use for parallel execution. Default is 1. |
| seed | Integer; the seed number for MCMC fitting. Default is NA. |
| ndim | Integer; the dimension of the latent space. Default is 2. |
| niter | Integer; the total number of MCMC iterations to run. Default is 15000. |
| nburn | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500 . |
| nthin | Integer; the number of MCMC iterations to thin. Default is 5. |
| nprint | Integer; the interval at which MCMC samples are displayed during execution. Default is 500. |
| jump_beta | Numeric; the jumping rule for the beta proposal density. Default is 0.4. |
| jump_theta | Numeric; the jumping rule for the theta proposal density. Default is 1.0. |
| jump_alpha | Numeric; the jumping rule for the alpha proposal density. Default is 1.0. |
| jump_gamma | Numeric; the jumping rule for the gamma proposal density. Default is 0.025. |
| jump_z | Numeric; the jumping rule for the z proposal density. Default is 0.5. |
| | |

70 Isirm2pl

| jump_w | Numeric; the jumping rule for the w proposal density. Default is 0.5. |
|---------------|---------------------------------------------------------------------------------------------------------|
| pr_mean_beta | Numeric; the mean of the normal prior for beta. Default is 0. |
| pr_sd_beta | Numeric; the standard deviation of the normal prior for beta. Default is 1.0. |
| pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0. |
| pr_sd_theta | Numeric; the standard deviation of the normal prior for theta. Default is 1.0. |
| pr_mean_gamma | Numeric; mean of log normal prior for gamma. Default is 0.5. |
| pr_sd_gamma | Numeric; standard deviation of log normal prior for gamma. Default is 1.0. |
| pr_a_theta | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001 . |
| pr_b_theta | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001 . |
| pr_mean_alpha | Numeric; the mean of the log normal prior for alpha. Default is 0.5. |
| pr_sd_alpha | Numeric; the standard deviation of the log normal prior for alpha. Default is 1.0. |
| fix_theta_sd | Logical; If TRUE, the standard deviation of the theta parameter is fixed. Default is FALSE. |
| fix_alpha_1 | Logical; If TRUE, the first element of the alpha parameter is fixed to 1. Default is TRUE. |
| • • • | Additional arguments for the for various settings. Refer to the functions in the Details. |

Details

Additional arguments and return values for each function are documented in the respective function's description.

- * For 2PL LSIRM with data included missing value are detailed in lsirm2pl_mar and lsirm2pl_mcar.
- * For 2PL LSIRM using the spike-and-slab model selection approach are detailed in lsirm2pl_ss.
- * For continuous version of 2PL LSIRM are detailed in lsirm2pl_normal_o.

For 2PL LSIRM with binary item response data, the probability of correct response by respondent j to item i with item effect β_i , respondent effect θ_j and the distance between latent position w_i of item i and latent position z_j of respondent j in the shared metric space, with γ represents the weight of the distance term. For 2pl model, the the item effect is assumed to have additional discrimination parameter α_i multiplied by θ_j :

$$logit(P(Y_{j,i} = 1 | \theta_j, \alpha_i, \beta_i, \gamma, z_j, w_i)) = \theta_j * \alpha_i + \beta_i - \gamma ||z_j - w_i||$$

For 2PL LSIRM with continuous item response data, the continuous value of response by respondent j to item i with item effect β_i , respondent effect θ_j and the distance between latent position w_i of item i and latent position z_j of respondent j in the shared metric space, with γ represents the weight of the distance term. For 2pl model, the the item effect is assumed to have additional discrimination parameter α_i multiplied by θ_j :

$$Y_{j,i} = \theta_j + \beta_i - \gamma ||z_j - w_i|| + e_{j,i}$$

where the error $e_{i,i} \sim N(0, \sigma^2)$

Isirm2pl 71

Value

lsirm2pl returns an object of list. The basic return list containing the following components:

data A data frame or matrix containing the variables used in the model.

bic A numeric value representing the Bayesian Information Criterion (BIC).

mcmc_inf Details about the number of MCMC iterations, burn-in periods, and thinning

intervals.

map_inf The log maximum a posteriori (MAP) value and the iteration number at which

this MAP value occurs.

beta_estimate Posterior estimates of the beta parameter.
theta_estimate Posterior estimates of the theta parameter.

sigma_theta_estimate

theta

Posterior estimates of the standard deviation of theta.

alpha_estimate posterior estimates of alpha parameter..
gamma_estimate Posterior estimates of gamma parameter.
z_estimate Posterior estimates of the z parameter.
w_estimate Posterior estimates of the w parameter.
beta Posterior samples of the beta parameter.

theta_sd Posterior samples of the standard deviation of theta.

Posterior samples of the theta parameter.

alpha Posterior samples of the alpha parameter.
gamma Posterior samples of the gamma parameter.

z Posterior samples of the z parameter, represented as a 3-dimensional matrix

where the last axis denotes the dimension of the latent space.

Posterior samples of the w parameter, represented as a 3-dimensional matrix

where the last axis denotes the dimension of the latent space.

accept_beta Acceptance ratio for the beta parameter.
accept_theta Acceptance ratio for the theta parameter.
accept_z Acceptance ratio for the z parameter.
accept_w Acceptance ratio for the w parameter.
accept_alpha Acceptance ratio for the alpha parameter.
accept_gamma Acceptance ratio for the gamma parameter.

... Additional return values for various settings. Refer to the functions in the De-

tails.

Note

If both spikenslab and fixed_gamma are set TRUE, it returns error because both are related to gamma.

See Also

```
The 2PL LSIRM for binary item response data as following:
```

```
lsirm2pl_o, lsirm2pl_fixed_gamma, lsirm2pl_mar,lsirm2pl_mcar, lsirm2pl_fixed_gamma_mar,
lsirm2pl_fixed_gamma_mcar, lsirm2pl_ss, lsirm2pl_mar_ss, and lsirm2pl_mcar_ss
```

The 2PL LSIRM for continuous item response data as following:

```
lsirm2pl_normal_o,lsirm2pl_normal_fixed_gamma,lsirm2pl_normal_mar,lsirm2pl_normal_mcar,lsirm1pl_normlsirm2pl_normal_fixed_gamma_mcar,lsirm2pl_normal_ss,lsirm2pl_normal_mar_ss,lsirm2pl_normal_mcar_ss
```

Examples

```
# generate example item response matrix
data <- matrix(rbinom(500, size = 1, prob = 0.5),ncol=10,nrow=50)
lsirm_result <- lsirm2pl(data)

# The code following can achieve the same result.
lsirm_result <- lsirm(data~lsirm2pl())</pre>
```

lsirm2pl_fixed_gamma 2PL LSIRM fixing gamma to 1.

Description

lsirm2pl_fixed_gamma is used to fit 2PL LSIRM fixing gamma to 1. lsirm2pl_fixed_gamma factorizes item response matrix into column-wise item effect, row-wise respondent effect and further embeds interaction effect in a latent space. Unlike 1PL model, 2PL model assumes the item effect can vary according to respondent, allowing additional parameter multiplied with respondent effect. The resulting latent space provides an interaction map that represents interactions between respondents and items.

Usage

```
lsirm2pl_fixed_gamma(
    data,
    ndim = 2,
    niter = 15000,
    nburn = 2500,
    nthin = 5,
    nprint = 500,
    jump_beta = 0.4,
    jump_theta = 1,
    jump_alpha = 1,
    jump_z = 0.5,
    jump_w = 0.5,
    pr_mean_beta = 0,
```

lsirm2pl_fixed_gamma 73

```
pr_sd_beta = 1,
pr_mean_theta = 0,
pr_sd_theta = 1,
pr_mean_alpha = 0.5,
pr_sd_alpha = 1,
pr_a_theta = 0.001,
pr_b_theta = 0.001,
verbose = FALSE,
fix_theta_sd = FALSE,
fix_alpha_1 = TRUE
)
```

| data | Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item. |
|---------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| ndim | Integer; the dimension of the latent space. Default is 2. |
| niter | Integer; the total number of MCMC iterations to run. Default is 15000. |
| nburn | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500. |
| nthin | Integer; the number of MCMC iterations to thin. Default is 5. |
| nprint | Integer; the interval at which MCMC samples are displayed during execution. Default is 500. |
| jump_beta | Numeric; the jumping rule for the beta proposal density. Default is 0.4. |
| jump_theta | Numeric; the jumping rule for the theta proposal density. Default is 1.0. |
| jump_alpha | Numeric; the jumping rule for the alpha proposal density. Default is 1.0. |
| jump_z | Numeric; the jumping rule for the z proposal density. Default is 0.5. |
| jump_w | Numeric; the jumping rule for the w proposal density. Default is 0.5. |
| pr_mean_beta | Numeric; the mean of the normal prior for beta. Default is 0. |
| pr_sd_beta | Numeric; the standard deviation of the normal prior for beta. Default is 1.0. |
| pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0. |
| pr_sd_theta | Numeric; the standard deviation of the normal prior for theta. Default is 1.0. |
| pr_mean_alpha | Numeric; the mean of the log normal prior for alpha. Default is 0.5. |
| pr_sd_alpha | Numeric; the standard deviation of the log normal prior for alpha. Default is 1.0. |
| pr_a_theta | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001 . |
| pr_b_theta | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001 . |
| verbose | Logical; If TRUE, MCMC samples are printed for each nprint. Default is FALSE. |

fix_theta_sd Logical; If TRUE, the standard deviation of the theta parameter is fixed. Default

is FALSE.

fix_alpha_1 Logical; If TRUE, the first element of the alpha parameter is fixed to 1. Default

is TRUE.

Details

lsirm2pl_fixed_gamma models the probability of correct response by respondent j to item i with item effect β_i , respondent effect θ_j and the distance between latent position w_i of item i and latent position z_j of respondent j in the shared metric space. For 2pl model, the the item effect is assumed to have additional discrimination parameter α_i multiplied by θ_i :

$$logit(P(Y_{j,i} = 1 | \theta_j, \alpha_i, \beta_i, z_j, w_i)) = \theta_j * \alpha_i + \beta_i - ||z_j - w_i||$$

Value

lsirm2pl_fixed_gamma returns an object of list containing the following components:

lsirm1pl_fixed_gamma returns an object of list containing the following components:

data Data frame or matrix containing the variables in the model.

bic Numeric value with the corresponding BIC.

mcmc_inf Details about the number of MCMC iterations, burn-in periods, and thinning

intervals.

map_inf The log maximum a posteriori (MAP) value and the iteration number at which

this MAP value occurs.

beta_estimate Posterior estimates of the beta parameter.

 $theta_estimate \ \ Posterior\ estimates\ of\ the\ theta\ parameter.$

sigma_theta_estimate

Posterior estimates of the standard deviation of theta.

z_estimate Posterior estimates of the z parameter.
w_estimate Posterior estimates of the w parameter.
beta Posterior samples of the beta parameter.
theta Posterior samples of the theta parameter.

theta_sd Posterior samples of the standard deviation of theta.

z Posterior samples of the z parameter, represented as a 3-dimensional matrix

where the last axis denotes the dimension of the latent space.

W Posterior samples of the w parameter, represented as a 3-dimensional matrix

where the last axis denotes the dimension of the latent space.

z_raw Posterior samples of the z parameter without procrustes matching.

w_raw Posterior samples of the w parameter without procrustes matching.

accept_beta Acceptance ratio for the beta parameter.

accept_theta Acceptance ratio for the theta parameter.

accept_z Acceptance ratio for the z parameter.

```
accept_w Acceptance ratio for the w parameter.

alpha_estimate Posterior estimates of the alpha parameter.

alpha Posterior estimates of the alpha parameter.

accept_alpha Acceptance ratio for the alpha parameter.
```

Examples

```
# generate example item response matrix
data <- matrix(rbinom(500, size = 1, prob = 0.5),ncol=10,nrow=50)

lsirm_result <- lsirm2pl_fixed_gamma(data)

# The code following can achieve the same result.
lsirm_result <- lsirm(data ~ lsirm2pl(spikenslab = FALSE, fixed_gamma = TRUE))</pre>
```

```
lsirm2pl_fixed_gamma_mar
```

2PL LSIRM fixing gamma to 1 for missing at random data.

Description

lsirm2pl_fixed_gamma_mar is used to fit 2PL LSIRM fixing gamma to 1 in incomplete data assumed to be missing at random. lsirm2pl_fixed_gamma_mar factorizes item response matrix into column-wise item effect, row-wise respondent effect and further embeds interaction effect in a latent space, while considering the missing element under the assumption of missing at random. Unlike 1pl model, 2pl model assumes the item effect can vary according to respondent, allowing additional parameter multiplied with respondent effect. The resulting latent space provides an interaction map that represents interactions between respondents and items.

Usage

```
lsirm2pl_fixed_gamma_mar(
  data,
  ndim = 2,
  niter = 15000,
  nburn = 2500,
  nthin = 5,
  nprint = 500,
  jump_beta = 0.4,
  jump_theta = 1,
  jump_alpha = 1,
  jump_z = 0.5,
  jump_w = 0.5,
  pr_mean_beta = 0,
  pr_sd_beta = 1,
  pr_mean_theta = 0,
```

```
pr_sd_theta = 1,
pr_mean_alpha = 0.5,
pr_sd_alpha = 1,
pr_a_theta = 0.001,
pr_b_theta = 0.001,
missing.val = 99,
verbose = FALSE,
fix_theta_sd = FALSE,
fix_alpha_1 = TRUE
)
```

| data | Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item. |
|---------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| ndim | Integer; the dimension of the latent space. Default is 2. |
| niter | Integer; the total number of MCMC iterations to run. Default is 15000. |
| nburn | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500. |
| nthin | Integer; the number of MCMC iterations to thin. Default is 5. |
| nprint | Integer; the interval at which MCMC samples are displayed during execution. Default is 500. |
| jump_beta | Numeric; the jumping rule for the beta proposal density. Default is 0.4. |
| jump_theta | Numeric; the jumping rule for the theta proposal density. Default is 1.0. |
| jump_alpha | Numeric; the jumping rule for the alpha proposal density. Default is 1.0. |
| jump_z | Numeric; the jumping rule for the z proposal density. Default is 0.5. |
| jump_w | Numeric; the jumping rule for the w proposal density. Default is 0.5. |
| pr_mean_beta | Numeric; the mean of the normal prior for beta. Default is 0. |
| pr_sd_beta | Numeric; the standard deviation of the normal prior for beta. Default is 1.0. |
| pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0. |
| pr_sd_theta | Numeric; the standard deviation of the normal prior for theta. Default is 1.0. |
| pr_mean_alpha | Numeric; the mean of the log normal prior for alpha. Default is 0.5. |
| pr_sd_alpha | Numeric; the standard deviation of the \log normal prior for alpha. Default is $1.0.$ |
| pr_a_theta | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001 . |
| pr_b_theta | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001 . |
| missing.val | Numeric; A number to replace missing values. Default is 99. |
| verbose | Logical; If TRUE, MCMC samples are printed for each nprint. Default is FALSE. |
| | |

fix_theta_sd Logical; If TRUE, the standard deviation of the theta parameter is fixed. Default

is FALSE.

fix_alpha_1 Logical; If TRUE, the first element of the alpha parameter is fixed to 1. Default

is TRUE.

Details

lsirm2pl_fixed_gamma_mar models the probability of correct response by respondent j to item i with item effect β_i , respondent effect θ_j and the distance between latent position w_i of item i and latent position z_j of respondent j in the shared metric space. For 2pl model, the the item effect is assumed to have additional discrimination parameter α_i multiplied by θ_i :

$$logit(P(Y_{j,i} = 1 | \theta_j, \alpha_i, \beta_i, z_j, w_i)) = \theta_j * \alpha_i + \beta_i - ||z_j - w_i||$$

Under the assumption of missing at random, the model takes the missing element into consideration in the sampling procedure. For the details of missing at random assumption and data augmentation, see References.

Value

lsirm2pl_fixed_gamma_mar returns an object of list containing the following components:

data Data frame or matrix containing the variables in the model.

missing.val A number to replace missing values.

bic Numeric value with the corresponding BIC.

mcmc_inf Details about the number of MCMC iterations, burn-in periods, and thinning

intervals.

map_inf The log maximum a posteriori (MAP) value and the iteration number at which

this MAP value occurs.

beta_estimate Posterior estimates of the beta parameter.

theta_estimate Posterior estimates of the theta parameter.

sigma_theta_estimate

Posterior estimates of the standard deviation of theta.

z_estimate Posterior estimates of the z parameter. w_estimate Posterior estimates of the w parameter.

imp_estimate Probability of imputating a missing value with 1.

beta Posterior samples of the beta parameter.
theta Posterior samples of the theta parameter.

theta_sd Posterior samples of the standard deviation of theta.

z Posterior samples of the z parameter, represented as a 3-dimensional matrix

where the last axis denotes the dimension of the latent space.

w Posterior samples of the w parameter, represented as a 3-dimensional matrix

where the last axis denotes the dimension of the latent space.

z_raw Posterior samples of the z parameter without procrustes matching.

Posterior samples of the w parameter without procrustes matching. w_raw Imputation for missing Values using posterior samples. imp Acceptance ratio for the beta parameter. accept_beta accept_theta Acceptance ratio for the theta parameter. Acceptance ratio for the z parameter. accept_z accept_w Acceptance ratio for the w parameter. alpha_estimate Posterior estimates of the alpha parameter. alpha Posterior estimates of the alpha parameter. accept_alpha Acceptance ratio for the alpha parameter.

References

Little, R. J., & Rubin, D. B. (2019). Statistical analysis with missing data (Vol. 793). John Wiley & Sons.

Examples

lsirm2pl_fixed_gamma_mcar

2PL LSIRM fixing gamma to 1 for missing completely at random data.

Description

Isirm2pl_fixed_gamma_mcar is used to fit 2PL LSIRM fixing gamma to 1 in incomplete data assumed to be missing completely at random. Isirm2pl_fixed_gamma_mcar factorizes item response matrix into column-wise item effect, row-wise respondent effect and further embeds interaction effect in a latent space, while ignoring the missing element under the assumption of missing completely at random. Unlike 1pl model, 2pl model assumes the item effect can vary according to respondent, allowing additional parameter multiplied with respondent effect. The resulting latent space provides an interaction map that represents interactions between respondents and items.

Usage

```
lsirm2pl_fixed_gamma_mcar(
  data,
  ndim = 2,
 niter = 15000,
 nburn = 2500,
  nthin = 5,
  nprint = 500,
  jump\_beta = 0.4,
  jump\_theta = 1,
  jump_alpha = 1,
  jump_z = 0.5,
  jump_w = 0.5,
  pr_mean_beta = 0,
  pr_sd_beta = 1,
  pr_mean_theta = 0,
  pr_sd_theta = 1,
  pr_mean_alpha = 0.5,
  pr_sd_alpha = 1,
 pr_a_theta = 0.001,
 pr_b_ten = 0.001,
 missing.val = 99,
  verbose = FALSE,
  fix_theta_sd = FALSE,
  fix_alpha_1 = TRUE
)
```

| data | Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item. |
|--------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| ndim | Integer; the dimension of the latent space. Default is 2. |
| niter | Integer; the total number of MCMC iterations to run. Default is 15000. |
| nburn | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500. |
| nthin | Integer; the number of MCMC iterations to thin. Default is 5. |
| nprint | Integer; the interval at which MCMC samples are displayed during execution. Default is 500. |
| jump_beta | Numeric; the jumping rule for the beta proposal density. Default is 0.4. |
| jump_theta | Numeric; the jumping rule for the theta proposal density. Default is 1.0. |
| jump_alpha | Numeric; the jumping rule for the alpha proposal density. Default is 1.0. |
| jump_z | Numeric; the jumping rule for the z proposal density. Default is 0.5. |
| jump_w | Numeric; the jumping rule for the w proposal density. Default is 0.5. |
| pr_mean_beta | Numeric; the mean of the normal prior for beta. Default is 0. |

| pr_sd_beta | Numeric; the standard deviation of the normal prior for beta. Default is 1.0. |
|---------------|------------------------------------------------------------------------------------------------------|
| pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0. |
| pr_sd_theta | Numeric; the standard deviation of the normal prior for theta. Default is 1.0. |
| pr_mean_alpha | Numeric; the mean of the log normal prior for alpha. Default is 0.5. |
| pr_sd_alpha | Numeric; the standard deviation of the log normal prior for alpha. Default is 1.0. |
| pr_a_theta | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001. |
| pr_b_theta | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001. |
| missing.val | Numeric; A number to replace missing values. Default is 99. |
| verbose | Logical; If TRUE, MCMC samples are printed for each nprint. Default is FALSE. |
| fix_theta_sd | Logical; If TRUE, the standard deviation of the theta parameter is fixed. Default is FALSE. |
| fix_alpha_1 | Logical; If TRUE, the first element of the alpha parameter is fixed to 1. Default is TRUE. |

Details

lsirm2pl_fixed_gamma_mcar models the probability of correct response by respondent j to item i with item effect β_i , respondent effect θ_j and the distance between latent position w_i of item i and latent position z_j of respondent j in the shared metric space. For 2pl model, the the item effect is assumed to have additional discrimination parameter α_i multiplied by θ_j :

$$logit(P(Y_{j,i} = 1 | \theta_j, \alpha_i, \beta_i, z_j, w_i)) = \theta_j * \alpha_i + \beta_i - ||z_j - w_i||$$

Under the assumption of missing completely at random, the model ignores the missing element in doing inference. For the details of missing completely at random assumption and data augmentation, see References.

Value

lsirm2pl_fixed_gamma_mar returns an object of list containing the following components:

Data frame or matrix containing the variables in the model.

Missing.val A number to replace missing values.

Dic Numeric value with the corresponding BIC.

McMc iterations, burn-in periods, and thinning intervals.

The log maximum a posteriori (MAP) value and the iteration number at which this MAP value occurs.

Details about the number of MCMC iterations, burn-in periods, and thinning intervals.

theta_estimate Posterior estimates of the theta parameter.

| sigma_theta_estimate | |
|----------------------|--------------------------------------------------------------------------------------------------------------------------------------------|
| | Posterior estimates of the standard deviation of theta. |
| z_estimate | Posterior estimates of the z parameter. |
| w_estimate | Posterior estimates of the w parameter. |
| beta | Posterior samples of the beta parameter. |
| theta | Posterior samples of the theta parameter. |
| theta_sd | Posterior samples of the standard deviation of theta. |
| Z | Posterior samples of the z parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space. |
| W | Posterior samples of the w parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space. |
| z_raw | Posterior samples of the z parameter without procrustes matching. |
| w_raw | Posterior samples of the w parameter without procrustes matching. |
| accept_beta | Acceptance ratio for the beta parameter. |
| accept_theta | Acceptance ratio for the theta parameter. |
| accept_z | Acceptance ratio for the z parameter. |
| accept_w | Acceptance ratio for the w parameter. |
| alpha_estimate | Posterior estimates of the alpha parameter. |
| alpha | Posterior estimates of the alpha parameter. |
| accept_alpha | Acceptance ratio for the alpha parameter. |

References

Little, R. J., & Rubin, D. B. (2019). Statistical analysis with missing data (Vol. 793). John Wiley & Sons.

Examples

```
# generate example item response matrix
data <- matrix(rbinom(500, size = 1, prob = 0.5),ncol=10,nrow=50)

# generate example missing indicator matrix
missing_mat <- matrix(rbinom(500, size = 1, prob = 0.2),ncol=10,nrow=50)

# make missing value with missing indicator matrix
data[missing_mat==1] <- 99

lsirm_result <- lsirm2pl_fixed_gamma_mcar(data)

# The code following can achieve the same result.
lsirm_result <- lsirm(data ~ lsirm2pl(spikenslab = FALSE, fixed_gamma = TRUE, missing_data = "mcar"))</pre>
```

82 lsirm2pl_mar

lsirm2pl_mar

2PL LSIRM for missing at random data.

Description

Isirm2pl_mar is used to fit 2PL LSIRM in incomplete data assumed to be missing at random. Isirm2pl_mar factorizes item response matrix into column-wise item effect, row-wise respondent effect in a latent space, while considering the missing element under the assumption of missing at random. Unlike 1PL model, 2PL model assumes the item effect can vary according to respondent, allowing additional parameter multiplied with respondent effect. The resulting latent space provides an interaction map that represents interactions between respondents and items.

Usage

```
lsirm2pl_mar(
  data,
  ndim = 2,
  niter = 15000,
  nburn = 2500,
  nthin = 5,
  nprint = 500,
  jump_beta = 0.4,
  jump\_theta = 1,
  jump_alpha = 1,
  jump_gamma = 0.025,
  jump_z = 0.5,
  jump_w = 0.5,
  pr_mean_beta = 0,
  pr_sd_beta = 1,
 pr_mean_theta = 0,
  pr_sd_theta = 1,
  pr_mean_gamma = 0.5,
  pr_sd_gamma = 1,
  pr_mean_alpha = 0.5,
  pr_sd_alpha = 1,
  pr_a_theta = 0.001,
  pr_b_ten = 0.001,
 missing.val = 99,
  verbose = FALSE,
  fix_{theta_sd} = FALSE,
  fix_alpha_1 = TRUE
)
```

Arguments

data

Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item.

lsirm2pl_mar 83

| ndim | Integer; the dimension of the latent space. Default is 2. |
|---------------|---------------------------------------------------------------------------------------------------------|
| niter | Integer; the total number of MCMC iterations to run. Default is 15000. |
| nburn | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500 . |
| nthin | Integer; the number of MCMC iterations to thin. Default is 5. |
| nprint | Integer; the interval at which MCMC samples are displayed during execution. Default is 500. |
| jump_beta | Numeric; the jumping rule for the beta proposal density. Default is 0.4. |
| jump_theta | Numeric; the jumping rule for the theta proposal density. Default is 1.0. |
| jump_alpha | Numeric; the jumping rule for the alpha proposal density. Default is 1.0. |
| jump_gamma | Numeric; the jumping rule for the gamma proposal density. Default is 0.025. |
| jump_z | Numeric; the jumping rule for the z proposal density. Default is 0.5. |
| jump_w | Numeric; the jumping rule for the w proposal density. Default is 0.5. |
| pr_mean_beta | Numeric; the mean of the normal prior for beta. Default is 0. |
| pr_sd_beta | Numeric; the standard deviation of the normal prior for beta. Default is 1.0. |
| pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0. |
| pr_sd_theta | Numeric; the standard deviation of the normal prior for theta. Default is 1.0. |
| pr_mean_gamma | Numeric; mean of log normal prior for gamma. Default is 0.5. |
| pr_sd_gamma | Numeric; standard deviation of log normal prior for gamma. Default is 1.0. |
| pr_mean_alpha | Numeric; the mean of the log normal prior for alpha. Default is 0.5. |
| pr_sd_alpha | Numeric; the standard deviation of the \log normal prior for alpha. Default is $1.0.$ |
| pr_a_theta | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001 . |
| pr_b_theta | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001 . |
| missing.val | Numeric; A number to replace missing values. Default is 99. |
| verbose | Logical; If TRUE, MCMC samples are printed for each nprint. Default is FALSE. |
| fix_theta_sd | Logical; If TRUE, the standard deviation of the theta parameter is fixed. Default is FALSE. |
| fix_alpha_1 | Logical; If TRUE, the first element of the alpha parameter is fixed to 1. Default is TRUE. |

Details

lsirm2pl_mar models the probability of correct response by respondent j to item i with item effect β_i , respondent effect θ_j in the shared metric space, with γ represents the weight of the distance term. For 2pl model, the the item effect is assumed to have additional discrimination parameter α_i multiplied by θ_j :

$$logit(P(Y_{j,i} = 1 | \theta_j, \alpha_i, \beta_i, \gamma, z_j, w_i)) = \theta_j * \alpha_i + \beta_i - \gamma ||z_j - w_i||$$

Under the assumption of missing at random, the model takes the missing element into consideration in the sampling procedure. For the details of missing at random assumption and data augmentation, see References.

84 lsirm2pl_mar

Value

lsirm2pl_mar returns an object of list containing the following components:

data Data frame or matrix containing the variables in the model.

missing.val A number to replace missing values.

bic Numeric value with the corresponding BIC.

mcmc_inf Details about the number of MCMC iterations, burn-in periods, and thinning

intervals.

map_inf The log maximum a posteriori (MAP) value and the iteration number at which

this MAP value occurs.

beta_estimate Posterior estimates of the beta parameter.
theta_estimate Posterior estimates of the theta parameter.

sigma_theta_estimate

Posterior estimates of the standard deviation of theta.

gamma_estimate posterior estimates of gamma parameter.

z_estimate Posterior estimates of the z parameter.

w_estimate Posterior estimates of the w parameter.

imp_estimate Probability of imputating a missing value with 1.

beta Posterior samples of the beta parameter.
theta Posterior samples of the theta parameter.
gamma Posterior samples of the gamma parameter.

theta_sd Posterior samples of the standard deviation of theta.

z Posterior samples of the z parameter, represented as a 3-dimensional matrix

where the last axis denotes the dimension of the latent space.

Posterior samples of the w parameter, represented as a 3-dimensional matrix

where the last axis denotes the dimension of the latent space.

z_raw Posterior samples of the z parameter without procrustes matching.
w_raw Posterior samples of the w parameter without procrustes matching.

imp Imputation for missing Values using posterior samples.

accept_beta Acceptance ratio for the beta parameter.

accept_theta Acceptance ratio for the theta parameter.

accept_z Acceptance ratio for the z parameter.

accept_w Acceptance ratio for the w parameter.

accept_gamma Acceptance ratio for the gamma parameter.

alpha_estimate Posterior estimates of the alpha parameter.

alpha Posterior estimates of the alpha parameter.

 Isirm2pl_mar_ss 85

References

Little, R. J., & Rubin, D. B. (2019). Statistical analysis with missing data (Vol. 793). John Wiley & Sons

Examples

```
# generate example item response matrix
data <- matrix(rbinom(500, size = 1, prob = 0.5), ncol=10, nrow=50)

# generate example missing indicator matrix
missing_mat <- matrix(rbinom(500, size = 1, prob = 0.2), ncol=10, nrow=50)

# make missing value with missing indicator matrix
data[missing_mat==1] <- 99

lsirm_result <- lsirm2pl_mar(data)

# The code following can achieve the same result.
lsirm_result <- lsirm(data ~ lsirm2pl(spikenslab = FALSE, fixed_gamma = FALSE, missing_data = "mar"))</pre>
```

lsirm2pl_mar_ss

2PL LSIRM with model selection approach for missing at random data.

Description

lsirm2pl_mar_ss is used to fit 2PL LSIRM based on spike-and-slab priors in incomplete data assumed to be missing at random. lsirm2pl_mar_ss factorizes item response matrix into column-wise item effect, row-wise respondent effect in a latent space, while considering the missing element under the assumption of missing at random. Unlike 1PL model, 2PL model assumes the item effect can vary according to respondent, allowing additional parameter multiplied with respondent effect. The resulting latent space provides an interaction map that represents interactions between respondents and items.

Usage

```
lsirm2pl_mar_ss(
   data,
   ndim = 2,
   niter = 15000,
   nburn = 2500,
   nthin = 5,
   nprint = 500,
   jump_beta = 0.4,
   jump_theta = 1,
   jump_alpha = 1,
```

86 lsirm2pl_mar_ss

```
jump_gamma = 1,
  jump_z = 0.5,
 jump_w = 0.5,
 pr_mean_beta = 0,
 pr_sd_beta = 1,
 pr_mean_theta = 0,
 pr_sd_theta = 1,
 pr_spike_mean = -3,
 pr_spike_sd = 1,
 pr_slab_mean = 0.5,
 pr_slab_sd = 1,
 pr_mean_alpha = 0.5,
 pr_sd_alpha = 1,
 pr_a_theta = 0.001,
 pr_b_t = 0.001,
 pr_xi_a = 1,
 pr_xi_b = 1,
 missing.val = 99,
 verbose = FALSE,
 fix_theta_sd = FALSE,
 fix_alpha_1 = TRUE
)
```

| data | Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item. |
|---------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| ndim | Integer; the dimension of the latent space. Default is 2. |
| niter | Integer; the total number of MCMC iterations to run. Default is 15000. |
| nburn | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500. |
| nthin | Integer; the number of MCMC iterations to thin. Default is 5. |
| nprint | Integer; the interval at which MCMC samples are displayed during execution. Default is 500. |
| jump_beta | Numeric; the jumping rule for the beta proposal density. Default is 0.4. |
| jump_theta | Numeric; the jumping rule for the theta proposal density. Default is 1.0. |
| jump_alpha | Numeric; the jumping rule for the alpha proposal density. Default is 1.0. |
| jump_gamma | Numeric; the jumping rule for the theta proposal density. Default is 1.0. |
| jump_z | Numeric; the jumping rule for the z proposal density. Default is 0.5. |
| jump_w | Numeric; the jumping rule for the w proposal density. Default is 0.5. |
| pr_mean_beta | Numeric; the mean of the normal prior for beta. Default is 0. |
| pr_sd_beta | Numeric; the standard deviation of the normal prior for beta. Default is 1.0. |
| pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0. |

lsirm2pl_mar_ss 87

| pr_sd_theta | Numeric; the standard deviation of the normal prior for theta. Default is 1.0. |
|---------------|------------------------------------------------------------------------------------------------------|
| pr_spike_mean | Numeric; the mean of spike prior for log gamma. Default is -3. |
| pr_spike_sd | Numeric; the standard deviation of spike prior for log gamma. Default is 1. |
| pr_slab_mean | Numeric; the mean of spike prior for log gamma. Default is 0.5. |
| pr_slab_sd | Numeric; the standard deviation of spike prior for log gamma. Default is is 1. |
| pr_mean_alpha | Numeric; the mean of the log normal prior for alpha. Default is 0.5. |
| pr_sd_alpha | Numeric; the standard deviation of the log normal prior for alpha. Default is 1.0. |
| pr_a_theta | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001. |
| pr_b_theta | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001. |
| pr_xi_a | Numeric; the first shape parameter of beta prior for latent variable xi. Default is 1. |
| pr_xi_b | Numeric; the second shape parameter of beta prior for latent variable xi. Default is 1. |
| missing.val | Numeric; a number to replace missing values. Default is 99. |
| verbose | Logical; If TRUE, MCMC samples are printed for each nprint. Default is FALSE. |
| fix_theta_sd | Logical; If TRUE, the standard deviation of the theta parameter is fixed. Default is FALSE. |
| fix_alpha_1 | Logical; If TRUE, the first element of the alpha parameter is fixed to 1. Default is TRUE. |

Details

lsirm2pl_mar_ss models the probability of correct response by respondent j to item i with item effect β_i , respondent effect θ_j in the shared metric space, with γ represents the weight of the distance term. For 2pl model, the the item effect is assumed to have additional discrimination parameter α_i multiplied by θ_j :

$$logit(P(Y_{i,i} = 1 | \theta_i, \alpha_i, \beta_i, \gamma, z_i, w_i)) = \theta_i * \alpha_i + \beta_i - \gamma ||z_i - w_i||$$

Under the assumption of missing at random, the model takes the missing element into consideration in the sampling procedure. For the details of missing at random assumption and data augmentation, see References. lsirm2pl_mar_ss model include model selection approach based on spike-and-slab priors for log gamma. For detail of spike-and-slab priors, see References.

Value

lsirm2pl_mar_ss returns an object of list containing the following components:

data Data frame or matrix containing the variables in the model.

missing.val A number to replace missing values.

bic Numeric value with the corresponding BIC.

88 lsirm2pl_mar_ss

mcmc_inf Details about the number of MCMC iterations, burn-in periods, and thinning intervals.

map_inf The log maximum a posteriori (MAP) value and the iteration number at which

this MAP value occurs.

beta_estimate Posterior estimates of the beta parameter. theta_estimate Posterior estimates of the theta parameter.

sigma_theta_estimate

Posterior estimates of the standard deviation of theta.

gamma_estimate posterior estimates of gamma parameter.

z_estimate Posterior estimates of the z parameter.

w_estimate Posterior estimates of the w parameter.

z_rawPosterior samples of the z parameter without procrustes matching.w_rawPosterior samples of the w parameter without procrustes matching.

beta Posterior samples of the beta parameter.
theta Posterior samples of the theta parameter.
gamma Posterior samples of the gamma parameter.

theta_sd Posterior samples of the standard deviation of theta.

z Posterior samples of the z parameter, represented as a 3-dimensional matrix

where the last axis denotes the dimension of the latent space.

Posterior samples of the w parameter, represented as a 3-dimensional matrix

where the last axis denotes the dimension of the latent space.

pi Posterior samples of phi which is indicator of spike and slab prior. If phi is 1,

 \log gamma follows the slab prior, otherwise follows the spike prior.

imp Imputation for missing Values using posterior samples.

accept_beta Acceptance ratio for the beta parameter.
accept_theta Acceptance ratio for the theta parameter.
accept_z Acceptance ratio for the z parameter.
accept_w Acceptance ratio for the w parameter.
accept_gamma Acceptance ratio for the gamma parameter.

pi_estimate Posterior estimation of phi. inclusion probability of gamma. if estimation of phi

is less than 0.5, choose Rasch model with gamma = 0, otherwise latent space

model with gamma > 0.

imp_estimate Probability of imputating a missing value with 1.

alpha_estimate Posterior estimates of the alpha parameter.
alpha Posterior estimates of the alpha parameter.
accept_alpha Acceptance ratio for the alpha parameter.

References

Little, R. J., & Rubin, D. B. (2019). Statistical analysis with missing data (Vol. 793). John Wiley & Sons. Ishwaran, H., & Rao, J. S. (2005). Spike and slab variable selection: Frequentist and Bayesian strategies. The Annals of Statistics, 33(2), 730-773.

Isirm2pl_mcar 89

Examples

```
# generate example item response matrix
data <- matrix(rbinom(500, size = 1, prob = 0.5), ncol=10, nrow=50)

# generate example missing indicator matrix
missing_mat <- matrix(rbinom(500, size = 1, prob = 0.2), ncol=10, nrow=50)

# make missing value with missing indicator matrix
data[missing_mat==1] <- 99

lsirm_result <- lsirm2pl_mar_ss(data)

# The code following can achieve the same result.
lsirm_result <- lsirm(data ~ lsirm2pl(spikenslab = TRUE, fixed_gamma = FALSE, missing_data = "mar"))</pre>
```

lsirm2pl_mcar

2PL LSIRM for missing completely at random data.

Description

lsirm2pl_mcar is used to fit 2PL LSIRM in incomplete data assumed to be missing completely at random. lsirm2pl_mcar factorizes item response matrix into column-wise item effect, row-wise respondent effect in a latent space, while ignoring the missing element under the assumption of missing completely at random. Unlike 1PL model, 2PL model assumes the item effect can vary according to respondent, allowing additional parameter multiplied with respondent effect. The resulting latent space provides an interaction map that represents interactions between respondents and items.

Usage

```
lsirm2pl_mcar(
  data,
  ndim = 2,
  niter = 15000,
  nburn = 2500,
  nthin = 5,
  nprint = 500,
  jump\_beta = 0.4,
  jump\_theta = 1,
  jump_alpha = 1,
  jump_gamma = 0.025,
  jump_z = 0.5,
  jump_w = 0.5,
  pr_mean_beta = 0,
  pr_sd_beta = 1,
  pr_mean_theta = 0,
```

90 lsirm2pl_mcar

```
pr_sd_theta = 1,
pr_mean_gamma = 0.5,
pr_sd_gamma = 1,
pr_mean_alpha = 0.5,
pr_sd_alpha = 1,
pr_a_theta = 0.001,
pr_b_theta = 0.001,
missing.val = 99,
verbose = FALSE,
fix_theta_sd = FALSE,
fix_alpha_1 = TRUE
)
```

| data | Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item. |
|---------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| ndim | Integer; the dimension of the latent space. Default is 2. |
| niter | Integer; the total number of MCMC iterations to run. Default is 15000. |
| nburn | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500. |
| nthin | Integer; the number of MCMC iterations to thin. Default is 5. |
| nprint | Integer; the interval at which MCMC samples are displayed during execution. Default is 500. |
| jump_beta | Numeric; the jumping rule for the beta proposal density. Default is 0.4. |
| jump_theta | Numeric; the jumping rule for the theta proposal density. Default is 1.0. |
| jump_alpha | Numeric; the jumping rule for the alpha proposal density. Default is 1.0. |
| jump_gamma | Numeric; the jumping rule for the gamma proposal density. Default is 0.025 |
| jump_z | Numeric; the jumping rule for the z proposal density. Default is 0.5. |
| jump_w | Numeric; the jumping rule for the w proposal density. Default is 0.5. |
| pr_mean_beta | Numeric; the mean of the normal prior for beta. Default is 0. |
| pr_sd_beta | Numeric; the standard deviation of the normal prior for beta. Default is 1.0. |
| pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0. |
| pr_sd_theta | Numeric; the standard deviation of the normal prior for theta. Default is 1.0. |
| pr_mean_gamma | Numeric; mean of log normal prior for gamma. Default is 0.5. |
| pr_sd_gamma | Numeric; standard deviation of log normal prior for gamma. Default is 1.0. |
| pr_mean_alpha | Numeric; the mean of the log normal prior for alpha. Default is 0.5. |
| pr_sd_alpha | Numeric; the standard deviation of the log normal prior for alpha. Default is 1.0. |
| pr_a_theta | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001 . |

Isirm2pl_mcar 91

pr_b_theta Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001.

missing.val Numeric; A number to replace missing values. Default is 99.

verbose Logical; If TRUE, MCMC samples are printed for each nprint. Default is FALSE.

fix_theta_sd Logical; If TRUE, the standard deviation of the theta parameter is fixed. Default is FALSE.

fix_alpha_1 Logical; If TRUE, the first element of the alpha parameter is fixed to 1. Default is TRUE.

Details

lsirm2pl_mcar models the probability of correct response by respondent j to item i with item effect β_i , respondent effect θ_j in the shared metric space, with γ represents the weight of the distance term. For 2pl model, the the item effect is assumed to have additional discrimination parameter α_i multiplied by θ_j :

$$logit(P(Y_{j,i} = 1 | \theta_j, \alpha_i, \beta_i, \gamma, z_j, w_i)) = \theta_j * \alpha_i + \beta_i - \gamma ||z_j - w_i||$$

Under the assumption of missing completely at random, the model ignores the missing element in doing inference. For the details of missing completely at random assumption and data augmentation, see References.

Value

lsirm2pl_mar returns an object of list containing the following components:

data A data frame or matrix containing the variables used in the model.

missing.val A number to replace missing values.

bic Numeric value with the corresponding BIC.

mcmc_inf Details about the number of MCMC iterations, burn-in periods, and thinning

intervals.

map_inf The log maximum a posteriori (MAP) value and the iteration number at which

this MAP value occurs.

beta_estimate Posterior estimates of the beta parameter.

theta_estimate Posterior estimates of the theta parameter.

sigma_theta_estimate

Posterior estimates of the standard deviation of theta.

gamma_estimate Posterior estimates of gamma parameter.

z_estimate Posterior estimates of the z parameter.

w_estimate Posterior estimates of the w parameter.

beta Posterior samples of the beta parameter.

theta Posterior samples of the theta parameter.

theta_sd Posterior samples of the standard deviation of theta.

92 lsirm2pl_mcar

| gamma | Posterior samples of the gamma parameter. |
|----------------|--------------------------------------------------------------------------------------------------------------------------------------------|
| Z | Posterior samples of the z parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space. |
| W | Posterior samples of the w parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space. |
| z_raw | Posterior samples of the z parameter without procrustes matching. |
| w_raw | Posterior samples of the w parameter without procrustes matching. |
| accept_beta | Acceptance ratio for the beta parameter. |
| accept_theta | Acceptance ratio for the theta parameter. |
| accept_z | Acceptance ratio for the z parameter. |
| accept_w | Acceptance ratio for the w parameter. |
| accept_gamma | Acceptance ratio for the gamma parameter. |
| alpha_estimate | Posterior estimates of the alpha parameter. |
| alpha | Posterior estimates of the alpha parameter. |
| accept_alpha | Acceptance ratio for the alpha parameter. |

References

Little, R. J., & Rubin, D. B. (2019). Statistical analysis with missing data (Vol. 793). John Wiley & Sons.

Examples

```
# generate example item response matrix
data <- matrix(rbinom(500, size = 1, prob = 0.5), ncol=10, nrow=50)

# generate example missing indicator matrix
missing_mat <- matrix(rbinom(500, size = 1, prob = 0.2), ncol=10, nrow=50)

# make missing value with missing indicator matrix
data[missing_mat==1] <- 99

lsirm_result <- lsirm2pl_mcar(data)

# The code following can achieve the same result.
lsirm_result <- lsirm(data ~ lsirm2pl(spikenslab = FALSE, fixed_gamma = FALSE, missing_data = "mcar"))</pre>
```

lsirm2pl_mcar_ss 93

lsirm2pl_mcar_ss

2PL LSIRM with model selection approach for missing completely at random data.

Description

lsirm2pl_mar_ss is used to fit 2PL LSIRM based on spike-and-slab priors in incomplete data assumed to be missing completely at random. lsirm2pl_mar_ss factorizes item response matrix into column-wise item effect, row-wise respondent effect in a latent space, while ignoring the missing element under the assumption of missing completely at random. Unlike 1PL model, 2PL model assumes the item effect can vary according to respondent, allowing additional parameter multiplied with respondent effect. The resulting latent space provides an interaction map that represents interactions between respondents and items.

Usage

```
lsirm2pl_mcar_ss(
  data,
  ndim = 2,
  niter = 15000,
  nburn = 2500,
  nthin = 5,
  nprint = 500,
  jump_beta = 0.4,
  jump\_theta = 1,
  jump_alpha = 1,
  jump_gamma = 1,
  jump_z = 0.5,
  jump_w = 0.5,
  pr_mean_beta = 0,
  pr_sd_beta = 1,
  pr_mean_theta = 0,
 pr_sd_theta = 1,
 pr_spike_mean = -3,
  pr_spike_sd = 1,
  pr_slab_mean = 0.5,
 pr_slab_sd = 1,
  pr_mean_alpha = 0.5,
  pr_sd_alpha = 1,
 pr_a_theta = 0.001,
 pr_b_t = 0.001,
  pr_xi_a = 1,
  pr_xi_b = 1,
 missing.val = 99,
  verbose = FALSE,
  fix_{theta_sd} = FALSE,
  fix_alpha_1 = TRUE
```

94 lsirm2pl_mcar_ss

)

| ٠ | - | |
|---|---------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| | data | Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item. |
| | ndim | Integer; the dimension of the latent space. Default is 2. |
| | niter | Integer; the total number of MCMC iterations to run. Default is 15000. |
| | nburn | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500. |
| | nthin | Integer; the number of MCMC iterations to thin. Default is 5. |
| | nprint | Integer; the interval at which MCMC samples are displayed during execution. Default is 500. |
| | jump_beta | Numeric; the jumping rule for the beta proposal density. Default is 0.4. |
| | jump_theta | Numeric; the jumping rule for the theta proposal density. Default is 1.0. |
| | jump_alpha | Numeric; the jumping rule for the alpha proposal density. Default is 1.0. |
| | jump_gamma | Numeric; the jumping rule for the theta proposal density. Default is 1.0. |
| | jump_z | Numeric; the jumping rule for the z proposal density. Default is 0.5. |
| | jump_w | Numeric; the jumping rule for the w proposal density. Default is 0.5. |
| | pr_mean_beta | Numeric; the mean of the normal prior for beta. Default is 0. |
| | pr_sd_beta | Numeric; the standard deviation of the normal prior for beta. Default is 1.0. |
| | pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0. |
| | pr_sd_theta | Numeric; the standard deviation of the normal prior for theta. Default is 1.0. |
| | pr_spike_mean | Numeric; the mean of spike prior for log gamma. Default is -3. |
| | pr_spike_sd | Numeric; the standard deviation of spike prior for log gamma. Default is 1. |
| | pr_slab_mean | Numeric; the mean of spike prior for log gamma. Default is 0.5. |
| | pr_slab_sd | Numeric; the standard deviation of spike prior for log gamma. Default is 1. |
| | pr_mean_alpha | Numeric; the mean of the log normal prior for alpha. Default is 0.5. |
| | pr_sd_alpha | Numeric; the standard deviation of the log normal prior for alpha. Default is 1.0. |
| | pr_a_theta | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001. |
| | pr_b_theta | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001. |
| | pr_xi_a | Numeric; the first shape parameter of beta prior for latent variable xi. Default is 1. |
| | pr_xi_b | Numeric; the second shape parameter of beta prior for latent variable xi. Default is 1. |
| | missing.val | Numeric; a number to replace missing values. Default is 99. |
| | | |

Isirm2pl_mcar_ss 95

verbose Logical; If TRUE, MCMC samples are printed for each nprint. Default is

FALSE.

fix_theta_sd Logical; If TRUE, the standard deviation of the theta parameter is fixed. Default

is FALSE.

fix_alpha_1 Logical; If TRUE, the first element of the alpha parameter is fixed to 1. Default

is TRUE.

Details

lsirm2pl_mcar_ss models the probability of correct response by respondent j to item i with item effect β_i , respondent effect θ_j in the shared metric space, with γ represents the weight of the distance term. For 2pl model, the the item effect is assumed to have additional discrimination parameter α_i multiplied by θ_j :

$$logit(P(Y_{j,i} = 1 | \theta_j, \alpha_i, \beta_i, \gamma, z_j, w_i)) = \theta_j * \alpha_i + \beta_i - \gamma ||z_j - w_i||$$

Under the assumption of missing at random, the model takes the missing element into consideration in the sampling procedure. For the details of missing at random assumption and data augmentation, see References. lsirm2pl_mcar_ss model include model selection approach based on spike-and-slab priors for log gamma. For detail of spike-and-slab priors, see References.

Value

lsirm2pl_mar_ss returns an object of list containing the following components:

data Data frame or matrix containing the variables in the model.

missing.val A number to replace missing values.

bic Numeric value with the corresponding BIC.

mcmc_inf Details about the number of MCMC iterations, burn-in periods, and thinning

intervals.

map_inf The log maximum a posteriori (MAP) value and the iteration number at which

this MAP value occurs.

beta_estimate Posterior estimates of the beta parameter.

theta_estimate Posterior estimates of the theta parameter.

sigma_theta_estimate

Posterior estimates of the standard deviation of theta.

gamma_estimate posterior estimates of gamma parameter.

z_estimate Posterior estimates of the z parameter.

w_estimate Posterior estimates of the w parameter.

beta Posterior samples of the beta parameter.

theta Posterior samples of the theta parameter.

gamma Posterior samples of the gamma parameter.

theta_sd Posterior samples of the standard deviation of theta.

Posterior samples of the z parameter, represented as a 3-dimensional matrix

where the last axis denotes the dimension of the latent space.

96 lsirm2pl_mcar_ss

| W | Posterior samples of the w parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space. |
|----------------|--------------------------------------------------------------------------------------------------------------------------------------------------------|
| z_raw | Posterior samples of the z parameter without procrustes matching. |
| w_raw | Posterior samples of the w parameter without procrustes matching. |
| pi | Posterior samples of phi which is indicator of spike and slab prior. If phi is 1, log gamma follows the slab prior, otherwise follows the spike prior. |
| accept_beta | Acceptance ratio for the beta parameter. |
| accept_theta | Acceptance ratio for the theta parameter. |
| accept_z | Acceptance ratio for the z parameter. |
| accept_w | Acceptance ratio for the w parameter. |
| accept_gamma | Acceptance ratio for the gamma parameter. |
| alpha_estimate | Posterior estimates of the alpha parameter. |
| alpha | Posterior estimates of the alpha parameter. |
| accept_alpha | Acceptance ratio for the alpha parameter. |

References

Little, R. J., & Rubin, D. B. (2019). Statistical analysis with missing data (Vol. 793). John Wiley & Sons. Ishwaran, H., & Rao, J. S. (2005). Spike and slab variable selection: Frequentist and Bayesian strategies. The Annals of Statistics, 33(2), 730-773.

Examples

```
# generate example item response matrix
data <- matrix(rbinom(500, size = 1, prob = 0.5), ncol=10, nrow=50)

# generate example missing indicator matrix
missing_mat <- matrix(rbinom(500, size = 1, prob = 0.2), ncol=10, nrow=50)

# make missing value with missing indicator matrix
data[missing_mat==1] <- 99

lsirm_result <- lsirm2pl_mcar_ss(data)

# The code following can achieve the same result.
lsirm_result <- lsirm(data ~ lsirm2pl(spikenslab = TRUE, fixed_gamma = FALSE, missing_data = "mcar"))</pre>
```

```
lsirm2pl_normal_fixed_gamma
```

2PL LSIRM fixing gamma to 1 with normal likelihood

Description

lsirm2pl_normal_fixed_gamma is used to fit 2PL LSIRM with gamma fixed to 1 for continuous variable. lsirm2pl_normal_fixed_gamma factorizes item response matrix into column-wise item effect, row-wise respondent effect and further embeds interaction effect in a latent space. Unlike 1PL model, 2PL model assumes the item effect can vary according to respondent, allowing additional parameter multiplied with respondent effect. The resulting latent space provides an interaction map that represents interactions between respondents and items.

Usage

```
lsirm2pl_normal_fixed_gamma(
  data,
  ndim = 2,
  niter = 15000,
  nburn = 2500,
  nthin = 5,
  nprint = 500,
  jump_beta = 0.4,
  jump\_theta = 1,
  jump_alpha = 1,
  jump_z = 0.5,
  jump_w = 0.5,
  pr_mean_beta = 0,
  pr_sd_beta = 1,
  pr_mean_theta = 0,
  pr_sd_theta = 1,
  pr_mean_alpha = 0.5,
  pr_sd_alpha = 1,
  pr_a_theta = 0.001,
  pr_b_t = 0.001,
  pr_a_{eps} = 0.001,
  pr_b_{eps} = 0.001,
  verbose = FALSE,
  fix_{theta_sd} = FALSE,
  fix_alpha_1 = TRUE
)
```

Arguments

data

Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item.

| ndim | Integer; the dimension of the latent space. Default is 2. |
|---------------|-----------------------------------------------------------------------------------------------------------|
| niter | Integer; the total number of MCMC iterations to run. Default is 15000. |
| nburn | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500 . |
| nthin | Integer; the number of MCMC iterations to thin. Default is 5. |
| nprint | Integer; the interval at which MCMC samples are displayed during execution. Default is 500. |
| jump_beta | Numeric; the jumping rule for the beta proposal density. Default is 0.4. |
| jump_theta | Numeric; the jumping rule for the theta proposal density. Default is 1.0. |
| jump_alpha | Numeric; the jumping rule for the alpha proposal density. Default is 1.0. |
| jump_z | Numeric; the jumping rule for the z proposal density. Default is 0.5. |
| jump_w | Numeric; the jumping rule for the w proposal density. Default is 0.5. |
| pr_mean_beta | Numeric; the mean of the normal prior for beta. Default is 0. |
| pr_sd_beta | Numeric; the standard deviation of the normal prior for beta. Default is 1.0. |
| pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0. |
| pr_sd_theta | Numeric; the standard deviation of the normal prior for theta. Default is 1.0. |
| pr_mean_alpha | Numeric; the mean of the log normal prior for alpha. Default is 0.5. |
| pr_sd_alpha | Numeric; the standard deviation of the log normal prior for alpha. Default is 1.0. |
| pr_a_theta | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001 . |
| pr_b_theta | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001 . |
| pr_a_eps | Numeric; the shape parameter of inverse gamma prior for variance of data likelihood. Default is 0.001 . |
| pr_b_eps | Numeric; the scale parameter of inverse gamma prior for variance of data likelihood. Default is 0.001. |
| verbose | Logical; If TRUE, MCMC samples are printed for each nprint. Default is FALSE. |
| fix_theta_sd | Logical; If TRUE, the standard deviation of the theta parameter is fixed. Default is FALSE. |
| fix_alpha_1 | Logical; If TRUE, the first element of the alpha parameter is fixed to 1. Default is TRUE. |
| | |

Details

lsirm2pl_normal_fixed_gamma models the continuous value of response by respondent j to item i with item effect β_i , respondent effect θ_j and the distance between latent position w_i of item i and latent position z_j of respondent j in the shared metric space. For 2pl model, the the item effect is assumed to have additional discrimination parameter α_i multiplied by θ_j :

$$Y_{j,i} = \theta_j + \beta_i - \gamma ||z_j - w_i|| + e_{j,i}$$

where the error $e_{j,i} \sim N(0, \sigma^2)$

Value

lsirm2pl_normal_fixed_gamma returns an object of list containing the following components:

data A data frame or matrix containing the variables used in the model.

bic A numeric value representing the Bayesian Information Criterion (BIC).

mcmc_inf Details about the number of MCMC iterations, burn-in periods, and thinning

intervals.

map_inf The log maximum a posteriori (MAP) value and the iteration number at which

this MAP value occurs.

beta_estimate Posterior estimates of the beta parameter.
theta_estimate Posterior estimates of the theta parameter.

 $sigma_theta_estimate$

Posterior estimates of the standard deviation of theta.

z_estimate
 w_estimate
 beta
 Posterior estimates of the w parameter.
 beta
 Posterior samples of the beta parameter.
 theta
 Posterior samples of the theta parameter.

theta_sd Posterior samples of the standard deviation of theta.

z Posterior samples of the z parameter, represented as a 3-dimensional matrix

where the last axis denotes the dimension of the latent space.

Posterior samples of the w parameter, represented as a 3-dimensional matrix

where the last axis denotes the dimension of the latent space.

z_raw Posterior samples of the z parameter without procrustes matching.
w_raw Posterior samples of the w parameter without procrustes matching.
accept_beta Acceptance ratio for the beta parameter.

accept_beta Acceptance ratio for the beta parameter.

accept_theta Acceptance ratio for the theta parameter.

accept_z Acceptance ratio for the z parameter.

accept_w Acceptance ratio for the w parameter.

sigma_estimate Posterior estimates of the standard deviation.

Posterior samples of the standard deviation.

Posterior estimates of the alpha parameter.

Posterior estimates of the alpha parameter.

Accept_alpha Acceptance ratio for the alpha parameter.

Examples

```
# generate example (continuous) item response matrix
data <- matrix(rnorm(500, mean = 0, sd = 1),ncol=10,nrow=50)

lsrm_result <- lsirm2pl_normal_fixed_gamma(data)

# The code following can achieve the same result.
lsirm_result <- lsirm(data ~ lsirm2pl(spikenslab = FALSE, fixed_gamma = TRUE))</pre>
```

```
lsirm2pl_normal_fixed_gamma_mar

2PL LSIRM fixing gamma to 1 with normal likelihood for missing at random data.
```

Description

lsirm2pl_normal_fixed_gamma_mar is used to fit 2PL LSIRM with gamma fixed to 1 for continuous variable in incomplete data assumed to be missing at random.

lsirm2pl_normal_fixed_gamma_mar factorizes item response matrix into column-wise item effect, row-wise respondent effect and further embeds interaction effect in a latent space, while considering the missing element under the assumption of missing at random. Unlike 1PL model, 2PL model assumes the item effect can vary according to respondent, allowing additional parameter multiplied with respondent effect. The resulting latent space provides an interaction map that represents interactions between respondents and items.

Usage

```
lsirm2pl_normal_fixed_gamma_mar(
  data,
  ndim = 2,
  niter = 15000,
  nburn = 2500,
  nthin = 5,
  nprint = 500,
  jump\_beta = 0.4,
  jump\_theta = 1,
  jump_alpha = 1,
  jump_z = 0.5,
  jump_w = 0.5,
  pr_mean_beta = 0,
  pr_sd_beta = 1,
  pr_mean_theta = 0,
  pr_sd_theta = 1,
  pr_mean_alpha = 0.5,
  pr_sd_alpha = 1,
  pr_a_theta = 0.001,
  pr_b_t = 0.001,
  pr_a_{eps} = 0.001,
  pr_b_{eps} = 0.001,
 missing.val = 99,
  verbose = FALSE,
  fix_theta_sd = FALSE,
  fix_alpha_1 = TRUE
)
```

| data | Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item. |
|---------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| ndim | Integer; the dimension of the latent space. Default is 2. |
| niter | Integer; the total number of MCMC iterations to run. Default is 15000. |
| nburn | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500. |
| nthin | Integer; the number of MCMC iterations to thin. Default is 5. |
| nprint | Integer; the interval at which MCMC samples are displayed during execution. Default is 500. |
| jump_beta | Numeric; the jumping rule for the beta proposal density. Default is 0.4. |
| jump_theta | Numeric; the jumping rule for the theta proposal density. Default is 1.0. |
| jump_alpha | Numeric; the jumping rule for the alpha proposal density. Default is 1.0. |
| jump_z | Numeric; the jumping rule for the z proposal density. Default is 0.5. |
| jump_w | Numeric; the jumping rule for the w proposal density. Default is 0.5. |
| pr_mean_beta | Numeric; the mean of the normal prior for beta. Default is 0. |
| pr_sd_beta | Numeric; the standard deviation of the normal prior for beta. Default is 1.0. |
| pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0. |
| pr_sd_theta | Numeric; the standard deviation of the normal prior for theta. Default is 1.0. |
| pr_mean_alpha | Numeric; the mean of the log normal prior for alpha. Default is 0.5. |
| pr_sd_alpha | Numeric; the standard deviation of the log normal prior for alpha. Default is 1.0. |
| pr_a_theta | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001. |
| pr_b_theta | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001. |
| pr_a_eps | Numeric; the shape parameter of inverse gamma prior for variance of data likelihood. Default is 0.001. |
| pr_b_eps | Numeric; the scale parameter of inverse gamma prior for variance of data likelihood Default is 0.001. |
| missing.val | Numeric; a number to replace missing values. Default is 99. |
| verbose | Logical; If TRUE, MCMC samples are printed for each nprint. Default is FALSE. |
| fix_theta_sd | Logical; If TRUE, the standard deviation of the theta parameter is fixed. Default is FALSE. |
| fix_alpha_1 | Logical; If TRUE, the first element of the alpha parameter is fixed to 1. Default is TRUE. |

Details

lsirm2pl_normal_fixed_gamma_mar models the continuous value of response by respondent j to item i with item effect β_i , respondent effect θ_j and the distance between latent position w_i of item i and latent position z_j of respondent j in the shared metric space. For 2pl model, the the item effect is assumed to have additional discrimination parameter α_i multiplied by θ_j :

$$Y_{j,i} = \theta_j + \beta_i - \gamma ||z_j - w_i|| + e_{j,i}$$

where the error $e_{j,i} \sim N(0, \sigma^2)$ Under the assumption of missing at random, the model takes the missing element into consideration in the sampling procedure. For the details of missing at random assumption and data augmentation, see References.

Value

lsirm2pl_normal_fixed_gamma_mar returns an object of list containing the following components:

data Data frame or matrix containing the variables in the model.

missing.val A number to replace missing values.

bic Numeric value with the corresponding BIC.

mcmc_inf Details about the number of MCMC iterations, burn-in periods, and thinning

intervals.

map_inf The log maximum a posteriori (MAP) value and the iteration number at which

this MAP value occurs.

beta_estimate Posterior estimates of the beta parameter.
theta_estimate Posterior estimates of the theta parameter.

sigma_theta_estimate

Posterior estimates of the standard deviation of theta.

z_estimate Posterior estimates of the z parameter. w_estimate Posterior estimates of the w parameter.

imp_estimate Probability of imputating a missing value with 1.

beta Posterior samples of the beta parameter.
theta Posterior samples of the theta parameter.

theta_sd Posterior samples of the standard deviation of theta.

z Posterior samples of the z parameter, represented as a 3-dimensional matrix

where the last axis denotes the dimension of the latent space.

w Posterior samples of the w parameter, represented as a 3-dimensional matrix

where the last axis denotes the dimension of the latent space.

z_raw Posterior samples of the z parameter without procrustes matching.w_raw Posterior samples of the w parameter without procrustes matching.

imp Imputation for missing Values using posterior samples.

accept_beta Acceptance ratio for the beta parameter.
accept_theta Acceptance ratio for the theta parameter.

```
accept_z Acceptance ratio for the z parameter.

accept_w Acceptance ratio for the w parameter.

sigma_estimate Posterior estimates of the standard deviation.

sigma Posterior samples of the standard deviation.

alpha_estimate Posterior estimates of the alpha parameter.

alpha Posterior estimates of the alpha parameter.

accept_alpha Acceptance ratio for the alpha parameter.
```

Examples

```
lsirm2pl_normal_fixed_gamma_mcar
```

2PL LSIRM fixing gamma to 1 with normal likelihood for missing completely at random data.

Description

lsirm2pl_normal_fixed_gamma_mcar is used to fit 2PL LSIRM with gamma fixed to 1 for continuous variable in incomplete data assumed to be missing completely at random.

lsirm2pl_normal_fixed_gamma_mcar factorizes item response matrix into column-wise item effect, row-wise respondent effect and further embeds interaction effect in a latent space, while ignoring the missing element under the assumption of missing completely at random. Unlike 1PL model, 2PL model assumes the item effect can vary according to respondent, allowing additional parameter multiplied with respondent effect. The resulting latent space provides an interaction map that represents interactions between respondents and items.

Usage

```
lsirm2pl_normal_fixed_gamma_mcar(
  data,
  ndim = 2,
  niter = 15000,
  nburn = 2500,
  nthin = 5,
  nprint = 500,
  jump\_beta = 0.4,
  jump\_theta = 1,
  jump_alpha = 1,
  jump_z = 0.5,
  jump_w = 0.5,
  pr_mean_beta = 0,
  pr_sd_beta = 1,
  pr_mean_theta = 0,
 pr_sd_theta = 1,
 pr_mean_alpha = 0.5,
 pr_sd_alpha = 1,
 pr_a_theta = 0.001,
 pr_b_t = 0.001,
 pr_a_{eps} = 0.001,
  pr_b_{eps} = 0.001,
 missing.val = 99,
  verbose = FALSE,
  fix_{theta_sd} = FALSE,
  fix_alpha_1 = TRUE
)
```

| data | Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item. |
|------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| ndim | Integer; the dimension of the latent space. Default is 2. |
| niter | Integer; the total number of MCMC iterations to run. Default is 15000. |
| nburn | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500. |
| nthin | Integer; the number of MCMC iterations to thin. Default is 5. |
| nprint | Integer; the interval at which MCMC samples are displayed during execution. Default is 500. |
| jump_beta | Numeric; the jumping rule for the beta proposal density. Default is 0.4. |
| jump_theta | Numeric; the jumping rule for the theta proposal density. Default is 1.0. |
| jump_alpha | Numeric; the jumping rule for the alpha proposal density. Default is 1.0. |
| jump_z | Numeric; the jumping rule for the z proposal density. Default is 0.5. |

| jump_w | Numeric; the jumping rule for the w proposal density. Default is 0.5. |
|---------------|-----------------------------------------------------------------------------------------------------------|
| pr_mean_beta | Numeric; the mean of the normal prior for beta. Default is 0. |
| pr_sd_beta | Numeric; the standard deviation of the normal prior for beta. Default is 1.0. |
| pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0. |
| pr_sd_theta | Numeric; the standard deviation of the normal prior for theta. Default is 1.0. |
| pr_mean_alpha | Numeric; the mean of the log normal prior for alpha. Default is 0.5. |
| pr_sd_alpha | Numeric; the standard deviation of the log normal prior for alpha. Default is 1.0. |
| pr_a_theta | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001 . |
| pr_b_theta | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is $0.001.$ |
| pr_a_eps | Numeric; the shape parameter of inverse gamma prior for variance of data likelihood. Default is 0.001 . |
| pr_b_eps | Numeric; the scale parameter of inverse gamma prior for variance of data likelihood. Default is 0.001 . |
| missing.val | Numeric; a number to replace missing values. Default is 99. |
| verbose | Logical; If TRUE, MCMC samples are printed for each nprint. Default is FALSE. |
| fix_theta_sd | Logical; If TRUE, the standard deviation of the theta parameter is fixed. Default is FALSE. |
| fix_alpha_1 | Logical; If TRUE, the first element of the alpha parameter is fixed to 1. Default is TRUE. |

Details

lsirm2pl_normal_fixed_gamma_mcar models the continuous value of response by respondent j to item i with item effect β_i , respondent effect θ_j and the distance between latent position w_i of item i and latent position z_j of respondent j in the shared metric space. For 2pl model, the the item effect is assumed to have additional discrimination parameter α_i multiplied by θ_j :

$$Y_{j,i} = \theta_j + \beta_i - \gamma ||z_j - w_i|| + e_{j,i}$$

where the error $e_{j,i} \sim N(0, \sigma^2)$ Under the assumption of missing completely at random, the model ignores the missing element in doing inference. For the details of missing completely at random assumption and data augmentation, see References.

Value

lsirm2pl_normal_fixed_gamma_mcar returns an object of list containing the following components:

data Data frame or matrix containing the variables in the model.

missing.val A number to replace missing values.

bic Numeric value with the corresponding BIC.

mcmc_inf Details about the number of MCMC iterations, burn-in periods, and thinning

intervals.

map_inf The log maximum a posteriori (MAP) value and the iteration number at which

this MAP value occurs.

beta_estimate Posterior estimates of the beta parameter. theta_estimate Posterior estimates of the theta parameter.

sigma_theta_estimate

Posterior estimates of the standard deviation of theta.

z_estimate
 w_estimate
 beta
 Posterior estimates of the w parameter.
 Posterior samples of the beta parameter.
 theta
 Posterior samples of the theta parameter.

theta_sd Posterior samples of the standard deviation of theta.

z Posterior samples of the z parameter, represented as a 3-dimensional matrix

where the last axis denotes the dimension of the latent space.

w Posterior samples of the w parameter, represented as a 3-dimensional matrix

where the last axis denotes the dimension of the latent space.

z_rawPosterior samples of the z parameter without procrustes matching.w_rawPosterior samples of the w parameter without procrustes matching.

accept_beta Acceptance ratio for the beta parameter.

accept_theta Acceptance ratio for the theta parameter.

accept_z Acceptance ratio for the z parameter.

accept_w Acceptance ratio for the w parameter.

sigma_estimate Posterior estimates of the standard deviation.

sigma Posterior samples of the standard deviation.
alpha_estimate Posterior estimates of the alpha parameter.
alpha Posterior estimates of the alpha parameter.
accept_alpha Acceptance ratio for the alpha parameter.

Examples

lsirm2pl_normal_mar

2PL LSIRM with normal likelihood and missing at random data.

Description

Isirm2pl_normal_mar is used to fit 2PL LSIRM for continuous variable in incomplete data assumed to be missing at random. Isirm2pl_normal_mar factorizes item response matrix into column-wise item effect, row-wise respondent effect and further embeds interaction effect in a latent space, while considering the missing element under the assumption of missing at random. Unlike 1PL model, 2PL model assumes the item effect can vary according to respondent, allowing additional parameter multiplied with respondent effect. The resulting latent space provides an interaction map that represents interactions between respondents and items.

Usage

```
lsirm2pl_normal_mar(
  data,
  ndim = 2,
  niter = 15000,
  nburn = 2500,
  nthin = 5,
  nprint = 500,
  jump\_beta = 0.4,
  jump\_theta = 1,
  jump_alpha = 1,
  jump_gamma = 1,
  jump_z = 0.5,
  jump_w = 0.5,
  pr_mean_beta = 0,
  pr_sd_beta = 1,
  pr_mean_theta = 0,
  pr_sd_theta = 1,
  pr_mean_gamma = 0.5,
  pr_sd_gamma = 1,
  pr_mean_alpha = 0.5,
  pr_sd_alpha = 1,
  pr_a_theta = 0.001,
  pr_b_t = 0.001,
  pr_a_{eps} = 0.001,
  pr_b_{eps} = 0.001,
 missing.val = 99,
  verbose = FALSE,
  fix_{theta_sd} = FALSE,
  fix_alpha_1 = TRUE
)
```

| • | 9 | |
|---|---------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| | data | Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item. |
| | ndim | Integer; the dimension of the latent space. Default is 2. |
| | niter | Integer; the total number of MCMC iterations to run. Default is 15000. |
| | nburn | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500. |
| | nthin | Integer; the number of MCMC iterations to thin. Default is 5. |
| | nprint | Integer; the interval at which MCMC samples are displayed during execution. Default is 500. |
| | jump_beta | Numeric; the jumping rule for the beta proposal density. Default is 0.4. |
| | jump_theta | Numeric; the jumping rule for the theta proposal density. Default is 1.0. |
| | jump_alpha | Numeric; the jumping rule for the alpha proposal density. Default is 1.0. |
| | jump_gamma | Numeric; the jumping rule for the gamma proposal density. Default is 0.025 |
| | jump_z | Numeric; the jumping rule for the z proposal density. Default is 0.5. |
| | jump_w | Numeric; the jumping rule for the w proposal density. Default is 0.5. |
| | pr_mean_beta | Numeric; the mean of the normal prior for beta. Default is 0. |
| | pr_sd_beta | Numeric; the standard deviation of the normal prior for beta. Default is 1.0. |
| | pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0. |
| | pr_sd_theta | Numeric; the standard deviation of the normal prior for theta. Default is 1.0. |
| | pr_mean_gamma | Numeric; mean of log normal prior for gamma. Default is 0.5. |
| | pr_sd_gamma | Numeric; standard deviation of log normal prior for gamma. Default is 1.0. |
| | pr_mean_alpha | Numeric; the mean of the log normal prior for alpha. Default is 0.5. |
| | pr_sd_alpha | Numeric; the standard deviation of the log normal prior for alpha. Default is 1.0. |
| | pr_a_theta | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001 . |
| | pr_b_theta | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001 . |
| | pr_a_eps | Numeric; the shape parameter of inverse gamma prior for variance of data likelihood. Default is 0.001 . |
| | pr_b_eps | Numeric; the scale parameter of inverse gamma prior for variance of data likelihood. Default is 0.001. |
| | missing.val | Numeric; a number to replace missing values. Default is 99. |
| | verbose | Logical; If TRUE, MCMC samples are printed for each nprint. Default is FALSE. |
| | fix_theta_sd | Logical; If TRUE, the standard deviation of the theta parameter is fixed. Default is FALSE. |
| | fix_alpha_1 | Logical; If TRUE, the first element of the alpha parameter is fixed to 1. Default is TRUE. |
| | | |

Details

lsirm2pl_normal_mar models the continuous value of response by respondent j to item i with item effect β_i , respondent effect θ_j and the distance between latent position w_i of item i and latent position z_j of respondent j in the shared metric space, with γ represents the weight of the distance term. For 2pl model, the the item effect is assumed to have additional discrimination parameter α_i multiplied by θ_i :

$$Y_{j,i} = \theta_j + \beta_i - \gamma ||z_j - w_i|| + e_{j,i}$$

where the error $e_{j,i} \sim N(0, \sigma^2)$ Under the assumption of missing at random, the model takes the missing element into consideration in the sampling procedure. For the details of missing at random assumption and data augmentation, see References.

Value

lsirm2pl_normal_mar returns an object of list containing the following components:

data Data frame or matrix containing the variables in the model.

missing.val A number to replace missing values.

bic Numeric value with the corresponding BIC.

mcmc_inf Details about the number of MCMC iterations, burn-in periods, and thinning

intervals.

map_inf The log maximum a posteriori (MAP) value and the iteration number at which

this MAP value occurs.

beta_estimate Posterior estimates of the beta parameter.

theta_estimate Posterior estimates of the theta parameter.

sigma_theta_estimate

Posterior estimates of the standard deviation of theta.

gamma_estimate posterior estimates of gamma parameter.

z_estimate Posterior estimates of the z parameter.

w_estimate Posterior estimates of the w parameter.

imp_estimate Probability of imputating a missing value with 1.

beta Posterior samples of the beta parameter.
theta Posterior samples of the theta parameter.
gamma Posterior samples of the gamma parameter.

theta_sd Posterior samples of the standard deviation of theta.

z Posterior samples of the z parameter, represented as a 3-dimensional matrix

where the last axis denotes the dimension of the latent space.

w Posterior samples of the w parameter, represented as a 3-dimensional matrix

where the last axis denotes the dimension of the latent space.

z_raw Posterior samples of the z parameter without procrustes matching.
w_raw Posterior samples of the w parameter without procrustes matching.

imp Imputation for missing Values using posterior samples.

Acceptance ratio for the theta parameter. accept_theta Acceptance ratio for the z parameter. accept_z Acceptance ratio for the w parameter. accept_w Acceptance ratio for the gamma parameter. accept_gamma sigma_estimate Posterior estimates of the standard deviation. Posterior samples of the standard deviation. sigma alpha_estimate Posterior estimates of the alpha parameter. alpha Posterior estimates of the alpha parameter. Acceptance ratio for the alpha parameter. accept_alpha

References

Little, R. J., & Rubin, D. B. (2019). Statistical analysis with missing data (Vol. 793). John Wiley & Sons.

Examples

lsirm2pl_normal_mar_ss

2pl LSIRM with normal likelihood and model selection approach for missing at random data.

Description

Isirm2pl_normal_mar_ss is used to fit 2pl LSIRM with model selection approach based on spike-and-slab priors for continuous variable in incomplete data assumed to be missing at random. Isirm2pl_normal_mar_ss factorizes item response matrix into column-wise item effect, row-wise respondent effect and further embeds interaction effect in a latent space, while considering the missing element under the assumption of missing at random. Unlike 1pl model, 2pl model assumes the item effect can vary according to respondent, allowing additional parameter multiplied with respondent effect. The resulting latent space provides an interaction map that represents interactions between respondents and items.

Usage

```
lsirm2pl_normal_mar_ss(
  data,
  ndim = 2,
  niter = 15000,
  nburn = 2500,
  nthin = 5,
  nprint = 500,
  jump\_beta = 0.4,
  jump\_theta = 1,
  jump_alpha = 1,
  jump_gamma = 1,
  jump_z = 0.5,
  jump_w = 0.5,
  pr_mean_beta = 0,
  pr_sd_beta = 1,
  pr_mean_theta = 0,
  pr_sd_theta = 1,
  pr_spike_mean = -3,
  pr_spike_sd = 1,
  pr_slab_mean = 0.5,
  pr_slab_sd = 1,
  pr_mean_alpha = 0.5,
  pr_sd_alpha = 1,
  pr_a_{eps} = 0.001,
  pr_b_{eps} = 0.001,
  pr_a_theta = 0.001,
 pr_b_t = 0.001,
  pr_xi_a = 0.001,
  pr_xi_b = 0.001,
  missing.val = 99,
  verbose = FALSE,
  fix_theta_sd = FALSE,
  fix_alpha_1 = TRUE
)
```

| data | Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item. |
|-------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| ndim | Integer; the dimension of the latent space. Default is 2. |
| niter | Integer; the total number of MCMC iterations to run. Default is 15000. |
| nburn | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500. |
| nthin | Integer; the number of MCMC iterations to thin. Default is 5. |

| nprint | Integer; the interval at which MCMC samples are displayed during execution. Default is 500. |
|---------------|-----------------------------------------------------------------------------------------------------------|
| jump_beta | Numeric; the jumping rule for the beta proposal density. Default is 0.4. |
| jump_theta | Numeric; the jumping rule for the theta proposal density. Default is 1.0. |
| jump_alpha | Numeric; the jumping rule for the alpha proposal density. Default is 1.0. |
| jump_gamma | Numeric; the jumping rule for the theta proposal density. Default is 1.0. |
| jump_z | Numeric; the jumping rule for the z proposal density. Default is 0.5. |
| jump_w | Numeric; the jumping rule for the w proposal density. Default is 0.5. |
| pr_mean_beta | Numeric; the mean of the normal prior for beta. Default is 0. |
| pr_sd_beta | Numeric; the standard deviation of the normal prior for beta. Default is 1.0. |
| pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0. |
| pr_sd_theta | Numeric; the standard deviation of the normal prior for theta. Default is 1.0. |
| pr_spike_mean | Numeric; the mean of spike prior for log gamma. Default is -3. |
| pr_spike_sd | Numeric; the standard deviation of spike prior for log gamma. Default is 1. |
| pr_slab_mean | Numeric; the mean of spike prior for log gamma. Default is 0.5. |
| pr_slab_sd | Numeric; the standard deviation of spike prior for log gamma. Default is is 1. |
| pr_mean_alpha | Numeric; the mean of the log normal prior for alpha. Default is 0.5. |
| pr_sd_alpha | Numeric; the standard deviation of the log normal prior for alpha. Default is 1.0. |
| pr_a_eps | Numeric; the shape parameter of inverse gamma prior for variance of data likelihood. Default is 0.001 . |
| pr_b_eps | Numeric; the scale parameter of inverse gamma prior for variance of data likelihood Default is 0.001. |
| pr_a_theta | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001. |
| pr_b_theta | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001 . |
| pr_xi_a | Numeric; the first shape parameter of beta prior for latent variable xi. Default is 1. |
| pr_xi_b | Numeric; the second shape parameter of beta prior for latent variable xi. Default is 1. |
| missing.val | Numeric; a number to replace missing values. Default is 99. |
| verbose | Logical; If TRUE, MCMC samples are printed for each nprint. Default is FALSE. |
| fix_theta_sd | Logical; If TRUE, the standard deviation of the theta parameter is fixed. Default is FALSE. |
| fix_alpha_1 | Logical; If TRUE, the first element of the alpha parameter is fixed to 1. Default is TRUE. |

Details

lsirm2pl_normal_mar_ss models the continuous value of response by respondent j to item i with item effect β_i , respondent effect θ_j and the distance between latent position w_i of item i and latent position z_j of respondent j in the shared metric space, with γ represents the weight of the distance term. For 2pl model, the the item effect is assumed to have additional discrimination parameter α_i multiplied by θ_i :

$$Y_{j,i} = \theta_j + \beta_i - \gamma ||z_j - w_i|| + e_{j,i}$$

where the error $e_{j,i} \sim N(0,\sigma^2)$ Under the assumption of missing at random, the model takes the missing element into consideration in the sampling procedure. For the details of missing at random assumption and data augmentation, see References. lsirm2pl_normal_mcar_ss model include model selection approach based on spike-and-slab priors for log gamma. For detail of spike-and-slab priors, see References.

Value

lsirm2pl_normal_mar_ss returns an object of list containing the following components:

data Data frame or matrix containing the variables in the model.

missing.val A number to replace missing values.

bic Numeric value with the corresponding BIC.

mcmc_inf Details about the number of MCMC iterations, burn-in periods, and thinning

intervals.

map_inf The log maximum a posteriori (MAP) value and the iteration number at which

this MAP value occurs.

beta_estimate Posterior estimates of the beta parameter.
theta_estimate Posterior estimates of the theta parameter.

sigma_theta_estimate

Posterior estimates of the standard deviation of theta.

gamma_estimate posterior estimates of gamma parameter.

z_estimate Posterior estimates of the z parameter.

w_estimate Posterior estimates of the w parameter.

z_rawPosterior samples of the z parameter without procrustes matching.w_rawPosterior samples of the w parameter without procrustes matching.

beta Posterior samples of the beta parameter.
theta Posterior samples of the theta parameter.
gamma Posterior samples of the gamma parameter.

theta_sd Posterior samples of the standard deviation of theta.

z Posterior samples of the z parameter, represented as a 3-dimensional matrix

where the last axis denotes the dimension of the latent space.

w Posterior samples of the w parameter, represented as a 3-dimensional matrix

where the last axis denotes the dimension of the latent space.

pi Posterior samples of phi which is indicator of spike and slab prior. If phi is 1,

log gamma follows the slab prior, otherwise follows the spike prior.

| imp | Imputation for missing Values using posterior samples. |
|-------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| accept_beta | Acceptance ratio for the beta parameter. |
| accept_theta | Acceptance ratio for the theta parameter. |
| accept_z | Acceptance ratio for the z parameter. |
| accept_w | Acceptance ratio for the w parameter. |
| accept_gamma | Acceptance ratio for the gamma parameter. |
| pi_estimate | Posterior estimation of phi. inclusion probability of gamma. if estimation of phi is less than 0.5 , choose Rasch model with gamma = 0 , otherwise latent space model with gamma > 0 . |
| <pre>imp_estimate</pre> | Probability of imputating a missing value with 1. |
| sigma_estimate | Posterior estimates of the standard deviation. |
| sigma | Posterior samples of the standard deviation. |
| alpha_estimate | Posterior estimates of the alpha parameter. |
| alpha | Posterior estimates of the alpha parameter. |
| accept_alpha | Acceptance ratio for the alpha parameter. |

References

Little, R. J., & Rubin, D. B. (2019). Statistical analysis with missing data (Vol. 793). John Wiley & Sons. Ishwaran, H., & Rao, J. S. (2005). Spike and slab variable selection: Frequentist and Bayesian strategies. The Annals of Statistics, 33(2), 730-773.

Examples

Description

lsirm2pl_normal_mcar is used to fit 2PL LSIRM for continuous variable in incomplete data assumed to be missing completely at random. lsirm2pl_normal_mcar factorizes item response matrix into column-wise item effect, row-wise respondent effect and further embeds interaction effect in a latent space, while ignoring the missing element under the assumption of missing completely at random. Unlike 1PL model, 2PL model assumes the item effect can vary according to respondent, allowing additional parameter multiplied with respondent effect. The resulting latent space provides an interaction map that represents interactions between respondents and items.

Usage

```
lsirm2pl_normal_mcar(
  data,
  ndim = 2,
  niter = 15000,
  nburn = 2500,
  nthin = 5,
  nprint = 500,
  jump_beta = 0.4,
  jump\_theta = 1,
  jump_alpha = 1,
  jump_gamma = 1,
  jump_z = 0.5,
  jump_w = 0.5,
  pr_mean_beta = 0,
  pr_sd_beta = 1,
 pr_mean_theta = 0,
 pr_sd_theta = 1,
  pr_mean_gamma = 0.5,
  pr_sd_gamma = 1,
  pr_mean_alpha = 0.5,
  pr_sd_alpha = 1,
  pr_a_theta = 0.001,
  pr_b_t = 0.001,
 pr_a_{eps} = 0.001,
  pr_b_{eps} = 0.001,
 missing.val = 99,
  verbose = FALSE,
  fix_theta_sd = FALSE,
  fix_alpha_1 = TRUE
)
```

| _ | |
|---------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| data | Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item. |
| ndim | Integer; the dimension of the latent space. Default is 2. |
| niter | Integer; the total number of MCMC iterations to run. Default is 15000. |
| nburn | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500. |
| nthin | Integer; the number of MCMC iterations to thin. Default is 5. |
| nprint | Integer; the interval at which MCMC samples are displayed during execution. Default is 500. |
| jump_beta | Numeric; the jumping rule for the beta proposal density. Default is 0.4. |
| jump_theta | Numeric; the jumping rule for the theta proposal density. Default is 1.0. |
| jump_alpha | Numeric; the jumping rule for the alpha proposal density. Default is 1.0. |
| jump_gamma | Numeric; the jumping rule for the gamma proposal density. Default is 0.025 |
| jump_z | Numeric; the jumping rule for the z proposal density. Default is 0.5. |
| jump_w | Numeric; the jumping rule for the w proposal density. Default is 0.5. |
| pr_mean_beta | Numeric; the mean of the normal prior for beta. Default is 0. |
| pr_sd_beta | Numeric; the standard deviation of the normal prior for beta. Default is 1.0. |
| pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0. |
| pr_sd_theta | Numeric; the standard deviation of the normal prior for theta. Default is 1.0. |
| pr_mean_gamma | Numeric; mean of log normal prior for gamma. Default is 0.5. |
| pr_sd_gamma | Numeric; standard deviation of log normal prior for gamma. Default is 1.0. |
| pr_mean_alpha | Numeric; the mean of the log normal prior for alpha. Default is 0.5. |
| pr_sd_alpha | Numeric; the standard deviation of the log normal prior for alpha. Default is 1.0. |
| pr_a_theta | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001. |
| pr_b_theta | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001 . |
| pr_a_eps | Numeric; the shape parameter of inverse gamma prior for variance of data likelihood. Default is 0.001 . |
| pr_b_eps | Numeric; the scale parameter of inverse gamma prior for variance of data likelihood. Default is 0.001 . |
| missing.val | Numeric; a number to replace missing values. Default is 99. |
| verbose | Logical; If TRUE, MCMC samples are printed for each nprint. Default is FALSE. |
| fix_theta_sd | Logical; If TRUE, the standard deviation of the theta parameter is fixed. Default is FALSE. |
| fix_alpha_1 | Logical; If TRUE, the first element of the alpha parameter is fixed to 1. Default is TRUE. |
| | |

Details

lsirm2pl_normal_mcar models the continuous value of response by respondent j to item i with item effect β_i , respondent effect θ_j and the distance between latent position w_i of item i and latent position z_j of respondent j in the shared metric space, with γ represents the weight of the distance term. For 2pl model, the the item effect is assumed to have additional discrimination parameter α_i multiplied by θ_i :

$$Y_{j,i} = \theta_j + \beta_i - \gamma ||z_j - w_i|| + e_{j,i}$$

where the error $e_{j,i} \sim N(0, \sigma^2)$ Under the assumption of missing completely at random, the model ignores the missing element in doing inference. For the details of missing completely at random assumption and data augmentation, see References.

Value

lsirm2pl_normal_mcar returns an object of list containing the following components:

data A data frame or matrix containing the variables used in the model.

missing.val A number to replace missing values.

bic Numeric value with the corresponding BIC.

mcmc_inf Details about the number of MCMC iterations, burn-in periods, and thinning

intervals.

map_inf The log maximum a posteriori (MAP) value and the iteration number at which

this MAP value occurs.

beta_estimate Posterior estimates of the beta parameter.

theta_estimate Posterior estimates of the theta parameter.

sigma_theta_estimate

Posterior estimates of the standard deviation of theta.

gamma_estimate Posterior estimates of gamma parameter.

z_estimate Posterior estimates of the z parameter.

w_estimate Posterior estimates of the w parameter.

beta Posterior samples of the beta parameter.

theta Posterior samples of the theta parameter.

theta_sd Posterior samples of the standard deviation of theta.

gamma Posterior samples of the gamma parameter.

z Posterior samples of the z parameter, represented as a 3-dimensional matrix

where the last axis denotes the dimension of the latent space.

w Posterior samples of the w parameter, represented as a 3-dimensional matrix

where the last axis denotes the dimension of the latent space.

z_raw Posterior samples of the z parameter without procrustes matching.
w_raw Posterior samples of the w parameter without procrustes matching.

accept_beta Acceptance ratio for the beta parameter.

accept_theta Acceptance ratio for the theta parameter.

accept_z Acceptance ratio for the z parameter.

accept_w Acceptance ratio for the w parameter.
accept_gamma Acceptance ratio for the gamma parameter.
sigma_estimate Posterior estimates of the standard deviation.
sigma Posterior samples of the standard deviation.
alpha_estimate Posterior estimates of the alpha parameter.
alpha Posterior estimates of the alpha parameter.
accept_alpha Acceptance ratio for the alpha parameter.

References

Little, R. J., & Rubin, D. B. (2019). Statistical analysis with missing data (Vol. 793). John Wiley & Sons.

Examples

lsirm2pl_normal_mcar_ss

2PL LSIRM with normal likelihood and model selection approach for missing completely at random data.

Description

lsirm2pl_normal_mcar_ss is used to fit 2PL LSIRM with model selection approach based on spike-and-slab priors for continuous variable in incomplete data assumed to be missing completely at random. lsirm2pl_normal_mcar_ss factorizes item response matrix into column-wise item effect, row-wise respondent effect and further embeds interaction effect in a latent space, while ignoring the missing element under the assumption of missing completely at random. Unlike 1PL model, 2PL model assumes the item effect can vary according to respondent, allowing additional parameter multiplied with respondent effect. The resulting latent space provides an interaction map that represents interactions between respondents and items.

Usage

```
lsirm2pl_normal_mcar_ss(
  data,
  ndim = 2,
  niter = 15000,
  nburn = 2500,
  nthin = 5,
  nprint = 500,
  jump\_beta = 0.4,
  jump\_theta = 1,
  jump_alpha = 1,
  jump_gamma = 1,
  jump_z = 0.5,
  jump_w = 0.5,
  pr_mean_beta = 0,
  pr_sd_beta = 1,
  pr_mean_theta = 0,
  pr_sd_theta = 1,
  pr_spike_mean = -3,
  pr_spike_sd = 1,
 pr_slab_mean = 0.5,
  pr_slab_sd = 1,
  pr_mean_alpha = 0.5,
 pr\_sd\_alpha = 1,
  pr_a_{eps} = 0.001,
  pr_b_{eps} = 0.001,
 pr_a_theta = 0.001,
 pr_b_t = 0.001,
  pr_xi_a = 0.001,
  pr_xi_b = 0.001,
 missing.val = 99,
  verbose = FALSE,
  fix_theta_sd = FALSE,
  fix_alpha_1 = TRUE
)
```

| data | Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item. |
|-------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| ndim | Integer; the dimension of the latent space. Default is 2. |
| niter | Integer; the total number of MCMC iterations to run. Default is 15000. |
| nburn | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500. |
| nthin | Integer; the number of MCMC iterations to thin. Default is 5. |

| nprint | Integer; the interval at which MCMC samples are displayed during execution. Default is 500. |
|---------------|--------------------------------------------------------------------------------------------------------|
| jump_beta | Numeric; the jumping rule for the beta proposal density. Default is 0.4. |
| jump_theta | Numeric; the jumping rule for the theta proposal density. Default is 1.0. |
| jump_alpha | Numeric; the jumping rule for the alpha proposal density. Default is 1.0. |
| jump_gamma | Numeric; the jumping rule for the theta proposal density. Default is 1.0. |
| jump_z | Numeric; the jumping rule for the z proposal density. Default is 0.5. |
| jump_w | Numeric; the jumping rule for the w proposal density. Default is 0.5. |
| pr_mean_beta | Numeric; the mean of the normal prior for beta. Default is 0. |
| pr_sd_beta | Numeric; the standard deviation of the normal prior for beta. Default is 1.0. |
| pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0. |
| pr_sd_theta | Numeric; the standard deviation of the normal prior for theta. Default is 1.0. |
| pr_spike_mean | Numeric; the mean of spike prior for log gamma. Default is -3. |
| pr_spike_sd | Numeric; the standard deviation of spike prior for log gamma. Default is 1. |
| pr_slab_mean | Numeric; the mean of spike prior for log gamma. Default is 0.5. |
| pr_slab_sd | Numeric; the standard deviation of spike prior for log gamma. Default is is 1. |
| pr_mean_alpha | Numeric; the mean of the log normal prior for alpha. Default is 0.5. |
| pr_sd_alpha | Numeric; the standard deviation of the log normal prior for alpha. Default is 1.0. |
| pr_a_eps | Numeric; the shape parameter of inverse gamma prior for variance of data likelihood. Default is 0.001. |
| pr_b_eps | Numeric; the scale parameter of inverse gamma prior for variance of data likelihood. Default is 0.001. |
| pr_a_theta | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001. |
| pr_b_theta | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001. |
| pr_xi_a | Numeric; the first shape parameter of beta prior for latent variable xi. Default is 1. |
| pr_xi_b | Numeric; the second shape parameter of beta prior for latent variable xi. Default is 1. |
| missing.val | Numeric; a number to replace missing values. Default is 99. |
| verbose | Logical; If TRUE, MCMC samples are printed for each nprint. Default is FALSE. |
| fix_theta_sd | Logical; If TRUE, the standard deviation of the theta parameter is fixed. Default is FALSE. |
| fix_alpha_1 | Logical; If TRUE, the first element of the alpha parameter is fixed to 1. Default is TRUE. |

Details

lsirm2pl_normal_mcar_ss models the continuous value of response by respondent j to item i with item effect β_i , respondent effect θ_j and the distance between latent position w_i of item i and latent position z_j of respondent j in the shared metric space, with γ represents the weight of the distance term. For 2pl model, the the item effect is assumed to have additional discrimination parameter α_i multiplied by θ_i :

$$Y_{j,i} = \theta_j + \beta_i - \gamma ||z_j - w_i|| + e_{j,i}$$

where the error $e_{j,i} \sim N(0,\sigma^2)$ Under the assumption of missing completely at random, the model ignores the missing element in doing inference. For the details of missing completely at random assumption and data augmentation, see References. lsirm2pl_normal_mcar_ss model include model selection approach based on spike-and-slab priors for log gamma. For detail of spike-and-slab priors, see References.

Value

lsirm2pl_normal_mcar_ss returns an object of list containing the following components:

data Data frame or matrix containing the variables in the model.

missing.val A number to replace missing values.

bic Numeric value with the corresponding BIC.

mcmc_inf Details about the number of MCMC iterations, burn-in periods, and thinning

intervals.

map_inf The log maximum a posteriori (MAP) value and the iteration number at which

this MAP value occurs.

beta_estimate Posterior estimates of the beta parameter.
theta_estimate Posterior estimates of the theta parameter.

sigma_theta_estimate

Posterior estimates of the standard deviation of theta.

gamma_estimate posterior estimates of gamma parameter.

z_estimate Posterior estimates of the z parameter.

w_estimate Posterior estimates of the w parameter.

beta Posterior samples of the beta parameter.

theta Posterior samples of the theta parameter.

gamma Posterior samples of the gamma parameter.

theta_sd Posterior samples of the standard deviation of theta.

z Posterior samples of the z parameter, represented as a 3-dimensional matrix

where the last axis denotes the dimension of the latent space.

w Posterior samples of the w parameter, represented as a 3-dimensional matrix

where the last axis denotes the dimension of the latent space.

z_raw Posterior samples of the z parameter without procrustes matching.
w_raw Posterior samples of the w parameter without procrustes matching.

pi Posterior samples of phi which is indicator of spike and slab prior. If phi is 1,

log gamma follows the slab prior, otherwise follows the spike prior.

lsirm2pl_normal_o

accept_beta Acceptance ratio for the beta parameter. accept_theta Acceptance ratio for the theta parameter. Acceptance ratio for the z parameter. accept_z accept_w Acceptance ratio for the w parameter. accept_gamma Acceptance ratio for the gamma parameter. sigma_estimate Posterior estimates of the standard deviation. Posterior samples of the standard deviation. sigma alpha_estimate Posterior estimates of the alpha parameter. alpha Posterior estimates of the alpha parameter. accept_alpha Acceptance ratio for the alpha parameter.

References

Little, R. J., & Rubin, D. B. (2019). Statistical analysis with missing data (Vol. 793). John Wiley & Sons. Ishwaran, H., & Rao, J. S. (2005). Spike and slab variable selection: Frequentist and Bayesian strategies. The Annals of Statistics, 33(2), 730-773.

Examples

lsirm2pl_normal_o

2PL LSIRM with normal likelihood

Description

lsirm2pl_normal_o is used to fit 2PL LSIRM for continuous variable. lsirm2pl_normal_o factorizes item response matrix into column-wise item effect, row-wise respondent effect and further embeds interaction effect in a latent space. Unlike 1PL model, 2PL model assumes the item effect can vary according to respondent, allowing additional parameter multiplied with respondent effect. The resulting latent space provides an interaction map that represents interactions between respondents and items.

lsirm2pl_normal_o 123

Usage

```
lsirm2pl_normal_o(
  data,
  ndim = 2,
 niter = 15000,
  nburn = 2500,
  nthin = 5,
  nprint = 500,
  jump\_beta = 0.4,
  jump\_theta = 1,
  jump_alpha = 1,
  jump_gamma = 0.025,
  jump_z = 0.5,
  jump_w = 0.5,
  pr_mean_beta = 0,
  pr_sd_beta = 1,
  pr_mean_theta = 0,
  pr_sd_theta = 1,
  pr_mean_gamma = 0.5,
  pr_sd_gamma = 1,
  pr_mean_alpha = 0.5,
 pr_sd_alpha = 1,
  pr_a_theta = 0.001,
  pr_b_t = 0.001,
 pr_a_{eps} = 0.001,
 pr_b_{eps} = 0.001,
  verbose = FALSE,
  fix_theta_sd = FALSE,
  fix_alpha_1 = TRUE
)
```

| data | Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item. |
|------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| ndim | Integer; the dimension of the latent space. Default is 2. |
| niter | Integer; the total number of MCMC iterations to run. Default is 15000. |
| nburn | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500. |
| nthin | Integer; the number of MCMC iterations to thin. Default is 5. |
| nprint | Integer; the interval at which MCMC samples are displayed during execution. Default is 500. |
| jump_beta | Numeric; the jumping rule for the beta proposal density. Default is 0.4. |
| jump_theta | Numeric; the jumping rule for the theta proposal density. Default is 1.0. |
| jump_alpha | Numeric; the jumping rule for the alpha proposal density. Default is 1.0. |

lsirm2pl_normal_o

| jump_gamma | Numeric; the jumping rule for the gamma proposal density. Default is 0.025 |
|---------------|-----------------------------------------------------------------------------------------------------------|
| jump_z | Numeric; the jumping rule for the z proposal density. Default is 0.5. |
| jump_w | Numeric; the jumping rule for the w proposal density. Default is 0.5. |
| pr_mean_beta | Numeric; the mean of the normal prior for beta. Default is 0. |
| pr_sd_beta | Numeric; the standard deviation of the normal prior for beta. Default is 1.0. |
| pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0. |
| pr_sd_theta | Numeric; the standard deviation of the normal prior for theta. Default is 1.0. |
| pr_mean_gamma | Numeric; mean of log normal prior for gamma. Default is 0.5. |
| pr_sd_gamma | Numeric; standard deviation of log normal prior for gamma. Default is 1.0. |
| pr_mean_alpha | Numeric; the mean of the log normal prior for alpha. Default is 0.5. |
| pr_sd_alpha | Numeric; the standard deviation of the \log normal prior for alpha. Default is $1.0.$ |
| pr_a_theta | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001 . |
| pr_b_theta | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001 . |
| pr_a_eps | Numeric; the shape parameter of inverse gamma prior for variance of data likelihood. Default is 0.001 . |
| pr_b_eps | Numeric; the scale parameter of inverse gamma prior for variance of data likelihood. Default is 0.001 . |
| verbose | Logical; If TRUE, MCMC samples are printed for each nprint. Default is FALSE. |
| fix_theta_sd | Logical; If TRUE, the standard deviation of the theta parameter is fixed. Default is FALSE. |
| fix_alpha_1 | Logical; If TRUE, the first element of the alpha parameter is fixed to 1. Default is TRUE. |
| | |

Details

lsirm2pl_normal_o models the continuous value of response by respondent j to item i with item effect β_i , respondent effect θ_j and the distance between latent position w_i of item i and latent position z_j of respondent j in the shared metric space, with γ represents the weight of the distance term. For 2pl model, the the item effect is assumed to have additional discrimination parameter α_i multiplied by θ_j :

$$Y_{j,i} = \theta_j + \beta_i - \gamma ||z_j - w_i|| + e_{j,i}$$

where the error $e_{j,i} \sim N(0, \sigma^2)$

Value

lsirm2pl_normal_o returns an object of list containing the following components:

data Data frame or matrix containing the variables used in the model.

bic A numeric value representing the Bayesian Information Criterion (BIC).

Isirm2pl_normal_o

mcmc_inf Details about the number of MCMC iterations, burn-in periods, and thinning

intervals.

map_inf The log maximum a posteriori (MAP) value and the iteration number at which

this MAP value occurs.

beta_estimate Posterior estimates of the beta parameter.
theta_estimate Posterior estimates of the theta parameter.

sigma_theta_estimate

Posterior estimates of the standard deviation of theta.

gamma_estimate Posterior estimates of gamma parameter.

z_estimate Posterior estimates of the z parameter.

w_estimate Posterior estimates of the w parameter.

beta Posterior samples of the beta parameter.

theta Posterior samples of the theta parameter.

theta_sd Posterior samples of the standard deviation of theta.

gamma Posterior samples of the gamma parameter.

z Posterior samples of the z parameter, represented as a 3-dimensional matrix

where the last axis denotes the dimension of the latent space.

w Posterior samples of the w parameter, represented as a 3-dimensional matrix

where the last axis denotes the dimension of the latent space.

z_raw Posterior samples of the z parameter without procrustes matching.w_raw Posterior samples of the w parameter without procrustes matching.

Acceptance ratio for the beta parameter. accept_beta accept_theta Acceptance ratio for the theta parameter. Acceptance ratio for the z parameter. accept_z accept_w Acceptance ratio for the w parameter. Acceptance ratio for the gamma parameter. accept_gamma sigma_estimate Posterior estimates of the standard deviation. Posterior samples of the standard deviation. sigma alpha_estimate Posterior estimates of the alpha parameter. alpha Posterior estimates of the alpha parameter. accept_alpha Acceptance ratio for the alpha parameter.

Examples

```
# generate example (continuous) item response matrix
data <- matrix(rnorm(500, mean = 0, sd = 1),ncol=10,nrow=50)
lsirm_result <- lsirm2pl_normal_o(data)

# The code following can achieve the same result.
lsirm_result <- lsirm(data ~ lsirm2pl(spikenslab = FALSE, fixed_gamma = FALSE))</pre>
```

126 lsirm2pl_normal_ss

lsirm2pl_normal_ss

2PL LSIRM with normal likelihood and model selection approach.

Description

lsirm2pl_normal_ss is used to fit 2PL LSIRM for continuous variable with model selection approach. lsirm2pl_normal_ss factorizes item response matrix into column-wise item effect, rowwise respondent effect and further embeds interaction effect in a latent space. Unlike 1PL model, 2PL model assumes the item effect can vary according to respondent, allowing additional parameter multiplied with respondent effect. The resulting latent space provides an interaction map that represents interactions between respondents and items.

Usage

```
lsirm2pl_normal_ss(
  data,
  ndim = 2,
  niter = 15000,
  nburn = 2500,
  nthin = 5,
  nprint = 500,
  jump\_beta = 0.4,
  jump\_theta = 1,
  jump_alpha = 1,
  jump_gamma = 1,
  jump_z = 0.5,
  jump_w = 0.5,
  pr_mean_beta = 0,
  pr_sd_beta = 1,
  pr_mean_theta = 0,
  pr_sd_theta = 1,
  pr_spike_mean = -3,
  pr_spike_sd = 1,
  pr_slab_mean = 0.5,
  pr_slab_sd = 1,
  pr_mean_alpha = 0.5,
  pr_sd_alpha = 1,
  pr_a_{eps} = 0.001,
  pr_b_{eps} = 0.001,
  pr_a_theta = 0.001,
  pr_b_t = 0.001,
  pr_xi_a = 0.001,
  pr_xi_b = 0.001,
  verbose = FALSE,
  fix_{theta_sd} = FALSE,
  fix_alpha_1 = TRUE
)
```

lsirm2pl_normal_ss 127

| 8 | |
|---------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| data | Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item. |
| ndim | Integer; the dimension of the latent space. Default is 2. |
| niter | Integer; the total number of MCMC iterations to run. Default is 15000. |
| nburn | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500. |
| nthin | Integer; the number of MCMC iterations to thin. Default is 5. |
| nprint | Integer; the interval at which MCMC samples are displayed during execution. Default is 500. |
| jump_beta | Numeric; the jumping rule for the beta proposal density. Default is 0.4. |
| jump_theta | Numeric; the jumping rule for the theta proposal density. Default is 1.0. |
| jump_alpha | Numeric; the jumping rule for the alpha proposal density. Default is 1.0. |
| jump_gamma | Numeric; the jumping rule for the theta proposal density. Default is 1.0. |
| jump_z | Numeric; the jumping rule for the z proposal density. Default is 0.5. |
| jump_w | Numeric; the jumping rule for the w proposal density. Default is 0.5. |
| pr_mean_beta | Numeric; the mean of the normal prior for beta. Default is 0. |
| pr_sd_beta | Numeric; the standard deviation of the normal prior for beta. Default is 1.0. |
| pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0. |
| pr_sd_theta | Numeric; the standard deviation of the normal prior for theta. Default is 1.0. |
| pr_spike_mean | Numeric; mean of spike prior for log gamma default value is -3. |
| pr_spike_sd | Numeric; standard deviation of spike prior for log gamma default value is 1. |
| pr_slab_mean | Numeric; mean of spike prior for log gamma default value is 0.5. |
| pr_slab_sd | Numeric; standard deviation of spike prior for log gamma default value is 1. |
| pr_mean_alpha | Numeric; the mean of the log normal prior for alpha. Default is 0.5. |
| pr_sd_alpha | Numeric; the standard deviation of the log normal prior for alpha. Default is 1.0. |
| pr_a_eps | Numeric; shape parameter of inverse gamma prior for variance of data likelihood. Default is 0.001. |
| pr_b_eps | Numeric; scale parameter of inverse gamma prior for variance of data likelihood. Default is 0.001. |
| pr_a_theta | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001. |
| pr_b_theta | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001. |
| pr_xi_a | Numeric; first shape parameter of beta prior for latent variable xi. Default is 1. |
| pr_xi_b | Numeric; second shape parameter of beta prior for latent variable xi. Default is 1. |
| | |

128 lsirm2pl_normal_ss

verbose Logical; If TRUE, MCMC samples are printed for each nprint. Default is

FALSE.

fix_theta_sd Logical; If TRUE, the standard deviation of the theta parameter is fixed. Default

is FALSE.

fix_alpha_1 Logical; If TRUE, the first element of the alpha parameter is fixed to 1. Default

is TRUE.

Details

Isirm2pl_normal_ss models the continuous value of response by respondent j to item i with item effect β_i , respondent effect θ_j and the distance between latent position w_i of item i and latent position z_j of respondent j in the shared metric space, with γ represents the weight of the distance term. For 2pl model, the the item effect is assumed to have additional discrimination parameter α_i multiplied by θ_i :

$$Y_{i,i} = \theta_i + \beta_i - \gamma ||z_i - w_i|| + e_{i,i}$$

where the error $e_{j,i} \sim N(0, \sigma^2)$. lsrm2pl_noraml_ss model include model selection approach based on spike-and-slab priors for log gamma. For detail of spike-and-slab priors, see References.

Value

lsirm2pl_normal_ss returns an object of list containing the following components:

data Data frame or matrix containing the variables in the model.

bic Numeric value with the corresponding BIC.

mcmc_inf number of mcmc iteration, burn-in periods, and thinning intervals.

map_inf value of log maximum a posterior and iteration number which have log maxi-

mum a posterior.

beta_estimate posterior estimation of beta. theta_estimate posterior estimation of theta.

sigma_theta_estimate

posterior estimation of standard deviation of theta.

sigma_estimate posterior estimation of standard deviation.

gamma_estimate posterior estimation of gamma.

z_estimate posterior estimation of z.
w_estimate posterior estimation of w.

pi_estimate posterior estimation of phi. inclusion probability of gamma. if estimation of phi

is less than 0.5, choose Rasch model with gamma = 0, otherwise latent space

model with gamma > 0.

beta posterior samples of beta. theta posterior samples of theta.

theta_sd posterior samples of standard deviation of theta.

sigma posterior samples of standard deviation.

gamma posterior samples of gamma.

| Z | posterior samples of z. The output is 3-dimensional matrix with last axis represent the dimension of latent space. |
|----------------|--------------------------------------------------------------------------------------------------------------------------------------------------------|
| W | posterior samples of w. The output is 3-dimensional matrix with last axis represent the dimension of latent space. |
| z_raw | Posterior samples of the z parameter without procrustes matching. |
| w_raw | Posterior samples of the w parameter without procrustes matching. |
| pi | posterior samples of phi which is indicator of spike and slab prior. If phi is 1, log gamma follows the slab prior, otherwise follows the spike prior. |
| accept_beta | accept ratio of beta. |
| accept_theta | accept ratio of theta. |
| accept_w | accept ratio of w. |
| accept_z | accept ratio of z. |
| accept_gamma | accept ratio of gamma. |
| alpha_estimate | Posterior estimates of the alpha parameter. |
| alpha | Posterior estimates of the alpha parameter. |
| accept_alpha | Acceptance ratio for the alpha parameter. |

References

Ishwaran, H., & Rao, J. S. (2005). Spike and slab variable selection: frequentist and Bayesian strategies. The Annals of Statistics, 33(2), 730-773.

Examples

```
# generate example (continuous) item response matrix
data <- matrix(rnorm(500, mean = 0, sd = 1),ncol=10,nrow=50)

lsirm_result <- lsirm2pl_normal_ss(data)

# The code following can achieve the same result.
lsirm_result <- lsirm(data ~ lsirm2pl(spikenslab = TRUE, fixed_gamma = FALSE))</pre>
```

lsirm2pl_o

2PL LSIRM.

Description

lsirm2pl_o is used to fit 2PL LSIRM. lsirm2pl_o factorizes item response matrix into column-wise item effect, row-wise respondent effect and further embeds interaction effect in a latent space. Unlike 1PL model, 2PL model assumes the item effect can vary according to respondent, allowing additional parameter multiplied with respondent effect. The resulting latent space provides an interaction map that represents interactions between respondents and items.

Usage

```
lsirm2pl_o(
  data,
  ndim = 2,
  niter = 15000,
  nburn = 2500,
  nthin = 5,
  nprint = 500,
  jump\_beta = 0.4,
  jump\_theta = 1,
  jump_alpha = 1,
  jump_gamma = 0.025,
  jump_z = 0.5,
  jump_w = 0.5,
  pr_mean_beta = 0,
  pr_sd_beta = 1,
 pr_mean_theta = 0,
 pr_sd_theta = 1,
  pr_mean_gamma = 0.5,
 pr_sd_gamma = 1,
 pr_mean_alpha = 0.5,
 pr_sd_alpha = 1,
  pr_a_theta = 0.001,
  pr_b_t = 0.001,
  verbose = FALSE,
  fix_{theta_sd} = FALSE,
  fix_alpha_1 = TRUE
)
```

| Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item. |
|-------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| Integer; the dimension of the latent space. Default is 2. |
| Integer; the total number of MCMC iterations to run. Default is 15000. |
| Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500. |
| Integer; the number of MCMC iterations to thin. Default is 5. |
| Integer; the interval at which MCMC samples are displayed during execution. Default is 500. |
| Numeric; the jumping rule for the beta proposal density. Default is 0.4. |
| Numeric; the jumping rule for the theta proposal density. Default is 1.0. |
| Numeric; the jumping rule for the alpha proposal density. Default is 1.0. |
| Numeric; the jumping rule for the gamma proposal density. Default is 0.025. |
| |

| jump_z | Numeric; the jumping rule for the z proposal density. Default is 0.5. |
|---------------|------------------------------------------------------------------------------------------------------|
| jump_w | Numeric; the jumping rule for the w proposal density. Default is 0.5. |
| pr_mean_beta | Numeric; the mean of the normal prior for beta. Default is 0. |
| pr_sd_beta | Numeric; the standard deviation of the normal prior for beta. Default is 1.0. |
| pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0. |
| pr_sd_theta | Numeric; the standard deviation of the normal prior for theta. Default is 1.0. |
| pr_mean_gamma | Numeric; mean of log normal prior for gamma. Default is 0.5. |
| pr_sd_gamma | Numeric; standard deviation of log normal prior for gamma. Default is 1.0. |
| pr_mean_alpha | Numeric; the mean of the log normal prior for alpha. Default is 0.5. |
| pr_sd_alpha | Numeric; the standard deviation of the log normal prior for alpha. Default is 1.0. |
| pr_a_theta | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001. |
| pr_b_theta | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001. |
| verbose | Logical; If TRUE, MCMC samples are printed for each nprint. Default is FALSE. |
| fix_theta_sd | Logical; If TRUE, the standard deviation of the theta parameter is fixed. Default is FALSE. |
| fix_alpha_1 | Logical; If TRUE, the first element of the alpha parameter is fixed to 1. Default is TRUE. |

Details

lsirm2pl_o models the probability of correct response by respondent j to item i with item effect β_i , respondent effect θ_j and the distance between latent position w_i of item i and latent position z_j of respondent j in the shared metric space, with γ represents the weight of the distance term. For 2pl model, the item effect is assumed to have additional discrimination parameter α_i multiplied by θ_j :

$$logit(P(Y_{j,i} = 1 | \theta_j, \alpha_i, \beta_i, \gamma, z_j, w_i)) = \theta_j * \alpha_i + \beta_i - \gamma ||z_j - w_i||$$

Value

lsirm2pl_o returns an object of list containing the following components:

| data | Data frame or matrix containing the variables used in the model. | |
|---------------|---------------------------------------------------------------------------------------------------|--|
| bic | A numeric value representing the Bayesian Information Criterion (BIC). | |
| mcmc_inf | Details about the number of MCMC iterations, burn-in periods, and thinning intervals. | |
| map_inf | The log maximum a posteriori (MAP) value and the iteration number at which this MAP value occurs. | |
| beta_estimate | Posterior estimates of the beta parameter. | |

theta_estimate Posterior estimates of the theta parameter.

sigma_theta_estimate

Posterior estimates of the standard deviation of theta.

gamma_estimate Posterior estimates of gamma parameter.

z_estimate Posterior estimates of the z parameter.

w_estimate Posterior estimates of the w parameter.

beta Posterior samples of the beta parameter.

theta Posterior samples of the theta parameter.

theta_sd Posterior samples of the standard deviation of theta.

gamma Posterior samples of the gamma parameter.

z Posterior samples of the z parameter, represented as a 3-dimensional matrix

where the last axis denotes the dimension of the latent space.

w Posterior samples of the w parameter, represented as a 3-dimensional matrix

where the last axis denotes the dimension of the latent space.

z_raw Posterior samples of the z parameter without procrustes matching.

w_raw Posterior samples of the w parameter without procrustes matching.

accept_beta Acceptance ratio for the beta parameter.

accept_z Acceptance ratio for the z parameter.

accept_w Acceptance ratio for the w parameter.

alpha_estimate Posterior estimates of the alpha parameter.

alpha Posterior estimates of the alpha parameter.

Examples

```
# generate example item response matrix
data <- matrix(rbinom(500, size = 1, prob = 0.5),ncol=10,nrow=50)

lsirm_result <- lsirm2pl_o(data)

# The code following can achieve the same result.
lsirm_result <- lsirm(data ~ lsirm2pl(spikenslab = FALSE, fixed_gamma = FALSE))</pre>
```

lsirm2pl_ss 133

lsirm2pl_ss

2PL LSIRM with model selection approach.

Description

lsirm2pl_ss is used to fit 2PL LSIRM with model selection approach based on spike-and-slab priors. lsirm2pl_ss factorizes item response matrix into column-wise item effect, row-wise respondent effect and further embeds interaction effect in a latent space. Unlike 1PL model, 2PL model assumes the item effect can vary according to respondent, allowing additional parameter multiplied with respondent effect. The resulting latent space provides an interaction map that represents interactions between respondents and items.

Usage

```
lsirm2pl_ss(
  data,
  ndim = 2,
  niter = 15000,
  nburn = 2500,
  nthin = 5,
  nprint = 500,
  jump_beta = 0.4,
  jump\_theta = 1,
  jump_alpha = 1,
  jump_gamma = 1,
  jump_z = 0.5,
  jump_w = 0.5,
  pr_mean_beta = 0,
  pr_sd_beta = 1,
  pr_mean_theta = 0,
  pr_sd_theta = 1,
  pr_spike_mean = -3,
  pr_spike_sd = 1,
  pr_slab_mean = 0.5,
  pr_slab_sd = 1,
  pr_mean_alpha = 0.5,
  pr_sd_alpha = 1,
  pr_a_theta = 0.001,
  pr_b_t = 0.001,
  pr_xi_a = 1,
  pr_xi_b = 1,
  verbose = FALSE,
  fix_{theta_sd} = FALSE,
  fix_alpha_1 = TRUE
)
```

lsirm2pl_ss

| ٩ | 2 | |
|---|---------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| | data | Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item. |
| | ndim | Integer; the dimension of the latent space. Default is 2. |
| | niter | Integer; the total number of MCMC iterations to run. Default is 15000. |
| | nburn | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500. |
| | nthin | Integer; the number of MCMC iterations to thin. Default is 5. |
| | nprint | Integer; the interval at which MCMC samples are displayed during execution. Default is 500. |
| | jump_beta | Numeric; the jumping rule for the beta proposal density. Default is 0.4. |
| | jump_theta | Numeric; the jumping rule for the theta proposal density. Default is 1.0. |
| | jump_alpha | Numeric; the jumping rule for the alpha proposal density. Default is 1.0. |
| | jump_gamma | Numeric; the jumping rule for the theta proposal density. Default is 1.0. |
| | jump_z | Numeric; the jumping rule for the z proposal density. Default is 0.5. |
| | jump_w | Numeric; the jumping rule for the w proposal density. Default is 0.5. |
| | pr_mean_beta | Numeric; the mean of the normal prior for beta. Default is 0. |
| | pr_sd_beta | Numeric; the standard deviation of the normal prior for beta. Default is 1.0. |
| | pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0. |
| | pr_sd_theta | Numeric; the standard deviation of the normal prior for theta. Default is 1.0. |
| | pr_spike_mean | Numeric; the mean of spike prior for log gamma. Default is -3. |
| | pr_spike_sd | Numeric; the standard deviation of spike prior for log gamma. Default is 1. |
| | pr_slab_mean | Numeric; the mean of spike prior for log gamma. Default is 0.5. |
| | pr_slab_sd | Numeric; the standard deviation of spike prior for log gamma. Default is is 1. |
| | pr_mean_alpha | Numeric; the mean of the log normal prior for alpha. Default is 0.5. |
| | pr_sd_alpha | Numeric; the standard deviation of the log normal prior for alpha. Default is 1.0. |
| | pr_a_theta | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001. |
| | pr_b_theta | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001. |
| | pr_xi_a | Numeric; the first shape parameter of beta prior for latent variable xi. Default is 1. |
| | pr_xi_b | Numeric; the second shape parameter of beta prior for latent variable xi. Default is 1. |
| | verbose | Logical; If TRUE, MCMC samples are printed for each nprint. Default is FALSE. |
| | fix_theta_sd | Logical; If TRUE, the standard deviation of the theta parameter is fixed. Default is FALSE. |
| | fix_alpha_1 | Logical; If TRUE, the first element of the alpha parameter is fixed to 1. Default is TRUE. |
| | | |

lsirm2pl_ss 135

Details

lsirm2pl_ss models the probability of correct response by respondent j to item i with item effect β_i , respondent effect θ_j and the distance between latent position w_i of item i and latent position z_j of respondent j in the shared metric space, with γ represents the weight of the distance term. For 2pl model, the item effect is assumed to have additional discrimination parameter α_i multiplied by θ_j :

$$logit(P(Y_{j,i} = 1 | \theta_j, \alpha_i, \beta_i, z_j, w_i)) = \theta_j * \alpha_i + \beta_i - \gamma ||z_j - w_i||$$

lsirm2pl_ss model include model selection approach based on spike-and-slab priors for log gamma. For detail of spike-and-slab priors, see References.

Value

lsirm2pl_ss returns an object of list containing the following components:

data Data frame or matrix containing the variables used in the model.

bic A numeric value representing the Bayesian Information Criterion (BIC).

mcmc_inf Details about the number of MCMC iterations, burn-in periods, and thinning

intervals.

map_inf The log maximum a posteriori (MAP) value and the iteration number at which

this MAP value occurs.

beta_estimate Posterior estimates of the beta parameter.
theta_estimate Posterior estimates of the theta parameter.

sigma_theta_estimate

Posterior estimates of the standard deviation of theta.

gamma_estimate Posterior estimates of gamma parameter.

z_estimate Posterior estimates of the z parameter.

w_estimate Posterior estimates of the w parameter.

beta Posterior samples of the beta parameter.

theta Posterior samples of the theta parameter.

theta_sd Posterior samples of the standard deviation of theta.

gamma Posterior samples of the gamma parameter.

z Posterior samples of the z parameter, represented as a 3-dimensional matrix

where the last axis denotes the dimension of the latent space.

Posterior samples of the w parameter, represented as a 3-dimensional matrix

where the last axis denotes the dimension of the latent space.

z_raw Posterior samples of the z parameter without procrustes matching.
w_raw Posterior samples of the w parameter without procrustes matching.

accept_beta Acceptance ratio for the beta parameter.
accept_theta Acceptance ratio for the theta parameter.
accept_z Acceptance ratio for the z parameter.
accept_w Acceptance ratio for the w parameter.

136 onepl

accept_gamma Acceptance ratio for the gamma parameter.

pi_estimate Posterior estimation of phi. inclusion probability of gamma. if estimation of phi is less than 0.5, choose Rasch model with gamma = 0, otherwise latent space model with gamma > 0.

pi Posterior samples of phi which is indicator of spike and slab prior. If phi is 1, log gamma follows the slab prior, otherwise follows the spike prior.

alpha_estimate Posterior estimates of the alpha parameter.

accept_alpha Acceptance ratio for the alpha parameter.

References

Ishwaran, H., & Rao, J. S. (2005). Spike and slab variable selection: Frequentist and Bayesian strategies. The Annals of Statistics, 33(2), 730-773.

Examples

```
# generate example item response matrix
data <- matrix(rbinom(500, size = 1, prob = 0.5),ncol=10,nrow=50)

lsirm_result <- lsirm2pl_ss(data)

# The code following can achieve the same result.
lsirm_result <- lsirm(data ~ lsirm2pl(spikenslab = TRUE, fixed_gamma = FALSE))</pre>
```

onepl

1PL Rasch model.

Description

onepl is used to fit 1PL Rasch model.

Usage

```
onepl(
   data,
   niter = 15000,
   nburn = 2500,
   nthin = 5,
   nprint = 500,
   jump_beta = 0.4,
   jump_theta = 1,
   pr_mean_beta = 0,
   pr_sd_beta = 1,
   pr_mean_theta = 0,
   pr_a_theta = 0.001,
   pr_b_theta = 0.001
```

onepl 137

Arguments

| data | Matrix; binary item response matrix to be analyzed. Each row is assumed to be respondent and its column values are assumed to be response to the corresponding item. |
|---------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| niter | Numeric; number of iterations to run MCMC sampling. default value is 15000. |
| nburn | Numeric; number of initial, pre-thinning, MCMC iterations to discard. default value is 2500. |
| nthin | Numeric; number of thinning, MCMC iterations to discard. default value is 5. |
| nprint | Numeric; MCMC samples is displayed during execution of MCMC chain for each nprint. default value is 500. |
| jump_beta | Numeric; jumping rule of the proposal density for beta. default value is 0.4. |
| jump_theta | Numeric; jumping rule of the proposal density for theta. default value is 1.0. |
| pr_mean_beta | Numeric; mean of normal prior for beta. default value is 0. |
| pr_sd_beta | Numeric; standard deviation of normal prior for beta. default value is 1.0. |
| pr_mean_theta | Numeric; mean of normal prior for theta. default value is 0. |
| pr_a_theta | Numeric; shape parameter of inverse gamma prior for variance of theta. default value is 0.001 . |
| pr_b_theta | Numeric; scale parameter of inverse gamma prior for variance of theta. default value is 0.001. |

Details

onep1 models the probability of correct response by respondent j to item i with item effect β_i , respondent effect θ_j :

$$logit(P(Y_{j,i} = 1 | \theta_j, \beta_i)) = \theta_j + \beta_i$$

Value

onepl returns an object of list containing the following components:

beta_estimate posterior estimation of beta.

 $theta_estimate \ \ posterior\ estimation\ of\ theta.$

sigma_theta_estimate

posterior estimation of standard deviation of theta.

beta posterior samples of beta. theta posterior samples of theta.

theta_sd posterior samples of standard deviation of theta.

accept_beta accept ratio of beta.
accept_theta accept ratio of theta.

plot plot

Examples

```
# generate example item response matrix
data <- matrix(rbinom(500, size = 1, prob = 0.5),ncol=10,nrow=50)
result <- onepl(data)</pre>
```

plot

Plotting the interaction map or summarizing the parameter estimate of fitted LSIRM with box plot.

Description

plot is used to plot the interaction map of fitted LSIRM or summarizing the parameter estimate of fitted LSIRM with box plot.

Usage

```
plot(
  object,
  ...,
  option = "interaction",
  rotation = FALSE,
  cluster = NA,
  which.clust = "item",
  interact = FALSE,
  chain.idx = 1
)
```

Arguments

object

cluster

| object | object of class 1511 iii. |
|----------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| | Additional arguments for the corresponding function. |
| option | Character; If value is "interaction", draw the interaction map that represents interactions between respondents and items. If value is "beta", draw the boxplot for the posterior samples of beta. If value is "theta", draw the distribution of the theta estimates per total test score for the data. If value is "alpha", draw the boxplot for the posterior samples of alpha. The "alpha" is only available for 2PL LSIRM. |
| rotation | Logical; If TRUE the latent positions are visualized after oblique (oblimin) rotation. |

Character; If value is "neyman" the cluster result are visualized by Point Process Cluster Analysis. If value is "spectral", spectral clustering method applied.

Default is NA.

Object of class 1sirm.

which.clust Character; Choose which values to clustering. "resp" is the option for respon-

dent and "item" is the option for items. Default is "item".

print.summary.lsirm 139

interact Logical; If TRUE, draw the interaction map interactively.

chain.idx Numeric; Index of MCMC chain. Default is 1.

Value

plot returns the interaction map or boxplot for parameter estimate.

Examples

```
# generate example item response matrix
data     <- matrix(rbinom(500, size = 1, prob = 0.5), ncol=10, nrow=50)
lsirm_result <- lsirm(data ~ lsirm1pl())
plot(lsirm_result)

# use oblique rotation
plot(lsirm_result, rotation = TRUE)

# interaction map interactively
plot(lsirm_result, interact = TRUE)

# clustering the respondents or items
plot(lsirm_result, cluster = TRUE)</pre>
```

Description

print.summary.lsirm is used to print summary the result of LSIRM.

Usage

```
## S3 method for class 'summary.lsirm' print(x, ...)
```

Arguments

x List; summary of LSIRM with summary.lsirm.

... Additional arguments.

Value

```
print.summary.lsirm return a summary of LSIRM.
```

140 summary.lsirm

Examples

```
# generate example item response matrix
data <- matrix(rbinom(500, size = 1, prob = 0.5),ncol=10,nrow=50)
lsirm_result <- lsirm(data ~ lsirm1pl())
summary(lsirm_result)</pre>
```

summary.lsirm

Summary the result of LSIRM

Description

summary is used to summary the result of LSIRM.

Usage

```
## S3 method for class 'lsirm'
summary(object, chain.idx = 1, estimate = "mean", CI = 0.95, ...)
```

Arguments

object Object of class lsirm.

chain.idx Numeric; Index of MCMC chain. Default is 1.

estimate Character; Specifies the type of posterior estimate to provide for beta parameters. Options are "mean", "median", or "mode". Default is "mean".

CI Numeric; The significance level for the highest posterior density interval (HPD) for the beta parameters. Default is 0.95.

... Additional arguments.

Value

summary.lsirm contains following elements. A print method is available.

call R call used to fit the model. Covariate coefficients posterior means. coef mcmc.opt The number of mcmc iteration, burn-in periods, and thinning intervals. map.inf Value of log maximum a posterior and iteration number which have log maximum a posterior. BIC Numeric value with the corresponding Bayesian information criterion (BIC). method Which model is fitted. missing The assumed missing type. One of NA, "mar" and "mcar". Type of input data (Binary or Continuous). dtype Whether a model selection approach using the spike-slab prior is applied. SS

TDRI 141

Examples

```
# generate example item response matrix
data <- matrix(rbinom(500, size = 1, prob = 0.5),ncol=10,nrow=50)
# 1PL LSIRM object
lsirm_result <- lsirm(data ~ lsirm1pl())
summary(lsirm_result)</pre>
```

TDRI

Inductive Reasoning Developmental Test

Description

TDRI dataset is the answer to Inductive Reasoning Developmental Test of 1,803 Brazilians with age varying from 5 to 85 years.

Usage

```
data(TDRI)
```

Format

A binary matrix with 1,803 rows and 56 columns.

Details

It presents data from 1,803 Brazilians (52.5% female) with age varying from 5 to 85 years (M = 15.75; SD = 12.21) that answered to the Inductive Reasoning Developmental Test – IRDT, with 56 items designed to assess developmentally sequenced and hierarchically organized inductive reasoning.

Source

https://figshare.com/articles/dataset/TDRI_dataset_csv/3142321

twopl

twopl

2PL Rasch model.

Description

twopl is used to fit 2PL Rasch model. Unlike 1PL model, 2PL model assumes the item effect can vary according to respondent, allowing additional parameter multiplied with respondent effect.

Usage

```
twopl(
 data,
 niter = 15000,
 nburn = 2500,
 nthin = 5,
 nprint = 500,
  jump\_beta = 0.4,
  jump\_theta = 1,
  jump_alpha = 1,
 pr_mean_beta = 0,
 pr_sd_beta = 1,
 pr_mean_theta = 0,
 pr_mean_alpha = 0.5,
 pr_sd_alpha = 1,
 pr_a_theta = 0.001,
 pr_b_teta = 0.001
)
```

| data | Matrix; binary item response matrix to be analyzed. Each row is assumed to be respondent and its column values are assumed to be response to the corresponding item. |
|--------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| niter | Numeric; number of iterations to run MCMC sampling. default value is 15000. |
| nburn | Numeric; number of initial, pre-thinning, MCMC iterations to discard. default value is 2500. |
| nthin | Numeric;number of thinning, MCMC iterations to discard. default value is 5. |
| nprint | Numeric; MCMC samples is displayed during execution of MCMC chain for each nprint. default value is 500. |
| jump_beta | Numeric; jumping rule of the proposal density for beta. default value is 0.4. |
| jump_theta | Numeric; jumping rule of the proposal density for theta. default value is 1.0. |
| jump_alpha | Numeric; jumping rule of the proposal density for alpha default value is 1.0. |
| pr_mean_beta | Numeric; mean of normal prior for beta. default value is 0. |
| pr_sd_beta | Numeric; standard deviation of normal prior for beta. default value is 1.0. |

twopl 143

pr_mean_theta Numeric; mean of normal prior for theta. default value is 0.

pr_mean_alpha Numeric; mean of normal prior for alpha. default value is 0.5.

pr_sd_alpha Numeric; mean of normal prior for beta. default value is 1.0.

Pr_a_theta Numeric; shape parameter of inverse gamma prior for variance of theta. default value is 0.001.

Pr_b_theta Numeric; scale parameter of inverse gamma prior for variance of theta. default value is 0.001.

Details

twop1 models the probability of correct response by respondent j to item i with item effect β_i , respondent effect θ_j . For 2pl model, the item effect is assumed to have additional discrimination parameter α_i multiplied by θ_j :

$$logit(P(Y_{i,i} = 1 | \theta_i, \beta_i, \alpha_i)) = \theta_i * \alpha_i + \beta_i$$

Value

twopl returns an object of list containing the following components:

beta_estimate posterior estimation of beta.

theta_estimate posterior estimation of theta.

sigma_theta_estimate

posterior estimation of stands

posterior estimation of standard deviation of theta.

alpha_estimate posterior estimation of alpha.

beta posterior samples of beta.

theta posterior samples of theta.

theta_sd posterior samples of standard deviation of theta.

alpha posterior samples of alpha.

accept_beta accept ratio of beta.
accept_theta accept ratio of theta.
accept_alpha accept ratio of alpha.

Examples

```
# generate example item response matrix
data <- matrix(rbinom(500, size = 1, prob = 0.5),ncol=10,nrow=50)
result <- twopl(data)</pre>
```

Index

| BFPT, 3 | lsirm2pl_normal_fixed_gamma_mar, 100, 100 |
|--------------------------------------------------------------------------------------------------------------------------------------------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| diagnostic, 3 | <pre>lsirm2pl_normal_fixed_gamma_mcar, 72,</pre> |
| gof, 4, 4 | lsirm2pl_normal_mar, 72, 107, 107 lsirm2pl_normal_mar_ss, 72, 110, 110 |
| <pre>lsirm, 5, 5 lsirm.formula, 6, 6 lsirm12pl, 6 lsirm1pl, 5-7, 7 lsirm1pl_fixed_gamma, 10, 10 lsirm1pl_fixed_gamma_mar, 10, 13, 13</pre> | lsirm2pl_normal_mcar, 72, 115, 115 lsirm2pl_normal_mcar_ss, 72, 118, 118 lsirm2pl_normal_o, 70, 72, 122, 122 lsirm2pl_normal_ss, 72, 126, 126 lsirm2pl_o, 72, 129, 129 lsirm2pl_ss, 70, 72, 133, 133 |
| lsirm1pl_fixed_gamma_mcar, 10, 16, 16 lsirm1pl_mar, 9, 10, 19, 19 | onepl, <i>136</i> , 136 |
| lsirm1pl_mar_ss, 10, 22, 22 lsirm1pl_mcar, 9, 10, 26, 26 lsirm1pl_mcar_ss, 10, 29, 29 | plot, <i>138</i> , 138 print.summary.lsirm, <i>139</i> , 139 |
| <pre>lsirm1pl_normal_fixed_gamma, 10, 32, 32 lsirm1pl_normal_fixed_gamma_mar, 10, 35,</pre> | summary, <i>140</i> summary.lsirm, 140 |
| <pre>lsirm1pl_normal_fixed_gamma_mcar, 10,</pre> | TDRI, 141 twopl, <i>142</i> , 142 |
| lsirm1pl_normal_mar, 10, 41, 41 lsirm1pl_normal_mar_ss, 10, 45, 45 lsirm1pl_normal_mcar, 10, 49, 49 lsirm1pl_normal_mcar_ss, 10, 52, 52 | |
| lsirm1pl_normal_o, 9, 10, 56, 56 lsirm1pl_normal_ss, 10, 59, 59 | |
| lsirm1pl_o, 10, 62, 62 lsirm1pl_ss, 9, 10, 65, 65 lsirm2pl, 5, 6, 68, 68 | |
| lsirm2pl_fixed_gamma, 72, 72 lsirm2pl_fixed_gamma_mar, 72, 75, 75 lsirm2pl_fixed_gamma_mcar, 72, 78, 78 lsirm2pl_mar, 70, 72, 82, 82 | |
| lsirm2pl_mar_ss, 72, 85, 85, 93 lsirm2pl_mcar, 70, 72, 89, 89 lsirm2pl_mcar_ss, 72, 93 lsirm2pl_normal_fixed_gamma, 72, 97, 97 | |