Package 'BSTFA'

August 28, 2025

Title Bayesian Spatio-Temporal Factor Analysis Model

Description Implements Bayesian spatio-temporal factor analysis models for multivariate data observed across space and time. The package provides tools for model fitting via Markov chain Monte Carlo (MCMC), spatial and temporal interpolation, and visualization of latent factors and loadings to support inference and exploration of underlying spatio-temporal patterns. Designed for use in environmental, ecological, or public health applications, with support for posterior prediction and uncertainty quantification. Includes functions such as BSTFA() for model fitting and plot_factor() to visualize the latent processes. Functions are based on and extended from methods described in Berrett, et al. (2020) <doi:10.1002/env.2609>.

```
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```

License GPL (>= 2)

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bisquare1d

Description

Evaluate bisquare bases for 1-dimensional space. Used internally within makeNewS.

Usage

bisquare1d(locs, knots)

Arguments

Matrix of 1-dimensional coordinates for locations of interest. locs knots A vector of 1-dimensional knot coordinates for a given resolution.

Value

A matrix containing the bisquare bases at a given resolution evaluated at the 1-dimensional input locations.

Author(s)

Candace Berrett and Adam Simpson

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Bisquare bases for 2-dimensional space

Description

Function to evaluate bisquare bases for 2-dimensional space. Used internally within makeNewS.

Usage

```
bisquare2d(locs, knots)
```

Arguments

locs Matrix of 2-dimensional coordinates for locations of interest.

A matrix of 2-dimensional knot coordinates for a given resolution.

Value

A matrix containing the bisquare bases for a given resolution evaluated at the input locations.

Author(s)

Candace Berrett and Adam Simpson

BSTFA

Reduced BSTFA function

Description

This function uses MCMC to draw from posterior distributions of a Bayesian spatio-temporal factor analysis model. All spatial processes use one of Fourier, thin plate spline, or multiresolution basis functions. The temporally-dependent factors use Fourier bases. The default values are chosen to work well for many data sets. Thus, it is possible to use this function using only three arguments: ymat, dates, and coords. The default number of MCMC iterations is 10000 (saving 5000); however, depending on the number of observations and processes modeled, it may need more draws than this to ensure the posterior draws are representative of the entire posterior distribution space.

```
BSTFA(
  ymat,
  dates,
  coords,
  iters = 10000,
  n.times = nrow(ymat),
```

```
n.locs = ncol(ymat),
  x = NULL,
 mean = FALSE,
  linear = TRUE,
  seasonal = TRUE,
  factors = TRUE,
  n.seasn.knots = min(7, ceiling(length(unique(yday(dates)))/3)),
  spatial.style = "eigen",
  n.spatial.bases = min(10, ceiling(n.locs/3)),
  knot.levels = 2,
  max.knot.dist = mean(dist(coords)),
  premade.knots = NULL,
  plot.knots = FALSE,
  n.factors = min(4, ceiling(n.locs/20)),
  factors.fixed = NULL,
  plot.factors = FALSE,
  load.style = "eigen",
  n.load.bases = 4,
  freq.lon = 2 * diff(range(coords[, 1])),
  freq.lat = 2 * diff(range(coords[, 2])),
  n.temp.bases = ifelse(floor(n.times * 0.1)%%2 == 1, floor(n.times * 0.1) - 1,
    floor(n.times * 0.1)),
  freq.temp = n.times,
  alpha.prec = 1/1e+05,
  tau2.gamma = 2,
  tau2.phi = 1e-07,
  sig2.gamma = 2,
  sig2.phi = 1e-05,
  sig2 = NULL,
  beta = NULL,
  xi = NULL,
  Fmat = matrix(0, nrow = n.times, ncol = n.factors),
  Lambda = matrix(0, nrow = n.locs, n.factors),
  thin = 1,
  burn = floor(iters * 0.5),
  verbose = TRUE,
  save.missing = TRUE,
  save.time = FALSE,
 marginalize = FALSE
)
```

Arguments

ymat Data matrix of size n. times by n. locs. Any missing data should be marked by NA. The model works best if the data are zero-centered for each location.

dates n.times length vector of class 'Date' corresponding to each date of the observed data. For now, the dates should be regularly spaced (e.g., daily).

coords n.locs by 2 matrix or data frame of coordinates for the locations of the observed data. If using longitude and latitude, longitude is assumed to be the first coordinate. iters Number of MCMC iterations to draw. Default value is 10000. Function only saves (iters-burn)/thin drawn values. n.times Number of observations for each location. Default is nrow(ymat). n.locs Number of observed locations. Default is ncol(ymat). Optional n.locs by p matrix of covariates for each location. If there are no covariates, set to NULL (default). Logical scalar. If TRUE, the model will fit a spatially-dependent mean for each mean location. Otherwise, the model will assume the means are zero at each location (default). linear Logical scalar. If TRUE (default), the model will fit a spatially-dependent linear increase/decrease (or slope) in time. Otherwise, the model will assume a zero change in slope across time. seasonal Logical scalar. If TRUE (default), the model will use circular b-splines to model a spatially-dependent annual process. Otherwise, the model will assume there is no seasonal (annual) process. factors Logical scalar. If TRUE (default), the model will fit a spatio-temporal factor analysis model with temporally-dependent factors and spatially-dependent loadings. Numeric scalar indicating the number of knots to use for the seasonal basis comn.seasn.knots ponents. The default value is min(7, ceiling(length(unique(yday(dates)))/3)), where 7 will capture approximately 2 peaks during the year. spatial.style Character scalar indicating the style of bases to use for the linear and seasonal components. Style options are 'fourier' (default), 'tps' for thin plate splines, and 'grid' for multiresolution bisquare bases using knots from a grid across the space. n.spatial.bases Numeric scalar indicating the number of spatial bases to use when spatial.style is either 'fourier' or 'tps'. Default value is min(16, ceiling(n.locs/3)). When spatial.style is 'fourier', this value must be an even square number. knot.levels Numeric scalar indicating the number of resolutions to use for when spatial.style='grid' and/or load.style='grid'. Default is 2. max.knot.dist Numeric scalar indicating the maximum distance at which a basis value is greater than zero when spatial.style='grid' and/or load.style='grid'. Default value is mean(dist(coords)). Optional list of length knot.levels with each list element containing a mapremade.knots trix of longitude-latitude coordinates of the knots to use for each resolution when spatial.style='grid' and/or load.style='grid'. Otherwise, when premade.knots = NULL (default), the knots are determined by using the standard multiresolution grids across the space. plot.knots Logical scalar indicating whether to plot the knots used when spatial.style='grid'

and/or load.style='grid'. Default is FALSE.

n.factors	Numeric scalar indicating how many factors to use in the model. Default is min(4,ceiling(n.locs/20)).
factors.fixed	Numeric vector of length n. factors indicating the locations to use for the fixed loadings. This is needed for model identifiability. If factors.fixed=NULL (default), the code will select locations with less than 20% missing data and that are far apart in the space.
plot.factors	Logical scalar indicating whether to plot the fixed factor locations. Default is FALSE.
load.style	Character scalar indicating the style of spatial bases to use for the spatially-dependent loadings. Options are 'fourier' (default) for the Fourier bases, 'tps' for thin plate splines, and 'grid' for multiresolution bases. This can be the same as or different than spatial.style.
n.load.bases	Numeric scalar indicating the number of bases to use for the spatially-dependent loadings when load.style is either 'fouier' or 'tps'. This can be the same as or different than n. spatial.bases. Default is 4. When load.style='fourier this value must be an even square number.
freq.lon	Numeric scalar used for spatial.style or load.style equal to 'fourier' or 'eigen'. For 'fourier', this is the frequency used for the first column of coords (assumed to be longitude) for the Fourier bases. For 'eigen', this is the range parameter of the exponential spatial correlation matrix used to create the eigenvectors. Default value is 2*diff(range(coords[,1])).
freq.lat	Numeric scalar used for spatial.style or load.style equal to 'fourier'. This is the frequency to use for the second column of coords (assumed to be latitude) for the Fourier bases. Default value is 2*diff(range(coords[,2])).
n.temp.bases	Numeric scalar indicating the number of Fourier bases to use for the temporally-dependent factors. The default value is 10% of n.times.
freq.temp	Numeric scalar indicating the frequency to use for the Fourier bases of the temporally-dependent factors. The default value is n. times.
alpha.prec	Numeric scalar indicating the prior precision for all model process coefficients. Default value is 1/100000.
tau2.gamma	Numeric scalar indicating the prior shape for the precision of the model coefficients. Default value is 2.
tau2.phi	Numeric scalar indicating the prior rate for the precision of the model coefficients. Default value is 1e-07.
sig2.gamma	Numeric scalar indicating the prior shape for the residual precision. Default value is 2.
sig2.phi	Numeric scalar indicating the prior rate for the residual precision. Default value is 1e-05.
sig2	Numeric scalar indicating the starting value for the residual variance. If NULL (default), the function will select a reasonable starting value.
beta	Numeric vector of length n.locs + p indicating starting values for the slopes. If NULL (default), the function will select reasonable starting values.
xi	Numeric vector of length (n.locs + p)*n.seasn.knots indicating starting values for the coefficients of the seasonal component. If NULL (default), the function will select reasonable starting values.

Fmat	Numeric matrix of size n. times by n. factors indicating starting values for the factors. Default value is to start all factor values at 0.
Lambda	Numeric matrix of size n.locs by n.factors indicating starting values for the loadings. Default value is to start all loadings at 0 .
thin	Numeric scalar indicating how many MCMC iterations to thin by. Default value is 1, indicating no thinning.
burn	Numeric scalar indicating how many MCMC iterations to burn before saving. Default value is one-half of iters.
verbose	Logical scalar indicating whether or not to print the status of the MCMC process. If TRUE (default), the function will print every time an additional 10% of the MCMC process is completed.
save.missing	Logical scalar indicating whether or not to save the MCMC draws for the missing observations. If TRUE (default), the function will save an additional MCMC object containing the MCMC draws for each missing observation. Use FALSE to save file space and memory.
save.time	Logical scalar indicating whether to save the computation time for each MCMC iteration. Default value is FALSE. When FALSE, the function compute_summary() will not be useful.
marginalize	Logical scalar indicating whether to sample hyper-coefficients by marginalizing out the corresponding parameters. Default value is FALSE. Setting to TRUE will be slower but can improve effective sample sizes.

Value

A list containing the following elements (any elements that are the same as in the function input are removed here for brevity):

- **mu** An meme object of size draws by n.locs containing posterior draws for the mean of each location. If mean=FALSE (default), the values will all be zero.
- **alpha.mu** An mcmc object of size draws by n.spatial.bases + p containing posterior draws for the coefficients modeling the mean process. If mean=FALSE (default), the values will all be zero.
- **tau2.mu** An meme object of size draws by 1 containing the posterior draws for the variance of the mean process. If mean=FALSE (default), the values will all be zero.
- **beta** An mcmc object of size draws by n.locs containing the posterior draws for the increase/decrease (slope) across time for each location.
- **alpha.beta** An mcmc object of size draws by n.spatial.bases + p containing posterior draws for the coefficients modeling the slope.
- **tau2.beta** An mcmc object of size draws by 1 containing posterior draws of the variance of the slopes.
- xi An mcmc object of size draws by n.seasn.knots*n.locs containing posterior draws for the coefficients of the seasonal process.
- **alpha.xi** An mcmc object of size draws by (n.spatial.bases + p)*n.seasn.knots containing posterior draws for the coefficients modeling each coefficient of the seasonal process.

tau2.xi An mcmc object of size draws by n.seasn.knots containing posterior draws of the variance of the coefficients of the seasonal process.

- **F.tilde** An mcmc object of size draws by n.times*n.factors containing posterior draws of the residual factors.
- **alphaT** An mcmc object of size draws by n.factors*n.temp.bases containing posterior draws of the coefficients for the factor temporally-dependent process.
- **Lambda.tilde** An meme object of size draws by n.factors*n.locs containing posterior draws of the loadings for each location.
- **alphaS** An meme object of size draws by n.factors*n.load.bases containing posterior draws of the coefficients for the loadings spatial process.
- **tau2.lambda** An meme object of size draws by 1 indicating the residual variance of the loadings spatial process.
- sig2 An meme object of size draws by 1 containing posterior draws of the residual variance of the data.
- **y.missing** If save.missing=TRUE, a matrix of size sum(missing) by draws containing posterior draws of the missing observations. Otherwise, the object is NULL.
- **time.data** A data frame of size iters by 6 containing the time it took to sample each parameter for every iteration.
- **setup.time** An object containing the time the model setup took.
- model.matrices A list containing the matrices used for each modeling process. newS is the matrix of spatial basis coefficients for the mean, linear, and seasonal process coefficients. linear.Tsub is the matrix used to enforce a linear increase/increase (slope) across time. seasonal.bs.basis is the matrix containing the circular b-splines of the seasonal process. confoundingPmat.prime is the matrix that enforces orthogonality of the factors from the mean, linear, and seasonal processes. QT contains the Fourier bases used to model the temporal factors. QS contains the bases used to model the spatial loadings.
- factors.fixed A vector of length n. factors giving the location indices of the fixed loadings.
- **iters** A scalar returning the number of MCMC iterations.
- y An n. times*n. locs vector of the observations.
- missing A logical vector indicating whether that element's observation was missing or not.
- doy A numeric vector of length n. times containing the day of year for each element in the original dates.
- knots.spatial For spatial.style='grid', a list of length knot.levels containing the coordinates for all knots at each resolution.
- **knots.load** For load.style='grid', a list of length knot.levels containing the coordinates for all knots at each resolution.
- draws The number of saved MCMC iterations after removing the burn-in and thinning.

Author(s)

Adam Simpson and Candace Berrett

Examples

```
data(utahDataList)
attach(utahDataList)
low.miss <- which(apply(is.na(TemperatureVals), 2, mean)<.02)
out <- BSTFA(ymat=TemperatureVals[1:50,low.miss],
    dates=Dates[1:50],
    coords=Coords[low.miss,],
    n.factors=2,
    iters=10)</pre>
```

BSTFAfull

Full BSTFA function

Description

This function uses MCMC to draw from posterior distributions of a Bayesian spatio-temporal factor analysis model. The spatial processes for the mean, linear, and seasonal behavior use one of Fourier, thin plate spline, or multiresolution basis functions. The temporal dependence of the factors is modeled using a vector autoregressive model. The spatially-dependent loadings are modeled using a mean-zero Gaussian process with an exponential covariance structure. The default values are chosen to work well for many data sets. Thus, it is possible to use this function using only three arguments: ymat, dates, and coords. The default number of MCMC iterations is 10000 (saving 5000); however, depending on the number of observations and processes modeled, it may need more draws than this to ensure the posterior draws are representative of the entire posterior distribution space.

```
BSTFAfull(
  ymat,
  dates.
  coords,
  iters = 10000,
  n.times = nrow(ymat),
  n.locs = ncol(ymat),
  x = NULL
  mean = FALSE,
  linear = TRUE,
  seasonal = TRUE,
  factors = TRUE,
  n.seasn.knots = min(7, ceiling(length(unique(yday(dates)))/3)),
  spatial.style = "grid",
  n.spatial.bases = ceiling(n.locs/2),
  knot.levels = 2,
  max.knot.dist = n.locs * 0.05,
  premade.knots = NULL,
  plot.knots = FALSE,
```

```
freq.lon = diff(range(coords[, 1])),
  freq.lat = diff(range(coords[, 2])),
  n.factors = min(4, ceiling(n.locs/20)),
  factors.fixed = NULL,
  plot.factors = FALSE,
  alpha.prec = 1/1e+05,
  tau2.gamma = 2,
  tau2.phi = 1e-07,
  sig2.gamma = 2,
  sig2.phi = 1e-05,
  omega.ii.mean = 1,
  omega.ii.var = 1,
  omega.ij.mean = 0,
  omega.ij.var = 2,
  S.F = diag(1, n.factors),
  nu.F = n.factors,
  phi.gamma = 3,
  phi.phi = 0.5,
  sig2 = NULL,
  beta = NULL,
 xi = NULL,
  Fmat = matrix(0, nrow = n.times, ncol = n.factors),
  Omega = diag(1, n.factors),
  Sigma.F = diag(1, n.factors),
 Lambda = matrix(0, nrow = n.locs, n.factors),
  phi.lambda = rep(1, n.factors),
  thin = 1,
  burn = floor(iters * 0.5),
  c.omega = matrix(0.001, n.factors, n.factors),
  c.phi.lambda = rep(0.001, n.factors),
  adapt.iter = (burn + 10),
  adapt.epsilon = 1e-20,
  verbose = TRUE,
  save.missing = TRUE,
  save.time = FALSE
)
```

Arguments

ymat	Data matrix of size n. times by n. locs. Any missing data should be marked by NA. The model works best if the data are zero-centered for each location.
dates	n.times length vector of class 'Date' corresponding to each date of the observed data. For now, the dates should be regularly spaced (e.g., daily).
coords	n.locs by 2 matrix or data frame of coordinates for the locations of the observed data. If using longitude and latitude, longitude is assumed to be the first coordinate.
iters	Number of MCMC iterations to draw. Default value is 10000. Function only saves (iters-burn)/thin drawn values.

n.times	Number of observations for each location. Default is nrow(ymat).
n.locs	Number of observed locations. Default is ncol(ymat).
х	Optional n.locs by p matrix of covariates for each location. If there are no covariates, set to NULL (default).
mean	Logical scalar. If TRUE, the model will fit a spatially-dependent mean for each location. Otherwise, the model will assume the means are zero at each location (default).
linear	Logical scalar. If TRUE (default), the model will fit a spatially-dependent linear increase/decrease (or slope) in time. Otherwise, the model will assume a zero change in slope across time.
seasonal	Logical scalar. If TRUE (default), the model will use circular b-splines to model a spatially-dependent annual process. Otherwise, the model will assume there is no seasonal (annual) process.
factors	Logical scalar. If TRUE (default), the model will fit a spatio-temporal factor analysis model with temporally-dependent factors and spatially-dependent loadings.
n.seasn.knots	Numeric scalar indicating the number of knots to use for the seasonal basis components. The default value is min(7, ceiling(length(unique(lubridate::yday(dates)))/3)), where 7 will capture approximately 2 peaks during the year.
spatial.style	Character scalar indicating the style of bases to use for the mean, linear, and seasonal components. Style options are 'fourier', 'tps' for thin plate splines, and 'grid' (default) for multiresolution bisquare bases using knots from a grid across the space.
n.spatial.base	
n.spatial.base	Numeric scalar indicating the number of spatial bases to use when spatial.style is either 'fourier' or 'tps'. Default value is min(8, ceiling(n.locs/3)).
knot.levels	Numeric scalar indicating the number of spatial bases to use when spatial.style
	Numeric scalar indicating the number of spatial bases to use when spatial.style is either 'fourier' or 'tps'. Default value is min(8, ceiling(n.locs/3)). Numeric scalar indicating the number of resolutions to use for when spatial.style='grid'.
knot.levels	Numeric scalar indicating the number of spatial bases to use when spatial.style is either 'fourier' or 'tps'. Default value is min(8, ceiling(n.locs/3)). Numeric scalar indicating the number of resolutions to use for when spatial.style='grid'. Default is 2. Numeric scalar indicating the maximum distance at which a basis value is greater
<pre>knot.levels max.knot.dist</pre>	Numeric scalar indicating the number of spatial bases to use when spatial.style is either 'fourier' or 'tps'. Default value is min(8, ceiling(n.locs/3)). Numeric scalar indicating the number of resolutions to use for when spatial.style='grid'. Default is 2. Numeric scalar indicating the maximum distance at which a basis value is greater than zero when spatial.style='grid'. Default value is mean(dist(coords)). Optional list of length knot.levels with each list element containing a matrix of longitude-latitude coordinates of the knots to use for each resolution when spatial.style='grid'. Otherwise, when premade.knots = NULL (default), the knots are determined by using the standard multiresolution grids across the
knot.levels max.knot.dist premade.knots	Numeric scalar indicating the number of spatial bases to use when spatial.style is either 'fourier' or 'tps'. Default value is min(8, ceiling(n.locs/3)). Numeric scalar indicating the number of resolutions to use for when spatial.style='grid'. Default is 2. Numeric scalar indicating the maximum distance at which a basis value is greater than zero when spatial.style='grid'. Default value is mean(dist(coords)). Optional list of length knot.levels with each list element containing a matrix of longitude-latitude coordinates of the knots to use for each resolution when spatial.style='grid'. Otherwise, when premade.knots = NULL (default), the knots are determined by using the standard multiresolution grids across the space. Logical scalar indicating whether to plot the knots used when spatial.style='grid'.
knot.levels max.knot.dist premade.knots plot.knots	Numeric scalar indicating the number of spatial bases to use when spatial.style is either 'fourier' or 'tps'. Default value is min(8, ceiling(n.locs/3)). Numeric scalar indicating the number of resolutions to use for when spatial.style='grid'. Default is 2. Numeric scalar indicating the maximum distance at which a basis value is greater than zero when spatial.style='grid'. Default value is mean(dist(coords)). Optional list of length knot.levels with each list element containing a matrix of longitude-latitude coordinates of the knots to use for each resolution when spatial.style='grid'. Otherwise, when premade.knots = NULL (default), the knots are determined by using the standard multiresolution grids across the space. Logical scalar indicating whether to plot the knots used when spatial.style='grid'. Default is FALSE. Numeric scalar indicating the frequency to use for the first column of coords (assumed to be longitude) for the Fourier bases when spatial.style='fourier'.

factors.fixed	Numeric vector of length n. factors indicating the locations to use for the fixed loadings. This is needed for model identifiability. If factors.fixed=NULL (default), the code will select locations with less than 20% missing data and that are far apart in the space.
plot.factors	Logical scalar indicating whether to plot the fixed factor locations. Default is FALSE.
alpha.prec	Numeric scalar indicating the prior precision for all model process coefficients. Default value is 1/100000.
tau2.gamma	Numeric scalar indicating the prior shape for the precision of the model coefficients. Default value is 2.
tau2.phi	Numeric scalar indicating the prior rate for the precision of the model coefficients. Default value is 1e-07.
sig2.gamma	Numeric scalar indicating the prior shape for the residual precision. Default value is 2.
sig2.phi	Numeric scalar indicating the prior rate for the residual precision. Default value is 1e-05.
omega.ii.mean	Numeric scalar indicating the prior mean for the diagonal elements of the autoregressive correlation matrix of the factors. Default is 1.
omega.ii.var	Numeric scalar indicating the prior variance for the diagonal elements of the autoregressive correlation matrix of the factors. Default is 1.
omega.ij.mean	Numeric scalar indicating the prior mean for the off-diagonal elements of the autoregressive correlation matrix of the factors. Default is 0.
omega.ij.var	Numeric scalar indicating the prior variance for the off-diagonal elements of the autoregressive correlation matrix of the factors. Default is 2.
S.F	Numeric matrix of size n.factors by n.factors indicating the prior residual covariance matrix for the factors. Default is diag(1,n.factors).
nu.F	Numeric scalar indicating the prior degrees of freedom for the residual covariance matrix of the factors. Default is n.factors; must be greater than or equal to n.factors.
phi.gamma	Numeric scalar indicating the prior shape of the spatial range parameter for the spatially-dependent loadings. Default value is 3.
phi.phi	Numeric scalar indicating the prior rate of the spatial range parameter for the spatially-dependent loadings. Default is 0.5.
sig2	Numeric scalar indicating the starting value for the residual variance. If NULL (default), the function will select a reasonable starting value.
beta	Numeric vector of length n.locs + p indicating starting values for the slopes. If NULL (default), the function will select reasonable starting values.
xi	Numeric vector of length $(n.locs + p)*n.seasn.knots$ indicating starting values for the coefficients of the seasonal component. If NULL (default), the function will select reasonable starting values.
Fmat	Numeric matrix of size n.times by n. factors indicating starting values for the factors. Default value is to start all factor values at 0.

Omega	Numeric matrix of size n.factors by n.factors indicating the starting value for the autoregressive correlation of the factors. Default value is the identity matrix.
Sigma.F	Numeric matrix of size n.factors by n.factors indicating the starting value for the residual covariance matrix of the factors. Default value is the identity matrix.
Lambda	Numeric matrix of size n.locs by n.factors indicating starting values for the loadings. Default value is to start all loadings at 0.
phi.lambda	Numeric vector of length n. factors indicating the starting values for the spatial range parameters for each loading. Default value is a vector of 1's.
thin	Numeric scalar indicating how many MCMC iterations to thin by. Default value is 1, indicating no thinning.
burn	Numeric scalar indicating how many MCMC iterations to burn before saving. Default value is one-half of iters.
c.omega	Numeric matrix of starting values for the proposal standard deviations (for the Metropolis random walk algorithm) for sampling proposal values of the autoregressive correlation matrix for the factors. Default is matrix(0.001, n.factors, n.factors).
c.phi.lambda	Numeric vector of starting values for the proposal standard deviations (for the Metropolis random walk algorithm) for sampling proposal values of the range of the spatially-dependent loadings. Default is rep(0.001, n.factors).
adapt.iter	Numeric scalar indicating the number of iterations to start adjusting the proposal standard deviations for the Metropolis random walk algorithms. Value must be at least 2 larger than burn. Default value is burn+10.
adapt.epsilon	Numeric scalar indicating the small value to add to the proposal standard deviations when using the adaptive Metropolis random walk algorithms. Default is 1e-20.
verbose	Logical scalar indicating whether or not to print the status of the MCMC process. If TRUE (default), the function will print every time an additional 10% of the MCMC process is completed.
save.missing	Logical scalar indicating whether or not to save the MCMC draws for the missing observations. If TRUE (default), the function will save an additional MCMC object containing the MCMC draws for each missing observation. Use FALSE to save file space and memory.
save.time	Logical scalar indicating whether to save the computation time for each MCMC iteration. Default value is FALSE. When FALSE, the function compute_summary() will not be useful.

Value

A list containing the following elements (any elements that are the same as in the function input are removed here for brevity):

mu An meme object of size draws by n.locs containing posterior draws for the mean of each location. If mean=FALSE (default), the values will all be zero.

alpha.mu An mcmc object of size draws by n.spatial.bases + p containing posterior draws for the coefficients modeling the mean process. If mean=FALSE (default), the values will all be zero.

- **tau2.mu** An meme object of size draws by 1 containing the posterior draws for the variance of the mean process. If mean=FALSE (default), the values will all be zero.
- **beta** An mcmc object of size draws by n.locs containing the posterior draws for the increase/decrease (slope) across time for each location.
- **alpha.beta** An meme object of size draws by n.spatial.bases + p containing posterior draws for the coefficients modeling the slope.
- **tau2.beta** An mcmc object of size draws by 1 containing posterior draws of the variance of the slopes.
- xi An mcmc object of size draws by n.seasn.knots*n.locs containing posterior draws for the coefficients of the seasonal process.
- **alpha.xi** An mcmc object of size draws by (n.spatial.bases + p)*n.seasn.knots containing posterior draws for the coefficients modeling each coefficient of the seasonal process.
- **tau2.xi** An meme object of size draws by 1 containing posterior draws of the variance of the coefficients of the seasonal process.
- **F.tilde** An mcmc object of size draws by n.times*n.factors containing posterior draws of the residual factors.
- **alphaT** An meme object of size draws by n.factors*n.temp.bases containing posterior draws of the coefficients for the factor temporally-dependent process.
- **Lambda.tilde** An mcmc object of size draws by n.factors*n.locs containing posterior draws of the loadings for each location.
- **alphaS** An mcmc object of size draws by n.factors*n.load.bases containing posterior draws of the coefficients for the loadings spatial process.
- **tau2.lambda** An meme object of size draws by 1 indicating the residual variance of the loadings spatial process.
- **sig2** An mcmc object of size draws by 1 containing posterior draws of the residual variance of the data.
- **y.missing** If save.missing=TRUE, a matrix of size sum(missing) by draws containing posterior draws of the missing observations. Otherwise, the object is NULL.
- **time.data** A data frame of size iters by 6 containing the time it took to sample each parameter for every iteration.
- **setup.time** An object containing the time the model setup took.
- **model.matrices** A list containing the matrices used for each modeling process. newS is the matrix of spatial basis coefficients for the mean, linear, and seasonal process coefficients. linear.Tsub is the matrix used to enforce a linear increase/increase (slope) across time. seasonal.bs.basis is the matrix containing the circular b-splines of the seasonal process. confoundingPmat.prime is the matrix that enforces orthogonality of the factors from the mean, linear, and seasonal processes. QT contains the fourier bases used to model the temporal factors. QS contains the bases used to model the spatial loadings.
- **factors.fixed** A vector of length n. factors giving the location indices of the fixed loadings.
- **iters** A scalar returning the number of MCMC iterations.

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y An n. times*n.locs vector of the observations.

missing A logical vector indicating whether that element's observation was missing or not.

doy A numeric vector of length n. times containing the day of year for each element in the original dates.

knots.spatial For spatial.style='grid', a list of length knot.levels containing the coordinates for all knots at each resolution.

draws The number of saved MCMC iterations after removing the burn-in and thinning.

Author(s)

Candace Berrett and Adam Simpson

Examples

computeLogLik

Compute log-likelihood

Description

Compute log-likelihood

Usage

```
computeLogLik(out, verbose = FALSE, addthin = 1)
```

Arguments

out Output from BSTFA or BSTFAfull.

verbose Logical scalar indicating whether to print status of the log-likelihood computa-

tion. Default is FALSE.

addthin Numeric scalar indicating the number of additional draws to thin by to reduce

the computation time. Default is 1 (no additional thinning).

Value

A matrix of size n.times*n.locs by draws log-likelihood values for each observation and each posterior draw.

16 compute_summary

Author(s)

Adam Simpson and Candace Berrett

Examples

```
data(out.sm)
attach(out.sm)
loglik <- computeLogLik(out.sm, addthin=2)</pre>
```

compute_summary

Print computation summary

Description

Print computation summary

Usage

```
compute_summary(out)
```

Arguments

out

Output from BSTFA or BSTFAfull.

Value

Prints the computation time per iteration for each parameter.

Author(s)

Adam Simpson

Examples

```
data(utahDataList)
attach(utahDataList)
low.miss <- which(apply(is.na(TemperatureVals), 2, mean)<.02)
out <- BSTFA(ymat=TemperatureVals[1:50,low.miss],
    dates=Dates[1:50],
    coords=Coords[low.miss,],
    n.factors=2,
    iters=10,
    save.time=TRUE)
compute_summary(out)</pre>
```

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convergence_diag

Check effective sample size and geweke diagnostic

Description

Check effective sample size and geweke diagnostic

Usage

```
convergence_diag(out, type = "eSS", cutoff = ifelse(type == "eSS", 100, 1.96))
```

Arguments

out Output from BSTFA or BSTFAfull.

type Character specifying which diagnostic to compute. Options are ess and geweke. cutoff Numeric scalar indicating the cutoff value to flag parameters that haven't con-

verged.

Value

A list containing the parameters not meeting the convergence cutoff criteria.

Author(s)

Adam Simpson

Examples

```
data(out.sm)
attach(out.sm)
convergence_diag(out.sm)
```

defineRegion

Define the initial region of interest.

Description

Define the region of interest. Used internally in the makePredS function.

Usage

```
defineRegion(out, location)
```

Arguments

out Output object from BSTFA or BSTFAfull functions.

location Matrix of coordinates for the new locations.

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Value

A list where each element of the list returns a vector of defining the "region" for each prediction location for the given knot resolution.

Author(s)

Candace Berrett and Adam Simpson

makeNewS

Create a matrix of bisquare bases for a set of locations.

Description

Create a matrix of bisquare bases for a set of locations. Used internally in BSTFA and BSTFAfull.

Usage

```
makeNewS(
  coords,
  n.locations,
  knot.levels = 2,
  max.knot.dist = mean(dist(coords)),
  x = NULL,
  premade.knots = NULL,
  plot.knots = FALSE,
  regions = FALSE
)
```

Arguments

coords Matrix of coordinates for locations of interest.

n.locations Number of observed locations.

knot.levels Number of levels for the knots. Default is 2.

max.knot.dist Maximum distance between an observation and a knot. Default is mean(dist(coords)).

x Optional matrix of covariates to include in the model.

premade.knots Optional list of length knot.levels each list item containing pre-chosen knots

for that level.

plot . knots Logical scalar indicating whether or not to plot the knots. Default is FALSE.

regions Logical scalar indicating if the space should be divided into multiresolution re-

gions. Default is FALSE.

Value

A matrix containing all the multiresolution bisquare bases evaluated at the input coordinates.

makePredS 19

Author(s)

Candace Berrett and Adam Simpson

makePredS

Create a matrix of bisquare bases for new locations.

Description

Create a matrix of bisquare bases for new locations. Used internally within the predictBSTFA function. Currently only implemented for 2-dimensional coordinates.

Usage

```
makePredS(out, location)
```

Arguments

out Output object from BSTFA or BSTFAfull functions.

location Matrix of coordinates for the new locations.

Value

A matrix containing the appropriate multiresolution bisquare bases evaluated at the input locations.

Author(s)

Candace Berrett and Adam Simpson

map_spatial_param

Plot a map of interpolated spatially-dependent parameter values.

Description

Plot a map of interpolated spatially-dependent parameter values.

```
map_spatial_param(
  out,
  parameter = "slope",
  loadings = 1,
  type = "mean",
  yearscale = TRUE,
  new_x = NULL,
  ci.level = c(0.025, 0.975),
```

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```
fine = 100,
color.gradient = (grDevices::colorRampPalette(rev(RColorBrewer::brewer.pal(9, name =
    "RdBu"))))(fine),
with.uncertainty = FALSE,
map = FALSE,
state = FALSE,
location = NULL,
addthin = 1
)
```

Arguments

out Output from BSTFA or BSTFAfull.

parameter One of 'slope' (default), 'loading', or 'mean'.

loadings If parameter='loading', an integer indicating which factor loading to plot.

type One of mean (default), median, ub, or 1b indicating which summary statistic to

plot at each location.

yearscale If parameter='slope', a logical scalar indicating whether to translate it to a

yearly scale (TRUE; default).

new_x If the original model included covariates x, include the same covariates for pre-

diction location.

ci.level If type='lb' or 'ub', the percentiles for the posterior interval.

fine Integer specifying the number of grid points along both the longitude and lat-

itude directions used to interpolate the parameter. The resulting interpolation grid will contain fine*fine total locations. If map=TRUE, state=TRUE, and location is specified, the grid will be clipped to the boundaries of the specified

state, removing locations outside of it.

color.gradient The color palette to use for the plot. Default is colorRampPalette(rev(RColorBrewer::brewer.pal(9

name='RdBu')))(fine).

with.uncertainty

Logical scalar indicating whether to include lower and upper credible interval

bounds for the parameter. Default is FALSE.

map Logical scalar indicating whether to include a map. Default value is FALSE. If

TRUE, location must be specified.

state Logical scalar used when map=TRUE indicating whether the location is a state

in the United States (TRUE) or a country (FALSE).

location Name of region to include in the map. Fed to region in the function ggplot2::map_data.

addthin Integer indicating the number of saved draws to thin. Default is to not thin

any addthin=1. This can save time when the object is from BSTFAfull and

parameter='loading'.

Value

A plot of spatially-dependent parameter values for a grid of interpolated locations.

out.sm 21

Author(s)

Adam Simpson and Candace Berrett

Examples

```
data(out.sm)
attach(out.sm)
map_spatial_param(out.sm, parameter='slope', map=TRUE, state=TRUE, location='utah', fine=25)
```

out.sm

Output of BSTFA evaluated on a subset of utahDataList

Description

List object named out.sm containing the output from running the BSTFA function provided in the example code below using a subset of the utahDataList.

Usage

out.sm

Format

See help(BSTFA) for details of what is included as output from the BSTFA function.

Examples

```
data(out.sm)
#Code used to obtain this output
data("utahDataList")
attach(utahDataList)
dates.ind <- 1151:1251
locs.use <- c(3, 8, 11, 16, 17,
               20, 23, 29, 30, 46,
               47, 49, 60, 62, 66, 73,
               75, 76, 77, 78, 85, 89, 94,
               96, 98, 100, 109, 112,
               115, 121, 124, 128, 133, 144)
temps.sm <- TemperatureVals[dates.ind, locs.use]</pre>
coords.sm <- Coords[locs.use,]</pre>
dates.sm <- Dates[dates.ind]</pre>
locsm.names <- Locations[locs.use]</pre>
set.seed(466)
out.sm <- BSTFA(ymat=temps.sm,</pre>
                 dates=dates.sm,
                 coords=coords.sm,
                 iters=5000,
                 burn=1000,
```

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```
thin=40,
factors.fixed=c(14, 22, 15, 20),
n.temp.bases=45,
save.missing=FALSE)
```

plot_annual

Plot annual/seasonal behavior at a specific location.

Description

Plot annual/seasonal behavior at a specific location.

Usage

```
plot_annual(
   out,
   location,
   add = FALSE,
   years = "one",
   interval = 0.95,
   yrange = NULL,
   new_x = NULL
)
```

Arguments

out	Output from BSTFA or BSTFAfull.
location	Either a single integer indicating the location in the data set to plot or a vector of length 2 providing the longitude and latitude of the new location.
add	Logical scalar indicating whether the annual/seasonal process should be added to the existing plot. Default is FALSE.
years	Either 'one' (indicating to plot just a single year; default) or 'all' (indicating to plot all years in the observed time period).
interval	Numeric value between 0 and 1 specifying the probability of the credible interval.
yrange	Numeric vector of length 2 providing the lower and upper bounds of the y-axis. If NULL (default), the y-axis limits are chosen using the range of the seasonal process and data.
new_x	If the original model included covariates \boldsymbol{x} , include the same covariates for location.

Value

A plot of the annual/seasonal process at location.

plot_factor 23

Author(s)

Candace Berrett and Adam Simpson

Examples

```
data(out.sm)
attach(out.sm)
plot_annual(out.sm, location=1)
```

plot_factor

Plot the temporally-dependent factors.

Description

Plot the temporally-dependent factors.

Usage

```
plot_factor(
  out,
  factor = 1,
  together = FALSE,
  include.legend = TRUE,
  type = "mean",
  uncertainty = TRUE,
  ci.level = c(0.025, 0.975),
  xrange = NULL
)
```

Arguments

out	Output from	BSTFA o	or BSTFAfull.

factor Integer or vector of integers specifying which factor(s) to plot.

together If length(factor)>1, logical scalar specifying whether to plot all factors on a

single plot. Default is FALSE.

include.legend If length(factor)>1 and together=TRUE, a logical scalar specifying whether

to include a legend. Default is TRUE.

type One of mean (default), median, ub, or 1b indicating which summary statistic to

plot at each location.

uncertainty Logical scalar indicating whether to include lower and upper credible interval

bounds for the parameter. Default is FALSE.

ci.level A vector of length 2 specifying the quantiles to use for lower and upper bounds

for type='lb', type='ub', or uncertainty=TRUE.

xrange A date vector of length 2 providing the lower and upper bounds of the dates to

include in the plot.

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Value

A plot of spatially-dependent parameter values for a grid of interpolated locations.

Author(s)

Candace Berrett and Adam Simpson

Examples

```
data(out.sm)
attach(out.sm)
plot_factor(out.sm, factor=1:4, together=TRUE)
```

plot_fourier_bases

Visualize fourier bases.

Description

Visualize fourier bases.

Usage

```
plot_fourier_bases(
  coords,
  R = 6,
  fine = 100,
  plot.3d = FALSE,
  freq.lon = diff(range(coords[, 1])),
  freq.lat = diff(range(coords[, 2])),
  par.mfrow = c(2, 3)
)
```

Arguments

coords	A matrix of coordinates of observed locations.
R	Integer indicating the number of bases to compute.
fine	Number of grid points to include on both axes. Total grid size will be fine^2. Default is 100.
plot.3d	Logical scalar indicating whether to plot the bases. Default is FALSE.
freq.lon	Numeric value indicating the frequency to use for the Fourier bases in the longitude direction. Default is diff(range(coords[,1])).
freq.lat	Numeric value indicating the frequency to use for the Fourier bases in the latitude direction. Default is diff(range(coords[,2])).
par.mfrow	If plot.3d=TRUE, how to divide the plotting window. See help(par) for more details.

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Value

A plot of the Fourier bases for a given frequency.

Author(s)

Adam Simpson

plot_location

Plot a location's time series of estimated/predicted values.

Description

Plot a location's time series of estimated/predicted values.

Usage

```
plot_location(
   out,
   location,
   new_x = NULL,
   type = "mean",
   par.mfrow = c(1, 1),
   pred.int = FALSE,
   ci.level = c(0.025, 0.975),
   uncertainty = TRUE,
   xrange = NULL,
   truth = FALSE,
   ylim = NULL
)
```

Arguments

out	Output from BSTFA or BSTFAfull.
location	Either a single integer indicating the location in the data set to plot or a vector of length 2 providing the longitude and latitude of the new location.
new_x	If the original model included covariates \boldsymbol{x} , include the same covariates for prediction location.
type	One of mean (default), median, ub, or 1b indicating which summary statistic of the predicted values to return.
par.mfrow	A vector of length 2 indicating the number of rows and columns to divide the plotting window. Default is $c(1,1)$.
pred.int	Logical scalar indicating whether the interval should be a posterior predictive interval (TRUE) or a posterior credible interval (FALSE; default).
ci.level	If type='lb' or 'ub', the percentiles for the posterior interval.

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uncertainty	Logical scalar indicating whether to plot the uncertainty bounds (TRUE; default) or not.
xrange	A date vector of length 2 providing the lower and upper bounds of the dates to include in the plot.
truth	Logical scalar indicating whether to include the observed measurements (TRUE) or not (default). If TRUE, location must be an integer corresponding to the column of the data matrix for the in-sample prediction location.
ylim	Numeric vector of length 2 providing the lower and upper bounds of the y-axis. If NULL (default), the y-axis limits are chosen using the range of the predictions.

Value

A plot of predicted values for location.

Author(s)

Candace Berrett and Adam Simpson

Examples

```
data(out.sm)
attach(out.sm)
plot_location(out.sm, location=1, pred.int=FALSE)
```

plot_spatial_param

Plot the spatially-dependent parameter for in-sample locations.

Description

Plot the spatially-dependent parameter for in-sample locations.

```
plot_spatial_param(
   out,
   parameter,
   loadings = 1,
   type = "mean",
   ci.level = c(0.025, 0.975),
   yearscale = TRUE,
   color.gradient = (grDevices::colorRampPalette(rev(RColorBrewer::brewer.pal(9, name = "RdBu"))))(50)
)
```

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Arguments

out	Output from BSTFA or BSTFAfull.
parameter	One of 'slope' (default), 'loading', or 'mean'.
loadings	If parameter='loading', an integer indicating which factor loading to plot.
type	One of mean (default), median, ub, or 1b indicating which summary statistic to plot at each location.
ci.level	If type='lb' or 'ub', the percentiles for the posterior interval.
yearscale	If parameter='slope', a logical scalar indicating whether to translate it to a yearly scale (TRUE; default).
color.gradient	The color palette to use for the plot. Default is colorRampPalette(rev(RColorBrewer::brewer.pal(9 name='RdBu')))(50).

Value

A plot of spatially-dependent parameter values for the observed locations.

Author(s)

Adam Simpson and Candace Berrett

Examples

```
data(out.sm)
attach(out.sm)
plot_spatial_param(out.sm, parameter='slope')
```

plot_trace

Plot trace plots

Description

Plot trace plots

```
plot_trace(
  out,
  parameter,
  param.range = NULL,
  par.mfrow = c(1, 1),
  density = TRUE
)
```

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Arguments

out	Output from BSTFA or BSTFAfull.
parameter	Parameter to plot. See BSTFA and BSTFAfull for parameter names.
param.range	Indices of the named parameter to plot. Default is to plot all relevant parameters.
par.mfrow	Vector of length 2 indicating the number of rows and columns to divide the plotting window.
density	Logical scalar indicating whether to include the density plot of the posterior

draws. Default is TRUE.

Value

A plot containing the trace plot (and density plot when density=TRUE) of the listed parameters.

Author(s)

Adam Simpson

Examples

```
data(out.sm)
attach(out.sm)
plot_trace(out.sm, parameter='beta', param.range=1)
```

predictBSTFA

Estimate/predict values of the time series at a specific location.

Description

Estimate/predict values of the time series at a specific location.

```
predictBSTFA(
  out,
  location = NULL,
  type = "mean",
  ci.level = c(0.025, 0.975),
  new_x = NULL,
  pred.int = FALSE
)
```

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Arguments

out	Output from BSTFA or BSTFAfull.
location	Either a single integer indicating the location in the data set to provide predictions or a vector of length 2 providing the longitude and latitude of the new location. If location=NULL (default), the function will return predictions for all in-sample locations.
type	One of all, mean (default), median, ub, or 1b indicating which summary statistic of the predicted values to return.
ci.level	If type='lb' or 'ub', the percentiles for the posterior interval.
new_x	If the original model included covariates \boldsymbol{x} , include the same covariates for prediction location.
pred.int	Logical scalar indicating whether to include additional uncertainty for posterior predictive intervals (TRUE) or not (FALSE; default – intervals represent posterior probabilities around the mean of location).

Value

A matrix or vector of estimated/predicted values for location.

Author(s)

Candace Berrett and Adam Simpson

Examples

```
data(out.sm)
attach(out.sm)
loc1means <- predictBSTFA(out.sm, location=1, pred.int=FALSE)</pre>
```

utahDataList	Utah Minimum Temperatures
--------------	---------------------------

Description

Zero-centered daily minimum temperatures averaged across 30-day windows from 1919 to 2014 across the US state of Utah; also includes dates, coordinates, and station names. Originally collected from the Utah Climate Center.

Usage

utahDataList

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Format

A data set with 4 variables:

TemperatureVals A 1251 by 146 matrix of zero-centered 30-day average daily minimum temperatures from 1912 through 2014. Missing observations are denoted using NA.

Dates A vector of length 1251 and class Date providing the day of each observation in the same order as the rows of TemperatureVals. Note that this package expects observation times to be regularly spaced.

Coords A 142 by 2 data frame containing the longitude (first variable) and latitude (second variable) of measured locations.

Locations A character vector of length 146 containing the station names for measured locations in the same order as the columns of TemperatureVals and the rows of Coords.

Source

https://climate.usu.edu

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